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Three-dimensional reactive transport simulation of Uranium in situ recovery: Large-scale well field applications in Shu Saryssu Bassin, Tortkuduk deposit (Kazakhstan)

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Abstract

Uranium in situ recovery (ISR) is the most widely used uranium mining technique worldwide. It consists of the dissolution of the ore by a mining solution, directly within the deposit. By predicting fluid flow and geochemical reactions in reservoirs, reactive transport (RT) modelling is a powerful tool to better understand and pilot ISR production. However, very few industrial uses have been reported thus far. This paper fills the gaps by illustrating a large-scale well-field application of RT modelling at one of the largest ISR mines worldwide, which is operated by Katco. This study highlights the robustness of a complex workflow based on the coupled reactive transport software HYTEC and its added value for the operator in the context of uranium ISR. The robustness demonstration is performed on 2394 wells covering 39 different production areas (blocks). The model reproduces the observed uranium concentrations and pH of pumped solutions over time scales up to 12 years. Only three parameters are manually adjusted to calibrate the model: global initial grades in clays (beidellite), calcite, and iron hydroxide (goethite). The discrepancy between simulated and observed uranium production and acid consumption decreases as the observation scale widens, showing that local errors compensate for each other. These deviations are mainly explained by the uncertainties of the 3D geological models and not by the RT simulations. Furthermore, the robustness of the model is a key asset for decision-making as it enables accurate predictions. This accuracy is illustrated through a case study of four of the simulated blocks. In 2019, after 10 years of production, the well field was redesigned to target the remaining uranium using the RT-based workflow. Several scenarios were simulated and sequentially optimised using a geometallurgical approach. The final adopted design predicted a 28% increase in uranium production and 35% in economic gains over the first two years of simulation alone (2019-2021). These theoretical gains were validated in practice as the comparison between the 2019 predictions and observations over 16 months showed a deviation less than 10% in the total uranium production, which decreased to 1.9% using the observed operational conditions, which reinforces the predictability of the workflow and validates the forecasted gains.

Keywords: In situ recovery, Uranium, Reactive transport, History matching, Optimisation, HYTEC

1. Introduction

In situ recovery (ISR), also known as in situ leaching (ISL) is currently the leading uranium extraction technique. From

less than 10% of the global production in 1997, it reached 46% in 2011 and increased to 57% in 2019 (OECD-NEA & IAEA, 2020). ISR consists of recovering uranium by direct leaching of the orebody without any mechanical action. This process is achieved by a structured network of injection and pumping wells, connecting the mineral deposit and the surface-processing plant. The network ensures the circulation of acidic or ba-

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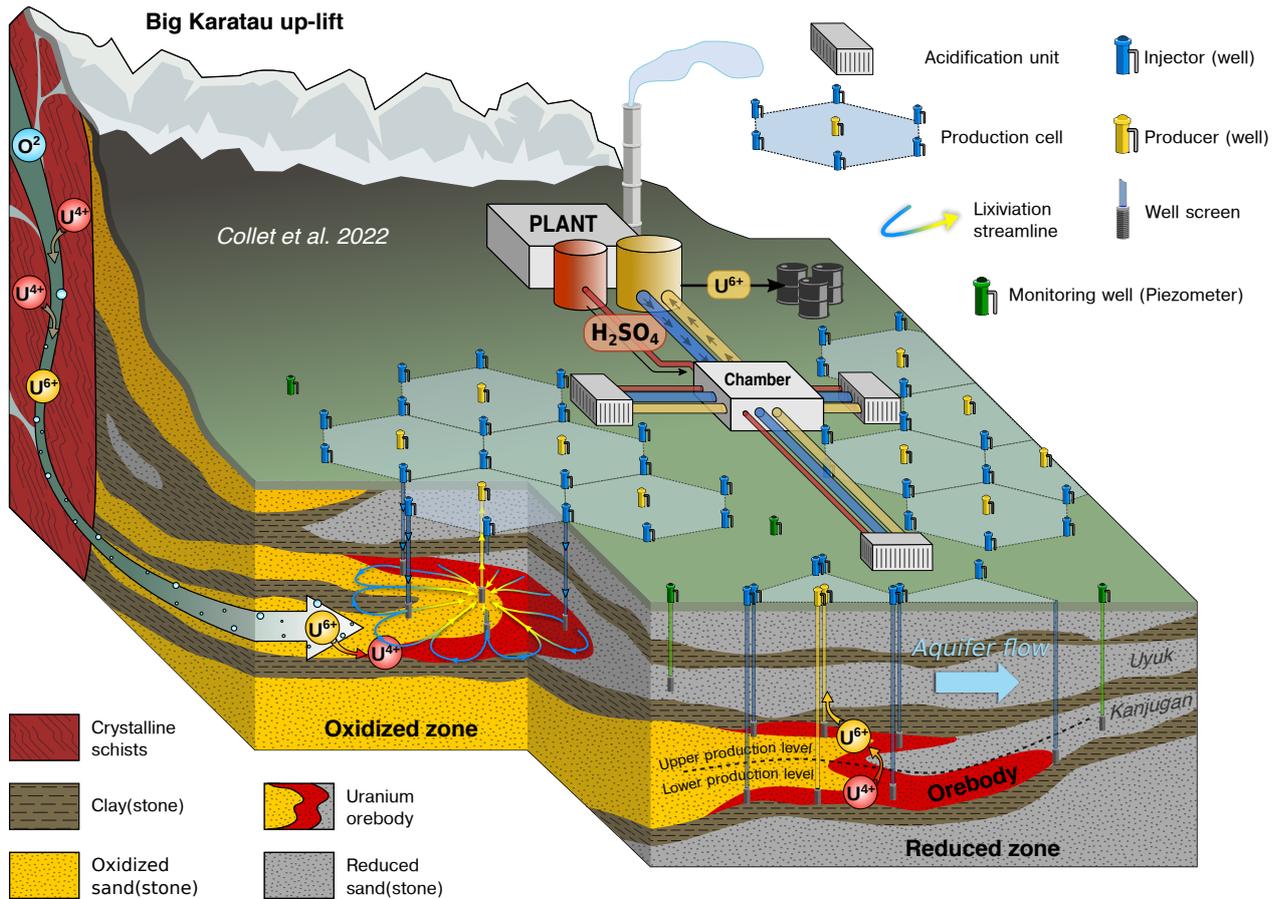


Fig. 1. Schematic view of the Katco Uranium In situ recovery (ISR) mine and the ISR process.

sic either-or oxidising solutions, increasing uranium mobility within the permeable deposit, which is pumped out towards the processing plant. Before being reinjected, the leaching solutions are restored by the additions of some chemical, e.g., acid

15 (IAEA, 2016).

The absence of mechanical extraction makes ISR by far the most cost-effective extraction technique (Kidd, 2009), and potentially more environmentally friendly (Taylor et al., 2004). Consequently, it is perfectly suited for large, deep and low-

20 grade sedimentary orebodies, where traditional open-pit and underground mining techniques are uneconomical (Dahlkamp, 2009; Kyser, 2014). The highly permeable and well confined roll-front deposits found in the USA, Uzbekistan and Kazakh-

25 stan are the archetypes of these deposits and currently dominate the global production (OECD-NEA & IAEA, 2020). Although this technique is characteristic of uranium mining, re-

cent studies highlighted a high potential for its use in extracting other commodities such as copper or gold (Sinclair and Thompson, 2015; Sereдкиn et al., 2016; Filippov and Hejny, 2017; Vargas et al., 2020). Hence ISR might be a fast-growing technology in the coming decades.

The economic potential and the technical challenges associated with ISR recently increased research interest. In particular, extensive literature has exposed the potential of reactive transport (RT) to investigate ISR (Nguyen et al., 1983; Nos, 2011; Martens et al., 2012; Johnson and Tutu, 2013; Ben Simon et al., 2014; Johnson and Tutu, 2015; Laurent et al., 2019). However, it is usually restrained to 1D laboratory experiments, such as column tests. In addition, the majority of ISR operations are conducted in post-Soviet countries (e.g., Kazakhstan), and a large number of publications are rarely accessible and published in Russian. Hence, only a few recent papers illustrate the

industrial usage of RT modelling in operations (Regnault et al., 2014; Noskov et al., 2018; Lagneau et al., 2018, 2019). In 2019, Lagneau et al. (2019) revealed the first results of the operational deployment of RT simulations at the Katco mine in Kazakhstan using the HYTEC RT simulator (van der Lee et al., 2003). They showed that an RT simulation based workflow reproduced the production history of one block (61 wells), a process known as history matching. They assessed the robustness of the model by applying it to another block in the vicinity, yielding equally good results. This paper documents the robustness of the same model by presenting the results obtained from 39 production blocks (2394 wells) in two independent reservoirs. This article represents a significant step-forward, placing RT history matching on the scale of what has been achieved in the neighbouring industry of oil and gas: industrial applications of non-reactive transport simulation coupled with history matching to drive the operations, allowing to increase the amount of oil and gas that can be extracted from existing resources (Oliver and Chen, 2011; Rwechungura et al., 2011; Udy et al., 2017). In addition, the literature mentioned the main applications of a robust RT-based workflow as short-term planning (Lagneau et al., 2019), long-term planning (Langanay et al., 2021) and environmental permitting through impact monitoring and post-operation remediation (Coral et al., 2018; de Boissezon et al., 2020). The present paper extends these results by presenting a real short-term well field optimisation case study that illustrates the geometallurgical approach and the economic benefits possible when managing the end of life of production areas with an RT-based workflow.

This paper is organised as described below. After providing a brief description of the Katco uranium mine, the first section presents the ISR modelling process with HYTEC. It includes the description of the workflow inputs (3D geological models, geochemical model, and operational conditions), and the presentation of modelled areas. Section 3 describes the history matching and case study results. Finally, Section 4 discusses limitations and perspectives on the robustness of the workflow and the history matching process, the importance of operational

conditions in forecasts, and finally, the industrial capacity of the workflow.

2. Materials and methods

2.1. Katco Mine

Created in 1996, Katco JV LLP is a joint venture mining company between Kazatomprom (49%) and Orano Mining (51%), which are the Kazakh and French national nuclear fuel cycle companies, respectively. With a yearly production ranging from 3200 t to 4000 t since 2009, corresponding to 7% of the global uranium production in 2019 (OECD-NEA & IAEA, 2020), Katco remains the largest in situ recovery (ISR) uranium mine worldwide (Lagneau et al., 2019). The mine, located in the Shu Saryssu Bassin - Kazakhstan, exploits the Tortkuduk and Muyunkum deposits along a southwest-northeast axis over 40 km in length. It currently operates this large territory in an acidic way thanks to processing plants, each of which is connected to the deposit by a well field.

2.1.1. Well field description

A well field is a large network of wells, that connect the processing plant to the orebody. Figure 1 schematically illustrates the organisation of one of the well fields sustaining the ISR process. The wells are arranged in hexagonal patterns with a radius of 40 m on average at Katco. At the hexagon vertices, injection wells (injectors) introduce the leaching solution to the orebody. Production wells (producers) are placed at the centre of the hexagons and deliver the pregnant solution to the processing plant. This pattern, referred to as "seven spots", ensures good circulation of the solutions through mineralisation and hence results in more effective leaching (Ward, 1983; Shao-Chih, 2008). Each hexagon is called a production cell and is considered a unit of extraction covering 4150 m² of the deposit. Due to the reservoir thickness, vertical overlapping up to three levels of wells is frequently required to intersect mineralisation. (Figure 1). In addition, the wells are frequently redrilled when the initial well is clogged or to locally accelerate the leaching process.

The hydraulic network connecting the plant to the wells (Figure 1) is organised in three subsets. First, a primary network of pipelines, named primary lines, links the plant to pump houses called transit chambers. Then, a second level of pipelines, called secondary lines, links these chambers to well houses referred to as acidification units. Finally, the acidification units connect the secondary lines to each well individually through a third network of buried pipes. An acidification unit is usually linked to a dozen production cells composed of approximately 45 injectors and 15 producers. This group of cells is called a production block. The mine currently operates 80 production blocks at any given time.

2.1.2. Production management

Four key indicators are used to manage the production and optimise the reservoir response. On the one hand, flow rates (injected and pumped) and added acid volumes are the two levers the operators use to adjust the production. On the other hand, the pH and uranium concentrations of pumped solutions allow us to calculate uranium production and acid consumption, from which the economic performance of the mine is derived. Therefore, accurate and regular knowledge of these four process data is critical.

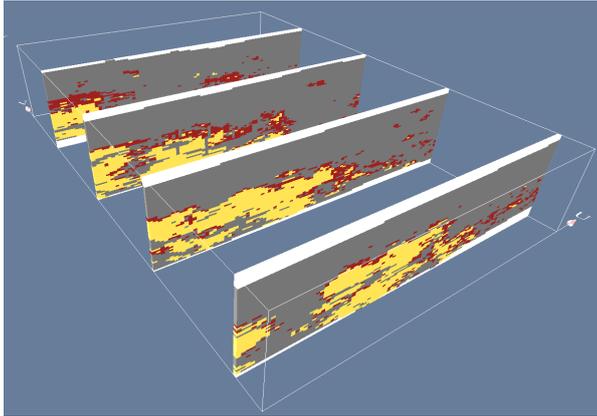
Each well and line are equipped with a flowmeter to monitor the flow rates, whose cumulative values are read every 24 h. The pregnant solutions from the producers and production lines are sampled and analysed on the same daily basis, providing the uranium concentration and pH. A systematic correction workflow is applied to make the measured data consistent with the basic conservation principles. First, outliers are removed using a combination of Hampel (Hampel, 1974; Liu et al., 2004) and other median-based filters (see Gonzalo, 2004). Then, missing values and mass conservation are addressed using a dynamic mass balance reconciliation method performed at the acidification unit scale. The process exploits the measure redundancy between wells and lines and is based on an unscented recursive nonlinear dynamic data reconciliation scheme (Vachhani et al., 2006) which is an adaptation of unscented Kalman filters,

(Julier and Uhlmann, 2004). This workflow is complemented by a systematic visual quality assurance before using the data.

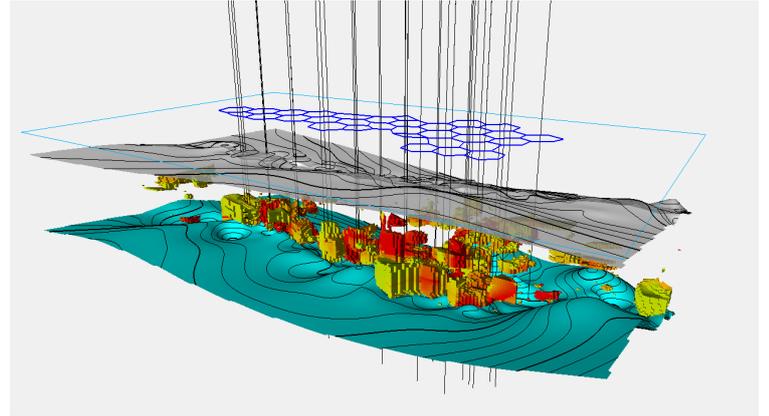
Regarding composition of the pregnant leach solution, the transit of the pumped solutions through the processing plant before being reinjected induces a homogenisation of the concentrations (Nos, 2011). Consequently, these concentrations are sampled at the outlet of the plant and considered identical for the entire well field connected to the plant. Sampling was performed twice a day and the following major species were measured: Al^{3+} , Ca^{2+} , Cl^- , H_2SO_4 , Fe^{2+} , Fe^{3+} , K^+ , Mg^{2+} , PO_4^{3-} , SO_4^{2-} , UO_2^{2+} . The final acidity of injected solutions is calculated using the baseline concentration from the plant, complemented by the added acid in the acidification unit (one of the operational levers previously discussed).

2.2. Reactive transport workflow for ISR at Katco Mine

The RT simulations (Lichtner et al., 1996; Steefel et al., 2005; Druhan and Tournassat, 2019) allow us to model and understand the coupled hydrodynamic and geochemical processes that occur within the aquifer during ISR operations. All RT simulations presented in this study were performed using the code HYTEC developed at Mines ParisTech (van der Lee et al., 2003). The HYTEC program provides a general multipurpose flexible framework for solving complex hydrogeochemical problems (Lagneau and van der Lee, 2010; Steefel et al., 2015). The code was successfully employed in benchmark studies (Carrayrou et al., 2010) and various applications, e.g., cement degradation (De Windt and Devillers, 2010; Seigneur et al., 2020), and geological storage of acid gases (Sin and Corvisier, 2019). The workflow developed using HYTEC for the ISR simulation has already been extensively described by Lagneau et al. (2019). Consequently only major elements of the workflow relevant to this study are presented below i.e., input parameters and modelled areas. The designed RT-based workflow requires three types of input parameters (Regnault et al., 2014; Langanay et al., 2021). First, a 3D geological block model, which contains the hydrodynamic parameters and the mineralogical description of the reservoir. Second, a geochem-



(a) Cross-sections of the ISATIS 3D model used for primary line E, showing the discrete oxidised-mineralised-reduced redox facies. As in Figure 1, O=yellow, M=red and R=grey.



(b) View of the PETREL 3D model used for blocks G1 and G2. The surfaces represent the top and bottom of the Uyuk Reservoir and the coloured voxels represent the uranium grades obtained by ordinary kriging (Olea, 1999, p.7-30).

Fig. 2. Examples of 3D block models.

ical model gathers the description of undergoing geochemical processes and the associated mineralogical database. Finally, the operational parameters, i.e., the well screen positions, the injected and pumped flow rates, and the chemical composition of the injected fluids, are input.

2.2.1. 3D geological block models

All 3D geological models used for the simulations were built from the same type of input data, and possess the same structure, to ensure a consistent representation of the Muyunkum sandstone roll-front (Petrov, 1998; Dahlkamp, 2009, 241-253). A 3D geological model consists of the reservoir discretised into a 3D grid of rectangular parallelepipedal voxels. The grid mesh size used (x, y, z) was (5 m, 5 m, 1 m) or (10 m, 10 m, 1 m). This grid held three geological properties. First, a two-class discrete lithological property discriminates the permeable (i.e., sandstone) from the impermeable facies (i.e., massive clays and carbonate layers). In HYTEC, these facies were associated with homogenous permeabilities of 1×10^{-4} m/s and 1×10^{-10} m/s for permeable and impermeable facies, respectively. For porosity, a unique value was used for each reservoir: 23% and 18% for Uyuk and Kanjugan, respectively (Figure 4). Second, the roll-front is represented by a discrete variable of three redox classes referred as OMR facies (Petit et al., 2012; Langanay

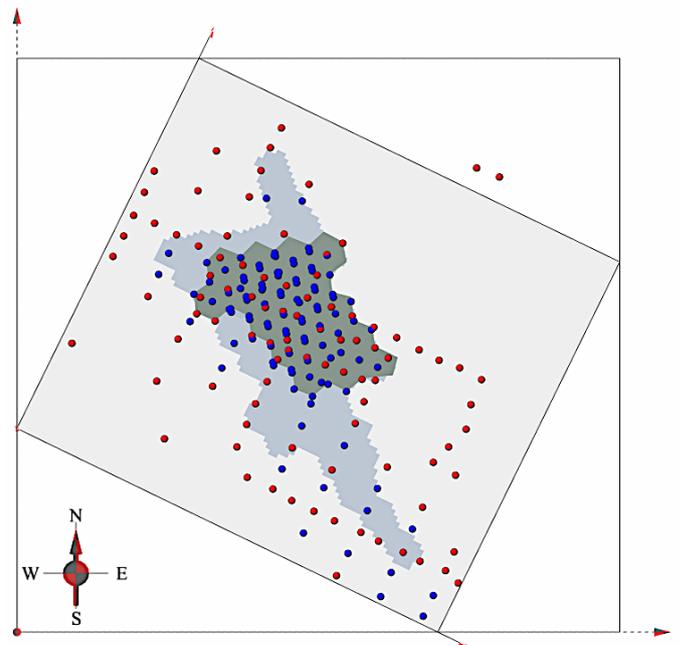


Fig. 3. Spatial distribution of the drill holes used to build the 3D model of primary line A. The red dots are the exploration and development drill holes (ED) while the blue dots are the drill holes added after the drilling campaign in blocks A1 and A2 (mostly technological wells). The light-grey polygon shows the total extent of the primary line A, while the dark grey polygon shows the extent of blocks A1 and A2.

et al., 2021). Uranium mineralisation (M) is observed at the interface between the downstream reduced facies (R) and the

oxidised upstream facies (O) of the reservoir (Figure 1 and Figure 2a). A homogenous dedicated mineralogy is defined for each facies. Third, the uraninite and coffinite accumulations are represented as a scalar field (Figure 2b). The input data available to build the models are the core description, core analysis (X-ray fluorescence) and drill hole logging (resistivity and gamma ray).

Although consistent input data were used to build all 3D geological models, the number of drill holes available to constrain the model varied depending on the area. Indeed, for each area of the mine, two datasets were available from the different drilling campaigns. The first available set corresponds to the exploration and development drill holes, which are required to characterise the deposit and to build the well field design (production cells and screen positioning). The usual drill spacing observed is 100 m by 50 m (200 – 250 drill holes per km²). The second is obtained from the drilling of technological wells, prior to the start of extraction. The 40 m diameter hexagon cell design provides much denser coverage (> 650 drill holes per km²). Consequently, the geological model constraints used for a model mainly depend on the moment the model was built, in regard to the available data at that time. Figure 3 illustrates the spatial distribution of the drill holes used to build the block model covering the primary line A. The distribution of the ED wells is not homogenous and the technological well data included cover blocks A1 and A2. Furthermore, in this article, the models built only with exploration and development drill hole data are referred to as ED while those built on top of the technological wells are referred to as EDT.

In addition to the number of available drill holes, the modelling process differed as two geostatistical methods were employed. The first is a stochastic based method and relies on the one hand on plurigaussian simulations for the discrete variables (Fontaine and Beucher, 2006; Langlais et al., 2008; Renard and Beucher, 2012), and, the other, relies on block simulation for the uranium grades scalar field. The models were built using ISATIS software combined with the R-geostats package (MINES ParisTech / ARMINES, 2021), based on the workflow

described by Petit et al. (2012). The second approach is deterministic and relies on simple kriging of indicators for the facies and on punctual ordinary kriging for the uranium grades (Olea, 1999, 7-30). In that case, the models were built within the PETREL software (Schlumberger, 2018; Suslov and Vaynerman, 2020). The main difference between the two approaches is that the first method preserves the geological variability while the second method tends to smooth it.

The effects of drill hole density and geostatistical methods are investigated later in this study.

2.2.2. Geometry and operational conditions of the well field

The geometry and operational conditions used for the simulations were provided at the well scale. For each well, geometry was defined using 2 parameters: coordinates of the well head and the vertical position of the well screen. The flow rates and composition of leaching solutions were defined on a daily basis using the data mentioned in Section 2.1.2.

2.2.3. Geochemical model

The geochemical model employed is derived from previous studies that identified the reactive mineralogy of uranium-bearing sandstone in the Shu-Saryssu basin (Yefteyeva, 1986; Petrov, 1998; Ben Simon et al., 2014; Robin et al., 2015, 2016). The kinetic and mineral databases as well as the underlying chemical processes used for the simulations were described previously (Lagneau et al., 2019, and references therein), and are briefly recapitulated below.

The geochemical model relies on six minerals: cristobalite alpha, kaolinite, smectites (beidellite), calcite, iron hydroxides (goethite), and uraninite.

On the one hand, the acidification of the aquifer is described in a straightforward manner through H₂SO₄ injection and reactivity with calcite, beidellite and goethite using equations 1, 2 and 3, respectively (Robin et al., 2016; Lagneau et al., 2019).

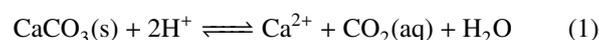
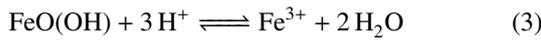
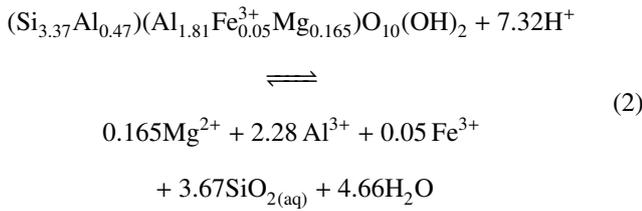


Table 1

Characteristics of the modelled primary lines.

	Size			3D model		
	Nb. blocks	Nb. cells	Nb. wells	Software used	Datasets used	Meshsize
A	4	53	199	Stochastic	partial EDT	10x10x1m
B	6	79	343	Stochastic	ED	5x5x1m
C	4	58	277	Stochastic	ED	5x5x1m
D	4	71	303	Stochastic	ED	5x5x1m
E	4	47	215	Stochastic	EDT	5x5x1m
F	4	62	275	Deterministic	EDT	5x5x1m
G	5	70	316	Deterministic	EDT	5x5x1m
H	6	71	334	Deterministic	EDT	5x5x1m
I	1	17	88	Deterministic	EDT	5x5x1m
J	1	10	44	Deterministic	EDT	5x5x1m
Total	39	538	2394			



On the other hand, the leaching of the U(IV) mineral phase (uraninite) is controlled by oxidative dissolution (Eq.4) by Fe^{3+} , which is first derived from the reactions with gangue minerals described previously, as well as recirculation of Fe^{3+} from the well field. Gangue minerals play a major role since they both control the pH and provide the oxidiser.



2.2.4. Modelled areas

As shown in Table 1, history matching work was performed on 39 production blocks from ten different primary lines, including 538 production cells composed of 2394 wells (1744 injectors and 650 producers). The primary lines are labelled

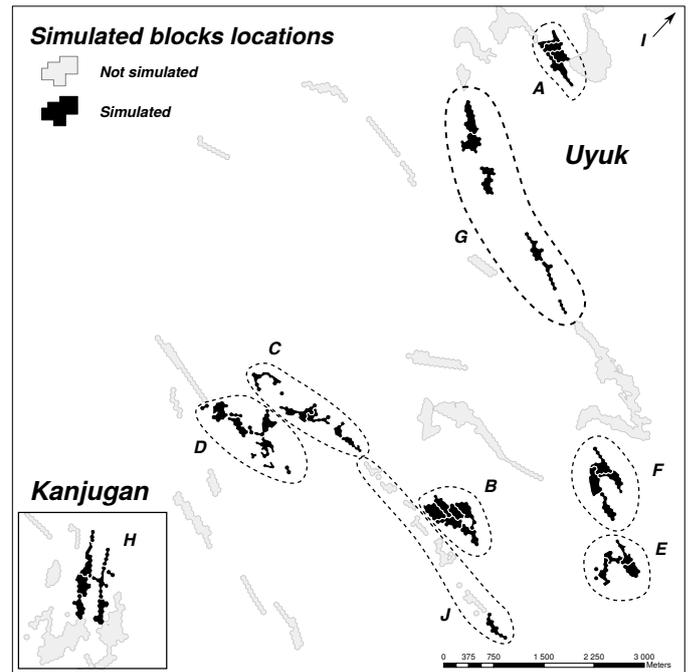


Fig. 4. Location of the simulated technological blocks. The primary line I, located north, is composed of four isolated blocks that are not displayed on the map.

from A to J, to be consistent with Lagneau et al. (2019). Their respective blocks are additionally assigned a number ranging from one to n . As a result, compared to Lagneau et al. (2019),

A1 and A2 retain the same name while block B becomes B4.

The location and geometry of the blocks are shown in [Figure 4](#). The choice of these 39 blocks is based on the availability of 3D geological models. The 3D geological models used were composed of (5 m, 5 m, 1 m) meshes covering the block surface with a 100 m lateral extension. Due to the variety of mineralisation shapes ([Figure 4](#)) and reservoir thickness, grids sizes ranged from 250 k to 800 k voxels with an average of 525 k voxels. Only primary line A was simulated at once, employing an upscaled grid of (10 m, 10 m, 1 m), resulting in a 1.2 M voxel grid.

2.3. Reservoir history matching

2.3.1. Concept

Of the four production management indicators listed in [Section 2.1.2](#), the operator does not directly control the acid and uranium concentrations of the pumped solutions. The main expectation of the operator with respect to a numerical model is therefore the correct prediction of these two state variables. History matching is the process of building one or more sets of models that account for the observed reservoir behaviour. It is a type of inverse problem which consists of an attempt to adjust some of the reservoir model parameters to better reproduce the state variables of interest observed in the past, taking into account the real operational conditions imposed on the reservoir. The greater the agreement among the forecasts, the more predictable the model ([Oliver and Chen, 2011](#)). In practice, we choose to adjust parameters for which we have a limited knowledge, and for which the state variables display sufficient sensitivity ([Yeh, 1986](#); [Carrera et al., 2005](#)).

2.3.2. Adjusted parameters and methodology

Three geochemical parameters were adjusted to fit the observed data: initial grades of beidellite (a single value for the three redox facies), grades of iron hydroxides in the oxidised facies and, finally, grades of calcite in the mineralised facies. The choice of these three parameters was motivated both by internal studies that showed their spatial variability, and by the

limited data available. All other parameters remained constant among the simulations and were described by [Lagneau et al. \(2019\)](#) (as detailed in [Section 2.2.3](#)).

Parameters adjustment followed an iterative process. For the simulation of a new block, the grades used for the closest calibrated block were established as a starting point and used in a first run. The results were compared to the observed data at the block scale, and the pH was adjusted by manually increasing or decreasing the beidellite grade, repeating the process until a satisfactory fit was obtained. The same principle was then applied to the calcite grade to fit the initial decrease in pH (~ 30 first days) and finally to the iron hydroxide grade affecting the rate of uranium dissolution during the first year.

2.3.3. Fit accuracy metrics

As explained by [Lagneau et al. \(2019\)](#), the necessity for the operator to produce reliable mining plans in both short and long terms prompts interest in block performance projections at different temporal and spatial scales. However, a long-term mining plan requires a good overall estimation of uranium production and acid consumption at the primary line scale i.e., cumulatively over long times; short-term planning demands a correct estimation on a monthly to weekly basis and at the block or cell scale. A good production model is therefore expected to provide both. Thus, the qualification of predictive models involves the adaptation of metrics allowing the intercomparison of different variables (acid and uranium concentrations), observed at various temporal (yearly and daily) and spatial (primary line, block, and well) scales. The two metrics applied in this paper are the log relative deviation (LRD) and the mean absolute scaled error (MASE).

The LRD has been used to assess the final deviation of the cumulated uranium production and acid consumption, as an alternative to the classic relative change (RC). They are defined in [equation 5](#) below:

$$RC(\gamma, \bar{\gamma}) = \frac{\gamma - \bar{\gamma}}{|\bar{\gamma}|} \quad LRD(\gamma, \bar{\gamma}) = \ln\left(\frac{\gamma}{\bar{\gamma}}\right) \quad (5)$$

where γ and $\bar{\gamma}$ are the simulated and the observed data, respectively. In both cases a positive relative change indicates that

$\gamma > \bar{\gamma}$, i.e., the simulation overestimates γ and vice versa. The reason for using the LRD rather than another indicator (i.e. the RC) is that it is a symmetric, additive and normed relative change metric (Törnqvist et al., 1985). Indeed, the RC is bounded to the interval $[-1, +\infty[$, where γ being null or positive, and possibly infinitely superior to $\bar{\gamma}$. With RC, the negative and positive deviations would not be treated in the same manner, e.g., a cell with an observed production of 10 t and a 5 t simulated cell has an RC of -50% while the opposite, a cell with an observed production of 5 t and a 10 t simulated cell has an RC of $+100\%$. In the case of the LRD, however, the previous example produces symmetric values of -30.1% and $+30.1\%$ respectively.

In addition to the LRD, the MASE has been used to capture the instantaneous deviation and score the fit quality over the full simulation. Among the many measures proposed in the literature for evaluating the forecasting performances of different methods (Hyndman and Koehler, 2006; Kim and Kim, 2016), the MASE, introduced in 2006 by Hyndman and Koehler, has proven to possess good mathematical properties, defined mean, finite variance and scale independence (Franses, 2016). The MASE is now a well-established metric (Makridakis et al., 2020) as it overcomes most of the bias occurring when comparing method performances on different datasets. It is defined as the mean absolute error (MAE) for the predicted values, scaled by the MAE of a simple one-step "naive forecast method", which consists of shifting the values one step backward (one step equals one day in our case):

$$\text{MASE} = \frac{\frac{1}{n} \sum_{i=1}^n |\gamma_i - \bar{\gamma}_i|}{\frac{1}{n-1} \sum_{i=2}^n |\bar{\gamma}_i - \bar{\gamma}_{i-1}|} \quad (6)$$

where $\gamma_i - \bar{\gamma}_i$ is the simulation error for the sample i , and n is the number of samples in the time series.

This metric should be understood as follows: a MASE of 0 equals a perfect fit; a MASE of 1 equals a fit as good as the one-step "naive forecast method"; and a MASE of n , n times worse, e.g MASE of 10 indicates a 10 times higher MAE. The

U and acid concentration evolution being continuous and rather smooth, as shown in the results section (e.g., Figure 5), a MASE should be visually appreciated as an almost perfect match in the interval $[0, 2]$, as very good in $]2, 3]$, as good in $]3, 5]$, acceptable in $]5, 7]$ and poor beyond.

2.4. End of block life management

The capacity to predict future reservoir performance is a key aspect of history matching and constitutes the true usefulness of an RT-based workflow. The ability to forecast the reservoir response to operational conditions with increased confidence indeed allows operational experiments to be performed to optimise the well field management. The end of block life management is one of these optimisation applications.

2.4.1. Concept

As a production area ages, uranium reserves are gradually depleted and therefore the uranium concentration of pumped solutions globally decreases. Below a certain concentration cut-off, production cells are systematically stopped, until the production block itself is closed. The spatial distribution of uranium is very uneven, and while many cells are depleted, some cells nevertheless still offer high potential and can be exploited. Managing the end of block life consists, on the one hand, of determining which areas must remain active and, on the other hand, of optimising the design with well re-drillings.

2.4.2. Primary line A end of life

In 2019, Collet et al. introduced an HYTEC-based optimisation methodology for the final stage of uranium recovery in old production blocks. This paper presents its implementation in a real case study based on primary line A. The methodology follows an iterative process. As a first step, a careful history matching is performed to adjust the model parameters (see Section 2.3). This step reinforces the predictivity of the model and provides access to the location of the remaining uranium in the deposit. The location of uranium at the end of extraction determines the choice of production cells to retain for the next

step. As a second step, a forecast simulation estimates the metallurgical response of each cell, which does not depend solely⁴⁷⁵ on uranium grades. Based on these data, the design is sequentially optimised by well re-drillings and different acidification strategies. The final outcome is the implementation of the most profitable design and acidification strategies in the well field.

3. Results

3.1. History matching

3.1.1. Uranium production

Figures 5 and 6 show the observed uranium production curves⁴⁸⁵ against the simulation results for the eight primary lines (see 2.2.4) and four blocks of interest respectively. Interestingly, all primary lines and blocks presented in this paper produce a large⁴⁹⁰ range of uranium extraction curves. This is due to several factors. First, the blocks of a primary line are usually exploited sequentially, e.g., for primary line E in Figure 5, each peak corresponds to a block start. This plays a major role in the production profile at the line scale but also at the block one,⁴⁹⁵ as the blocks that started later benefit from the acidification of the first blocks to be operated. Second, as studied by Lagneau⁴⁹⁵ et al. (2019) and Langanay et al. (2021), the local distribution of uraninite and the geometry of the reservoir (Figure 4) vary from one area to another and it has a great impact on arrival and⁴⁶⁰ height of production peaks, and shapes of descending slopes. Third, these diverse production profiles are explained by the⁵⁰⁰ modification of the operational conditions with time, i.e., the acidity of the leaching solutions and the flow rates. Although some blocks such as E2 exhibit an intense initial acidification⁴⁶⁵ followed by a constant decrease, other assets, as illustrated by blocks B1 and F1, undergo multiple acidification campaigns,⁵⁰⁵ sometimes carried out with cell additions and closures. In addition, some areas, particularly for the Kanjungan deposit, are⁴⁷⁰ prone to clogging, requiring many workovers and cleaning actions to maintain a sufficient flow rate. This phenomenon is characterised by sawtooth wave production profiles, each peak⁵¹⁰ matching a well cleaning campaign. It is clearly observed at

primary line H in Figure 5, and specifically at block H5 in Figure 6.

Despite the very different behaviours of blocks and primary lines, the model systematically manages to reproduce the trend and is usually very close to the production data, for both the instantaneous and cumulative extraction. This result indicates the robustness of the workflow to account for the geological and geochemical spatial variability and its capacity to accurately predict the response of the reservoir with respect to the various operational conditions imposed by the operator.

According to Lagneau et al. (2019), the misfit between the model and the observed data is largely due to the uncertainties in the geology and, more specifically, in the uranium distribution. This explanation has been sustained by the study of the effects of the geological uncertainties on the simulated uranium recovery performed by Langanay et al. (2021). Additionally, Lagneau et al. (2019) argue that the block size is well above the range of constraints for the geostatistical model, and the uncertainty is globally averaged at the block scale. The results of the statistical study of the misfit shown in Figure 7 validate these assumptions. The univariate statistics of the LRD and MASE for uranium and acid production examined three spatial scales of interest: primary line, block and cell. Since a single block was modelled for both primary lines J and I (Table 1), their results were considered at the block scale and not at the primary scale. The LRD of the total uranium produced follows a quasi-normal distribution approximately centred at zero for all scales, which implies that the underestimations and overestimations globally compensate. Additionally, the smaller the scale is, the higher the distance of the distribution mean and median from zero and the higher the standard deviation of the misfit ($2.3 \pm 14.0\%$, $8.6 \pm 28.7\%$, $25.8 \pm 69.9\%$ for primary lines, blocks and cells, respectively). This finding indicates a larger range of errors and worse fits overall, due to the larger discrepancy between the geological model and reality. The confidence of the results produced by the model at the cell scale is then much lower. A similar result is obtained for the MASE. The average MASE at the primary line scale is 4.0 ± 1.9 , which is considered

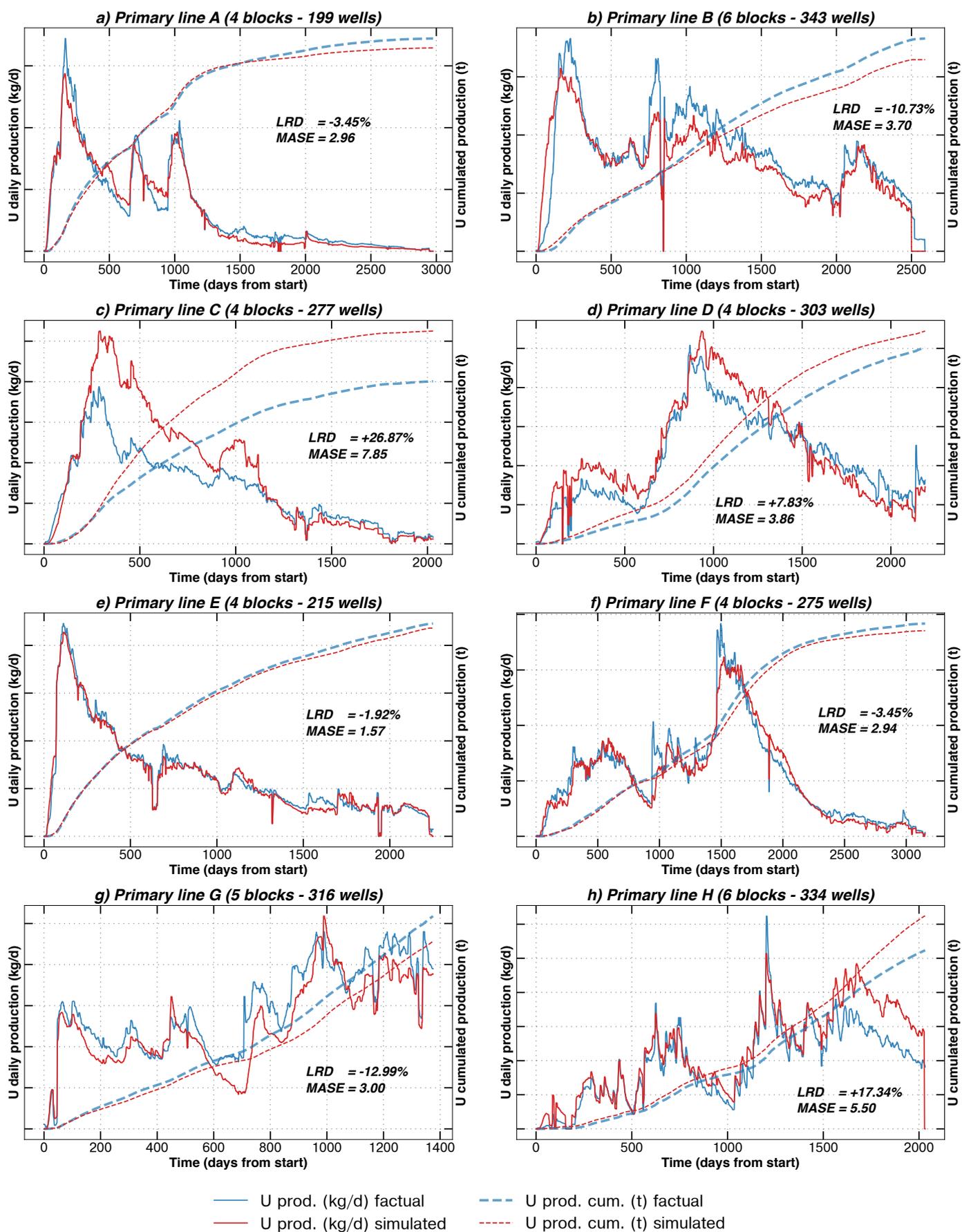


Fig. 5. History matching results of uranium production at the primary line scale. For visualisation, the daily values are smoothed by median filtering with a 3-day window. LRD is the logarithmic relative deviation, and MASE is the mean absolute scaled error.

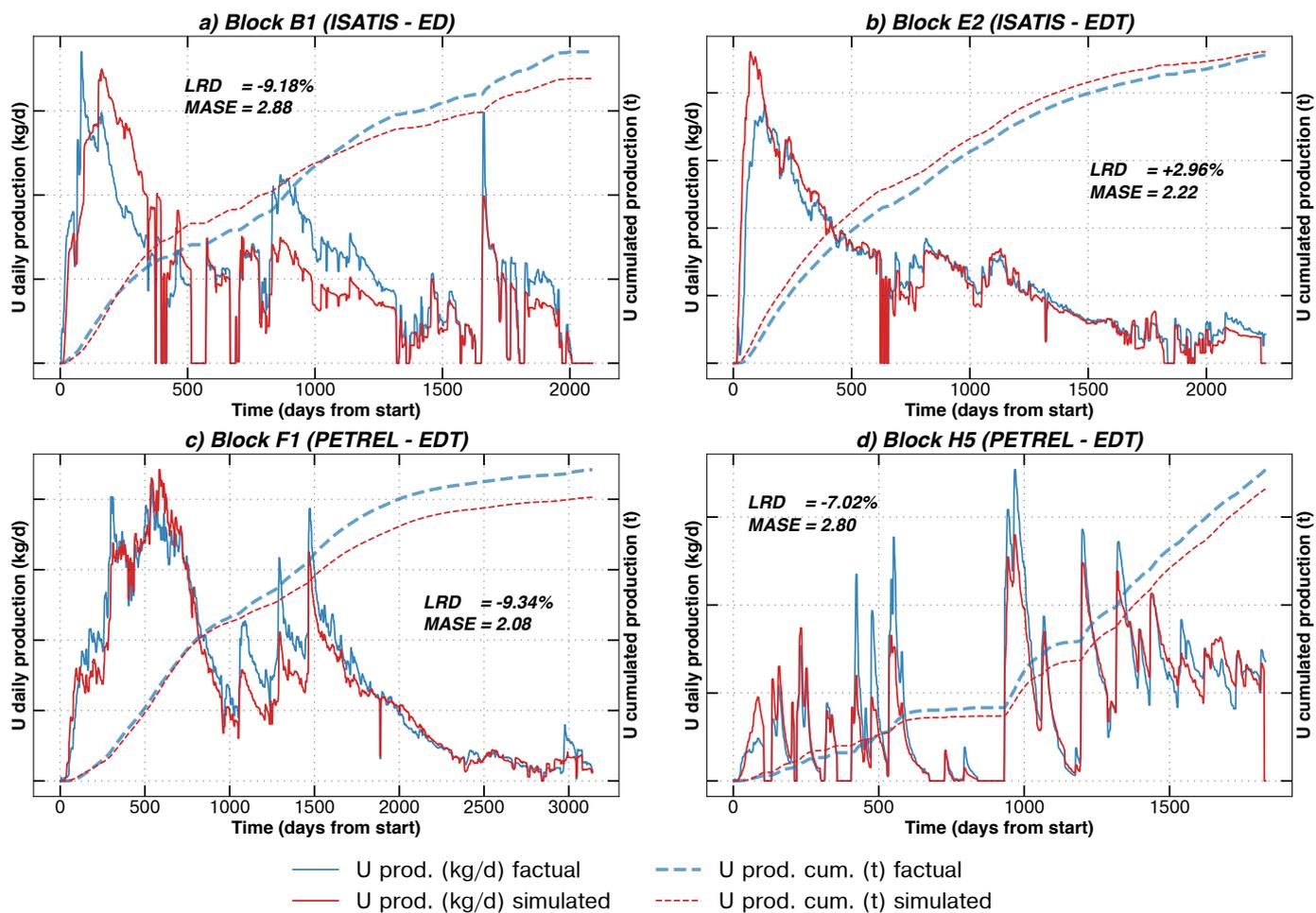


Fig. 6. History matching results of uranium production at the block scale.

good. It increases to 5.8 ± 5.2 at the block scale and more than doubles (9.7 ± 9.3) at the cell scale with a standard deviation 4.5 times higher than at the primary line scale.

3.1.2. Acid consumption

Figure 8 shows the history matching results for the pumped solution pH and the corresponding back calculated acid recovery for the blocks G2, E3, H2 and H5. For uranium, and for the same reasons (see Section 3.1.1), the profiles vary substantially from one block to another. However, unlike uranium, the acidity fit results in alternate intervals when the data are correctly matched and intervals with important LRDs. This fit is particularly acute during the first year of production ($80.1 \pm 62.1\%$) because the model relies on the acidic dissolution of the smectites but ignores the ion-exchange reactions that play a major role

in acid consumption (Robin et al., 2016, 2020). This choice is mainly motivated by technical reasons, as incorporating sorption processes would be very CPU-intensive.

The results on the 39 blocks show that the intervals can be classified into three classes (Figure 8):

- The first one coheres to the first year of production (± 50 days). In addition to clay dissolution, a large quantity of protons are sorbed in the smectite interlayer space, lowering the acidity of the leaching solutions. The simulation systematically underestimates the acid consumption during this phase.
- The second class corresponds to intervals observed after the first year of extraction, when the pH remains below 2.1 (~ 0.93 g/L of H_2SO_4 dissolved) for a sufficiently

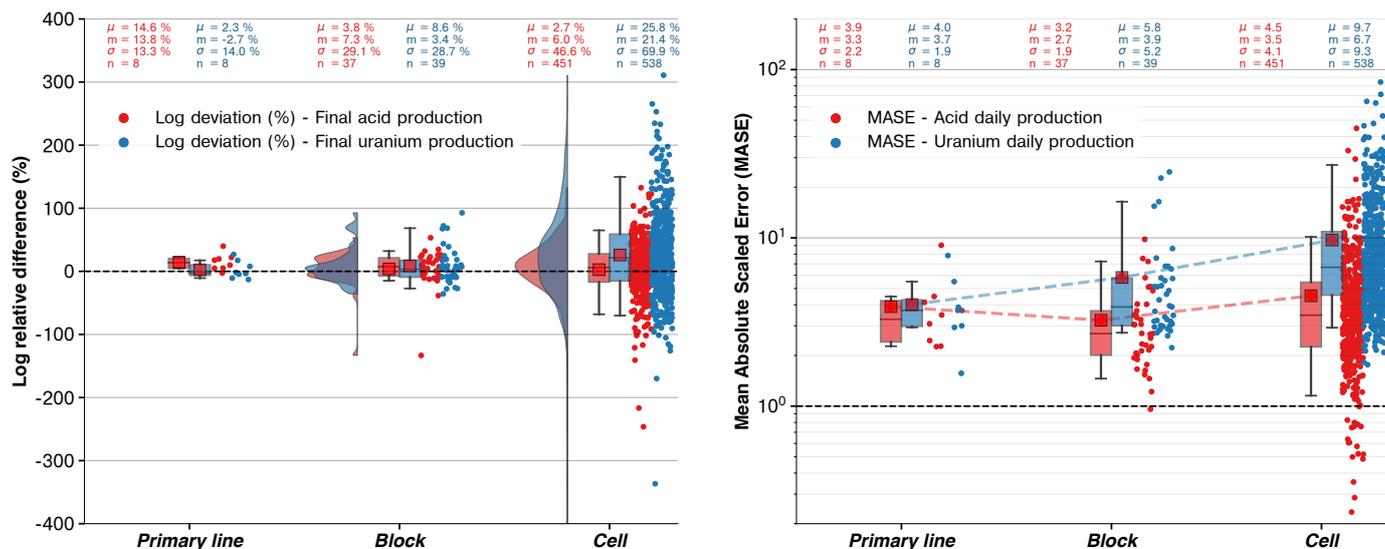


Fig. 7. Log relative difference (fact vs. simulated) and mean absolute scaled error (MASE) of the uranium and acid production predictions per scale of interest. The boxes show the interquartile range (Q3-Q1) of the dataset while the whiskers extend to show the p5-p95 of the distribution. The red squares represent the mean values. μ is the average, m is the median, σ is the standard deviation and n is the number of samples.

540 long time (~ 50 days). These intervals are shown as vertical grey bands in Figure 8. In that case, the sorption sites of the clay are fully saturated with protons, and clay dissolution controls acid consumption. Hence, the model very accurately reproduces the pH evolution with respect to the operational conditions (acidity of the leaching solution) at times up to 1500 days (e.g., block E3 in Figure 8.b).

- 550 • Finally, a third type of interval alternates with the previous one interval when the pH exceeds 2.1. They are characterised by an overestimation of the acid consumption by the model due to proton desorption from the clay which increases the acidity of the pumped solution.

The systematic discrepancy between the observed data and the model for the first year of production increases the difficulty of estimating the acid consumption during this period. However, proton desorption is a very slow process occurring over very long times (de Boissezon et al., 2017; Lagneau et al., 2019), and the misfit observed after the first year of extraction is very small, even when the pH exceeds 2.1. This finding is especially true since a block reaches a pH of 2.1 only when its

acidification has been stopped. Thus, the pregnant leach solution from the plant is not complemented with additional acid and the block shows very low acid consumption. Therefore, the model provides a good estimate of the acid consumption after the first year of production and can be used as a predictive tool in operation.

Practically, the calibration of the beidellite content to fit the observed data has been achieved by only examining the intervals when the model correctly reproduced the acid consumption (class 2). However blocks with a short history do not show any intervals of class 2 which makes calibration impossible, which is the case for blocks J1 and E4, as well as 87 cells ($\sim 16\%$ of the 538 cells considered in the study). This result explains why these blocks and cells were not included in the statistical study for acid consumption and why the number of samples n displayed between uranium and acid cases differs in Figure 7 and between Figure 9 and Figure 10.

Statistical analyses of acid consumption show the same trend as the uranium fit. The final deviations follow a quasi-normal distribution, centred at zero, with a standard deviation increasing when the scale diminishes. The mean MASE also increases

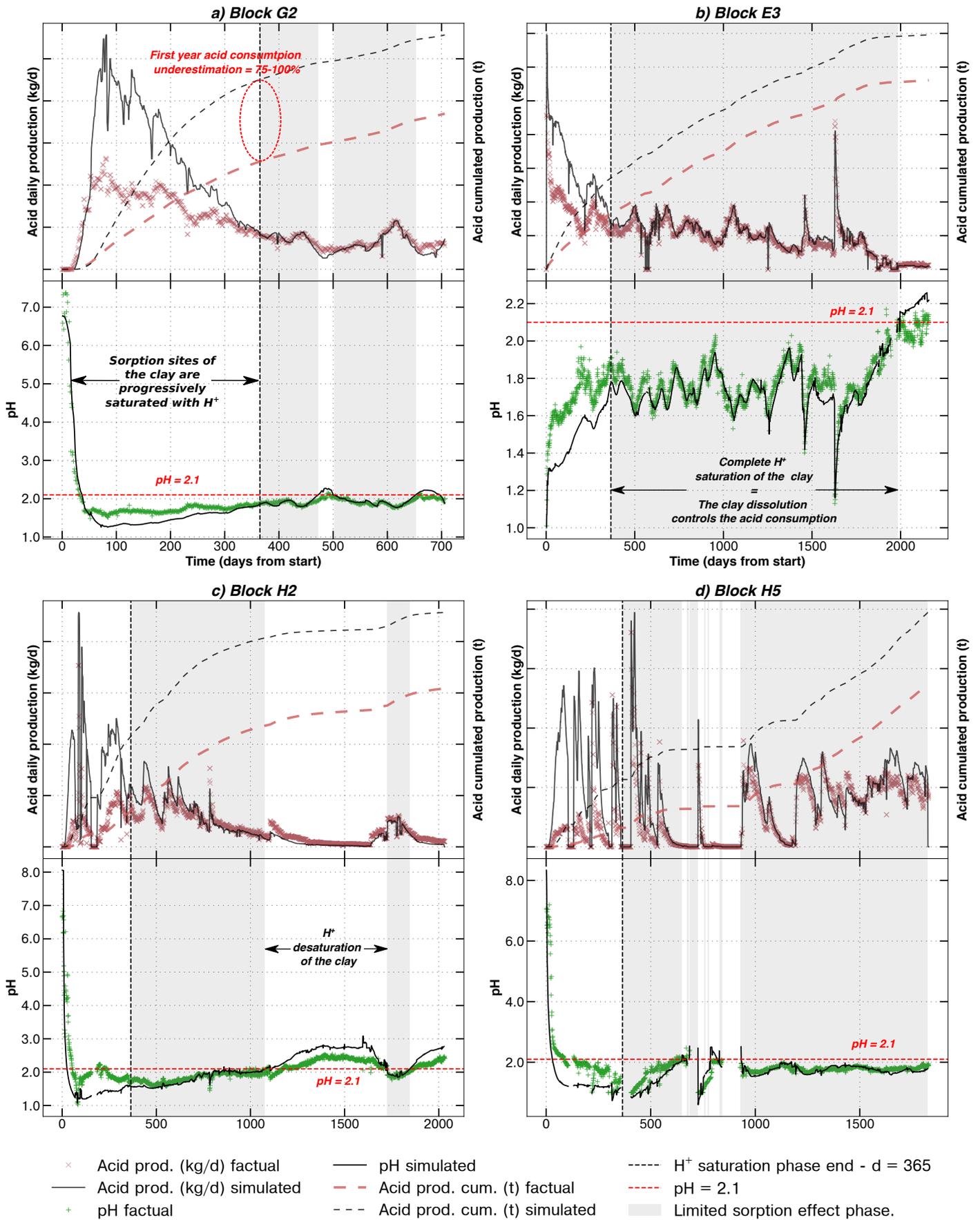


Fig. 8. History matching results of the pH and back calculated recovered acid at the block scale. For visualisation reasons, the recovered acid daily values are smoothed by a median filtering with a 3-day window. 14

1.41 times between the block scale and the well scale. This result confirms the fact that the misfit observed at the cell scale compensates at the block scale.

The mean MASE is also 1.21 times larger at the primary line scale than at the block scale because the blocks of a primary line operate sequentially. As acidification is conducted at the block scale, the primary line scale aggregates intervals with potentially different behaviours. Consequently, separation between behaviours cannot be achieved at the primary line scale.

Interestingly, the deviations are more centred at zero and exhibit a lower standard deviation for acid consumption than for uranium, both at the block scale ($3.8 \pm 29.1\%$ vs. $8.6 \pm 28.7\%$) and at the well scale ($-2.7 \pm 46.6\%$ vs. $25.8 \pm 69.9\%$). Additionally, the average mean MASE is 2.23 times lower at the block scale and 2.15 times lower at the well scale with a lower standard deviation. This result suggests a better performance of the model for predicting acid consumption than for predicting uranium output. This better performance is easily explained by the fact that the beidellite content is manually adjusted by the user, while the uraninite distribution is the result of the geostatistical process with high uncertainties. It also confirms that the local variations in beidellite content are much lower than those in uraninite content.

3.1.3. Effects of the 3D modelling method and well density constraints

Figures 9a - 10b, show results of the statistical analyses (LRD and MASE), respectively, of the uranium and acid deviations with respect to the 3D block model building method (stochastic vs. deterministic) and to the density of wells used to constrain the model. The effect of the well density (ED vs. EDT) is only observable for the primary line covered by stochastically built 3D blocks (~ 58% of blocks and cells).

Regarding uranium production, ED assets show a more off-centre average relative log deviation with a higher standard deviation at every scale, and the MASE is systematically higher for ED with a larger standard deviation (more extreme over and underestimations). The accuracy of the uranium recovery fore-

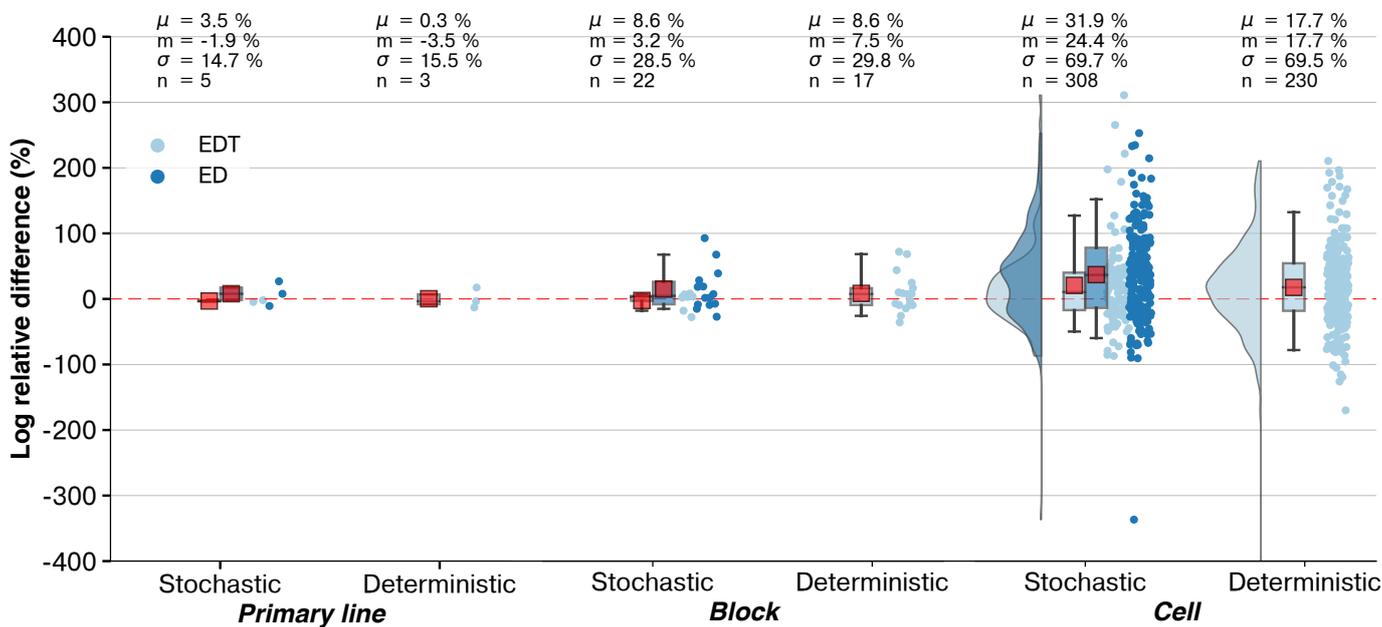
cast model is directly linked to the constraint density used to build the geological model. Therefore, the fact that a lower constraint on the 3D block model results in higher misfits proves that a major part of the misfit is due to the incorrectness of the 3D block model, and not the RT-based workflow itself.

For the acid recovered through the pumped solutions, LRD and MASE are only slightly better when the well-density constraint is low (ED) which might seem contradictory. This result is, however, explained by the direct control of the acid consumption by the beidellite grade, which is not a geostatistical outcome, but imposed by the user.

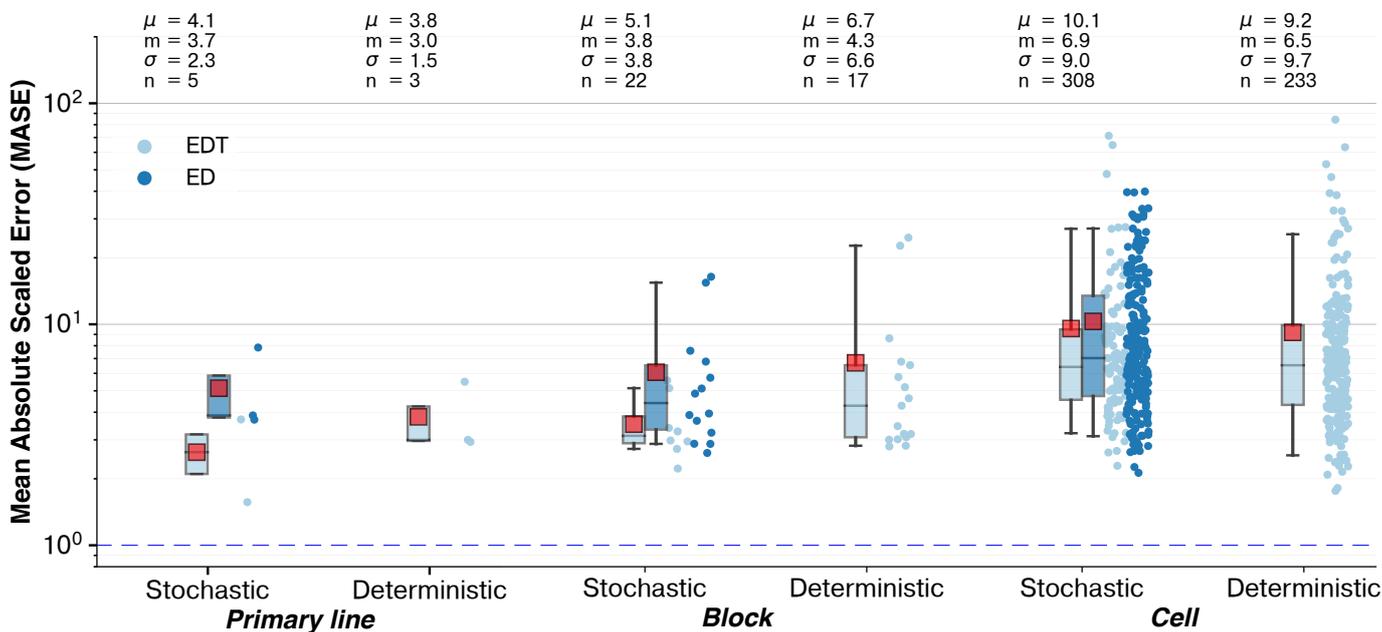
Comparing the stochastic and the deterministic methods for EDT, the first method produces better results at the primary line and block scale for uranium recovery and slightly better results at the cell scale. Therefore, this method is recommended for systematic use in all studies on operating blocks, i.e., already drilled (EDT).

3.1.4. Spatial variability of adjusted geochemical parameters

As indicated in Section 2.3.2, the adjustment necessary to obtain the results previously presented only included three global parameters: initial grades of beidellite (a single value for the three redox facies), grades of iron hydroxides in the oxidised facies and, finally, grades of calcite in the mineralised facies. Figure 11 shows the univariate distribution and spatial variability (from one block to another) of these parameters. Two remarkable observations were made. First, the parameters are spatially continuous i.e., they slightly vary between two neighbouring blocks. Second, the range of values used is consistent with the mineralogical characterisation of the reservoirs (internal studies) and rather narrow ($3.4 \pm 1.2\%$ for the beidellite). In particular, neither calcite nor iron hydroxides have been considered for Kanjugan, consistent with the mineralogical studies available (internal sources). This result reinforces the robustness of the workflow and indicates the geological soundness of the history matching process.

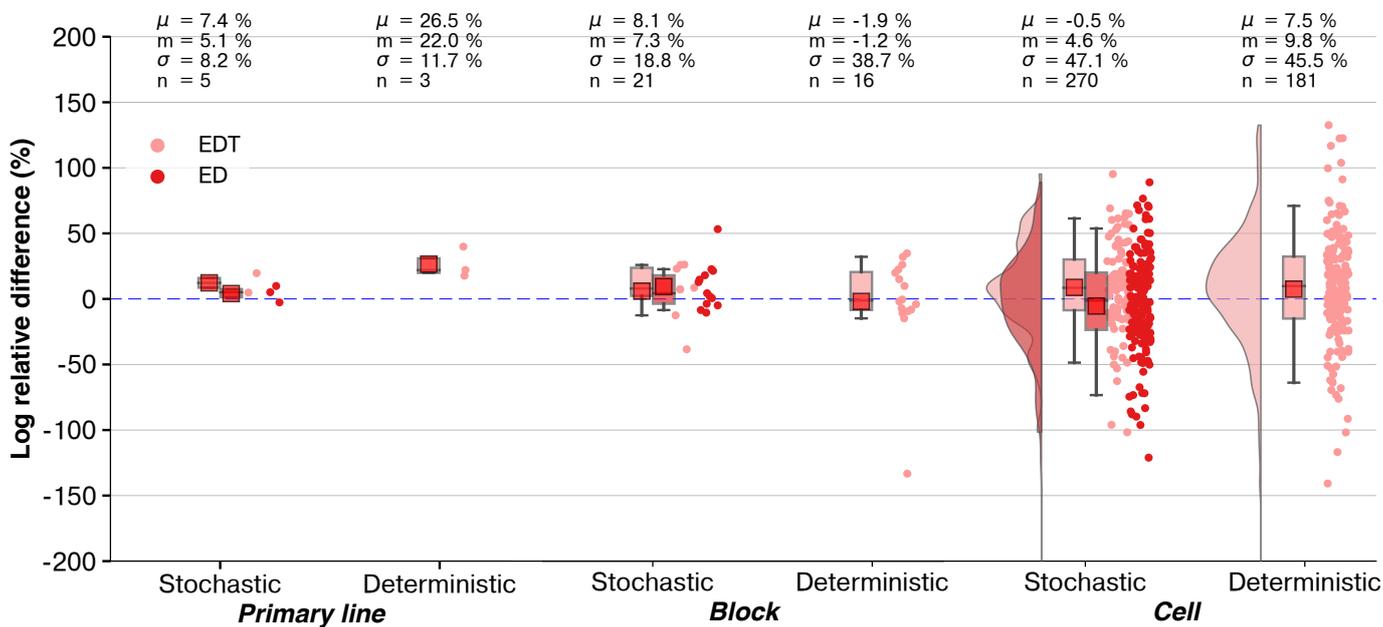


(a) Log relative difference (LRD) of the final cumulative uranium production predictions.

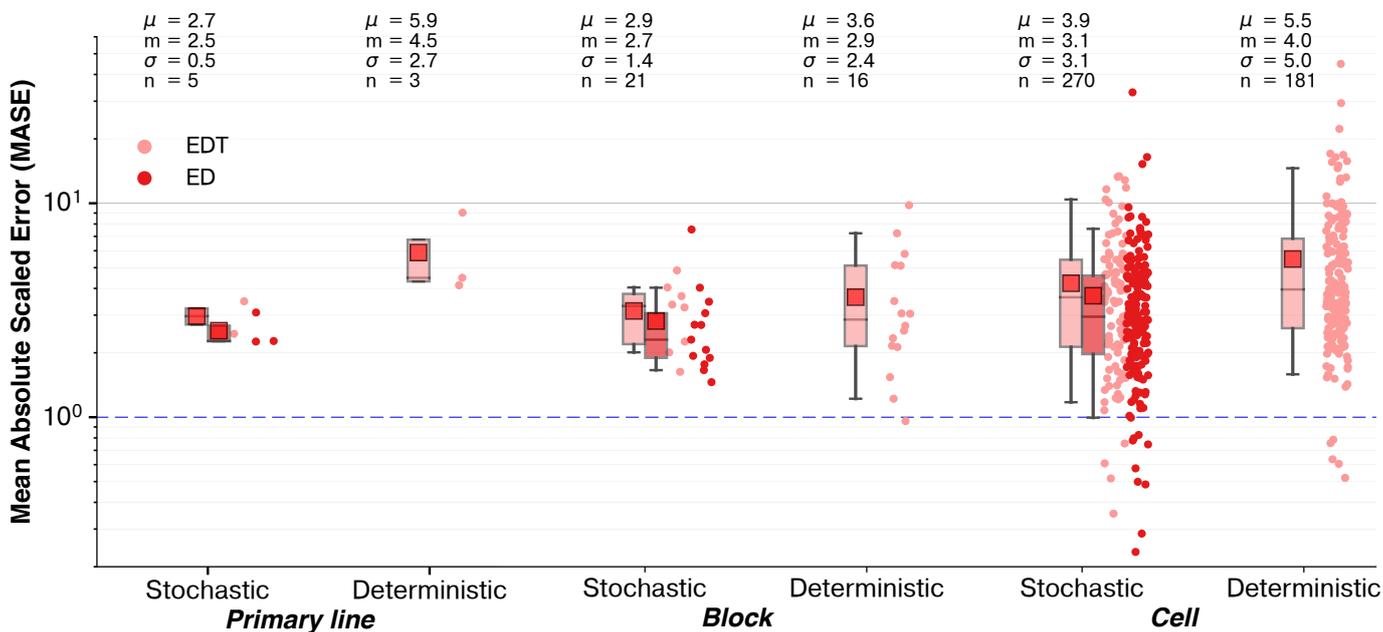


(b) Mean absolute error (MASE) of uranium production predictions.

Fig. 9. Same as for Figure 7 but for uranium production only, grouped by 3D geological model modelling method and well constraint density.

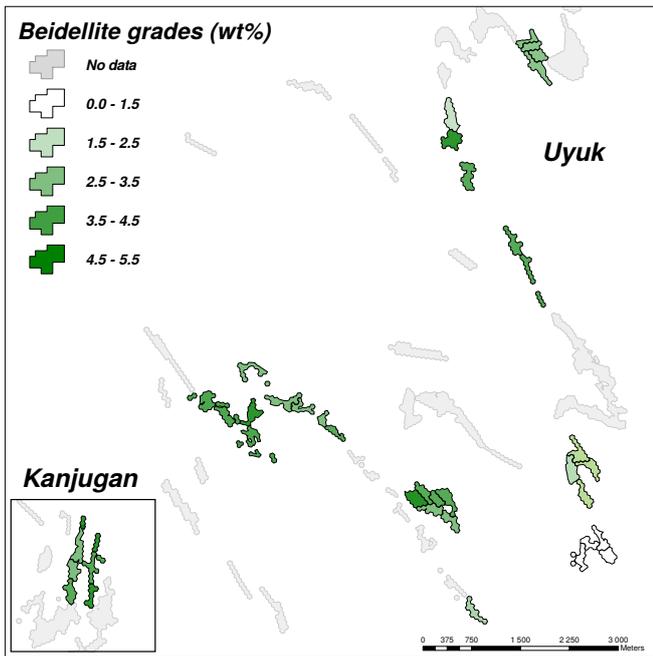


(a) Log relative difference (LRD) of the cumulative acid recovered predictions.

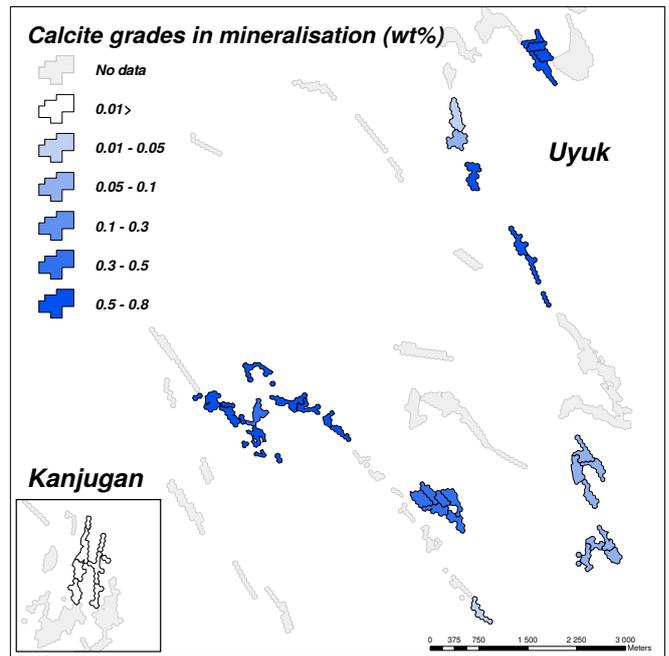


(b) Mean absolute error (MASE) of simulated acid recovered predictions.

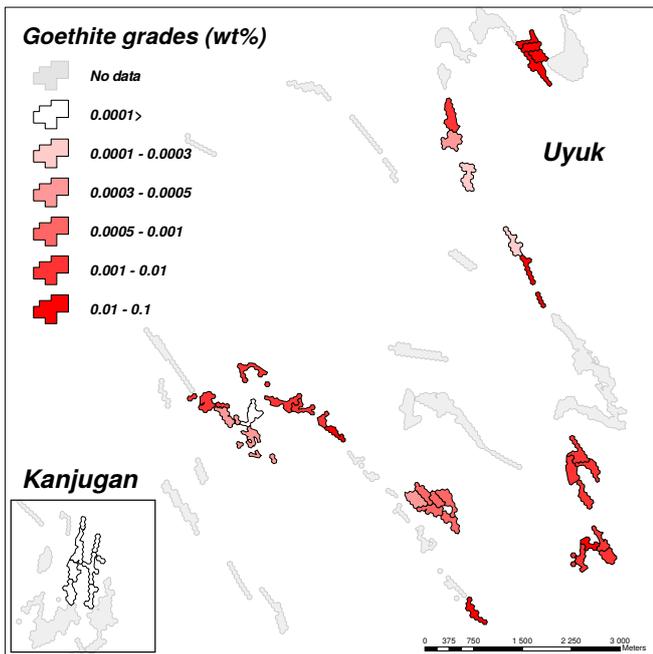
Fig. 10. Same as for Figure 9 but for the acid recovered.



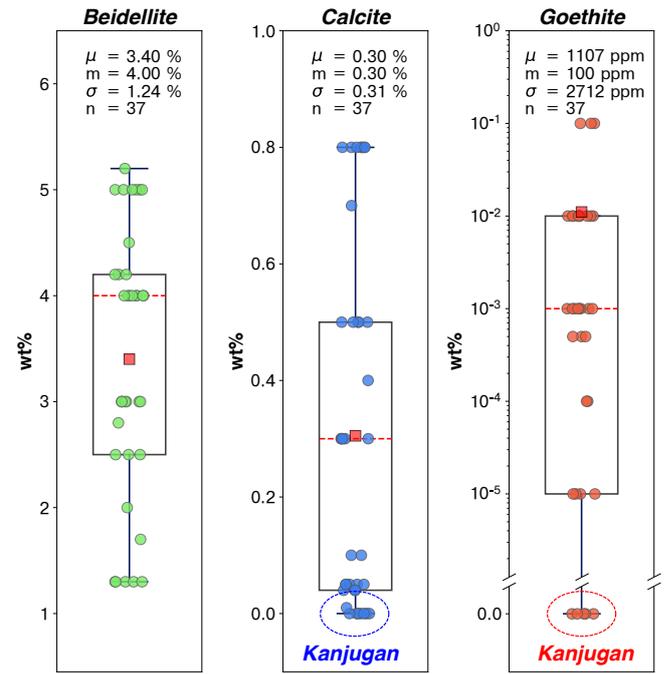
(a) Beidellite grades (wt%).



(b) Calcite grades (wt%).



(c) Iron hydroxides (goethite) grades (wt%).



(d) Distribution (box-and-whisker plot) of the parameters among the blocks.

Fig. 11. Spatial and univariate distributions of the geochemical parameters used to calibrate the models (adjusted at the technological block scale). In d) the boxes show the interquartile range (Q3-Q1) of the dataset while the whiskers extend to show the p5-p95 of the distribution. The red dashed lines and squares are the median and the mean of the datasets, respectively; μ is the average, m is the median, σ is the standard deviation and n is the number of samples.

3.2. Optimisation case study - Primary line A end of life

As introduced in Section 2.4, the true usefulness of history matching and of a robust model lies in the capacity to predict the response of a reservoir, with increased confidence, while considering various operational conditions. The next section presents the results of the optimised end of life of primary line A, based on the history matching results previously presented. First, the optimisation results from 2019 are described in detail. Second, the predictions made for the optimised well-field based on the history-matched model are compared to 16 months of observed production data.

3.2.1. Optimisation results

The history matching results showed that 37.1% of the initial estimated uranium reserves were still present under the outline of the technological blocks (day 3248 in Figure 12) before the optimisation of primary line A. Following the implementation of the procedure described in Section 2.4, the optimised design was successively improved.

Figure 13 shows the overall operational conditions tested and the production predictions for four different scenarios. Only the first two years of predictions were considered because the uncertainties in the operational parameters were considered too strong after this period. The first of these scenarios, called the reference case, relied on a well field design established empirically. In that case, the cells retained for the end of life were selected based on the previously observed production curves (high uranium concentration) and low estimated recovery (back calculated from the initial reserve of the cell minus the observed production) recorded as is and simulated in HYTEC. The three other scenarios were built based on the procedure using the RT-based workflow, which is described in detail in Section 2.4.2. The “Int. 1” and “Int. 2” cases represent intermediate test scenarios where additional wells have been proposed. The final scenario corresponds to the optimum scenario reached in the limited time available for the study.

The operational conditions used to generate the predictions vary very little from one scenario to another. For example,

the cumulative flow and the total acid tonnage varied by 8% and 6%, respectively. The final case shows the lowest acid usage and a water imbalance. This imbalance is due to injector-producer inversions, temporary injection through the producer to fully invade its vicinity and lower the pH, which were not considered in the previous cases.

In contrast to operational conditions, production predictions increase substantially as scenarios are optimised ($P_{base} < P_{int1-2} < P_{final}$, with P the uranium production). Between the base case and the final scenario retained, HYTEC predicted a 28% increase in uranium production over the first two years. Application of the cost model, which includes CAPEX (drilling, acidification unit, . . .) and OPEX (electricity, acid, plant reagents, . . .), as well as incomes, results in an increase in the net present value (NPV) of 35%. In addition, the final overall uranium concentration of the pumped solutions is increased by 23%, indicating that the trend will continue and that the gap widens beyond the two considered years.

Figure 12 shows the spatial distribution of uranium and the pH plume at key time points in a simulation. The simulation shown corresponds to the final scenario, of which the new outline was estimated in the last image, at 3454 days. Note that the first five images remain the same regardless of the chosen optimisation scheme; this period corresponds to the historical production of zone A.

This final design was applied to the well field in late 2019, and is one of the main decision-making processes based on HYTEC results at Katco. Currently, it provides the best opportunity to compare HYTEC predictions with the production observed.

3.2.2. Comparison of 2019 predictions with 2021 observed data

As planned, the study area effectively restarted in November 2019 and has been operated continuously since then. We were able to compare the predictions made in 2019 with the observed data (March 2021). A simulation was also conducted using the observed operational conditions: restarted wells, re-drilling, flow rates, acid, etc. Figure 14 shows the obtained

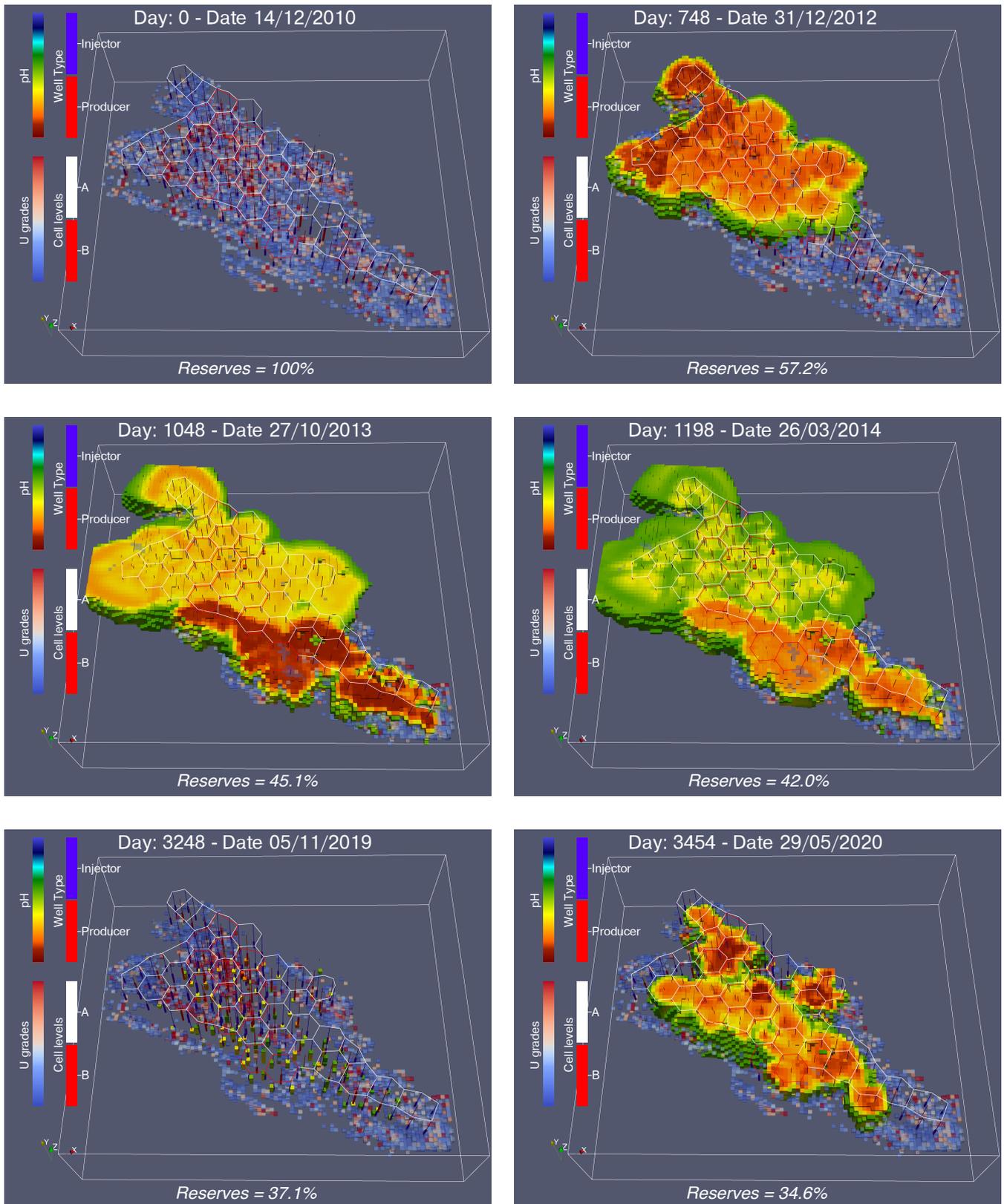


Fig. 12. Simulation results for the optimisation of the primary line A at different time steps: 3D map of the uraninite grades, initial cell design and wells and extension of the low pH plume (< 2.5). Block size ~ 800x1000 m and reservoir thickness ~ 35 m.

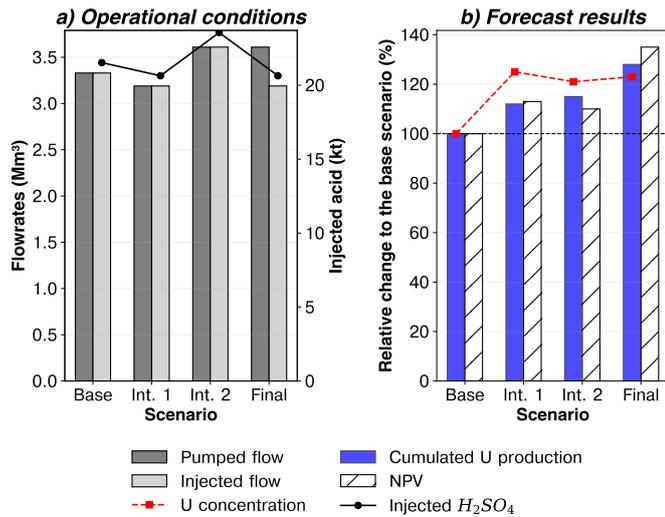


Fig. 13. Comparison of the operational conditions (a) and forecast results (b) used in four different scenarios. The base case scenario is shown on the left while the final adopted scenario is shown on the right. Int. 1 and Int. 2 are two intermediary tested scenarios.

750 results. The optimisation of the area (35 cells, 130 wells) was planned to be conducted in two stages. In Figure 14, the start of the second stage corresponds to the large peak visible at $t = 128$ days. The start date of the second stage was 15 days later than expected, and the data predicted in 2019 for the second unit were shifted by this duration to adjust to reality. This process introduces a bias that is nevertheless considered minimal. 755

730 The results show that the predicted and observed production trends match very well. After 484 days, or 16 months, predictions only underestimate total uranium production by 9.2%. Using actual operating conditions the trends are even better than expected, and the underestimation drops to 1.6%, which 760 is excellent. First, this result once again proves the robustness and accuracy of the model to reproduce the reservoir response. It is indeed capable of reproducing a complex production history spanning more than 3500 days, including operational constraints and well field design that vary substantially over time, 765 which no analytical approach is capable of reproducing. Second, this exercise proves the predictive capacity of the workflow and confirms the production and economic added value described in Section 3.2.1. Third, these results highlight the 745

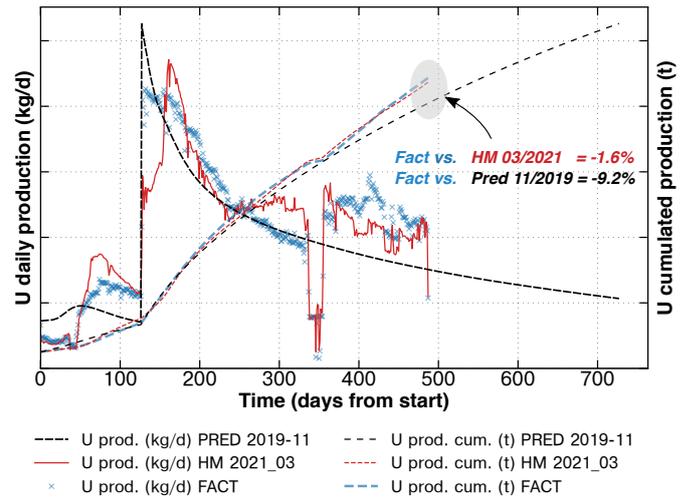


Fig. 14. Uranium production predictions from 2019 compared with observed production (March 2021) and predictions updated with observed operational conditions (March 2021).

criticality of correct operational parameter estimates. In this case study, these parameters explain most of the deviation observed between the 2019 predictions and the a posteriori observed data.

4. Discussion

4.1. Model robustness and history matching

The results presented in Section 3 have shown the capacity of the workflow to correctly reproduce production histories, and to predict the response of the reservoir while considering the operational constraints imposed on it. This robustness is strong at the scale of the production block and primary lines, which makes the tool usable for all mine planning operations and constitutes a major breakthrough in the exploitation of uranium by ISR.

However, manual calibration performed globally on the initial grades of calcite, iron hydroxides and clays, is not sufficient to explain all the variability in production data, particularly at the technological cell scale. Our assumption is that a correct reproduction at this scale would require a much finer description of the 3D geological model, i.e., spatial variability of the parameters, a finer history matching (up to voxel scale adjustment), and the consideration of more parameters, including the 770

uranium grades. The need for a finer description is supported by two main reasons.

First, internal studies have shown that initial grades of calcite, iron hydroxides and clays, as well as hydrodynamic parameters (permeability and porosity), might vary strongly and sharply even at the cell scale. This variability is also observed vertically at drill hole level. Not surprisingly, for instance, the use of an average value of beidellite at the block scale fails to adequately reproduce local acid consumption at the cell scale. Second, the uranium grades, which are one of the main parameters controlling uranium production, have not been adjusted at all in the model calibration process, which in itself is a strength of the current workflow. Uranium grades are indeed only the result of geostatistical processes. However, in addition to the uncertainties inherent in estimation methods and to the uranium local variability below the range of drill hole spacing, at least one major known source of bias affects the evaluation of the spatial distribution of uraninite. This bias is because the estimate of the grade at the boreholes, which is used to constrain the 3D geological model, is calculated mainly from a logging gamma signal (radioactivity). However, in roll-front deposits, two in-situ chemical elements are gamma emitters, namely, uranium (U) and radium (Ra), and are not evenly spatially distributed. This results in Ra/U ratios varying sometimes up to an order of magnitude, with complex distributions. The few available measurements increase the difficulty of mapping these disequilibria, and in practice, a single correction ratio value is used across several primary lines. It logically has the effect of providing a good estimate of the overall grade but taints the local values with error. This explanation is completely consistent with the results obtained in Section 3.1.1, i.e., errors at the cell scale follow a normal distribution centred at zero, and compensate for each other, resulting in better matches at block and primary line scales.

In the absence of additional data (drill holes) to constrain the geostatistical processes (which represent unaffordable costs for the operator), the remaining alternative to improve 3D geological models is the automation of the parameter adjustment

by a computer: mineral (e.g., uraninite and beidellite) grade scalar fields, as well as hydrological parameters such as permeability and porosity. This approach, known as automated history matching, has been widely studied and applied to reservoirs since the 1960s (de Marsily et al., 2000), in hydrogeology (Carrera et al., 2005; Zhou et al., 2014), and in the petroleum industry (Oliver and Chen, 2011; Rwechungura et al., 2011). Automated history matching allows us to adjust scalar or discrete fields up to the voxel scale, improving the forecast of models with higher confidences. Therefore, the development of large-scale reactive-transport inversion frameworks is highly desirable, and it is probably the area with the highest potential for workflow improvements.

4.2. Operational conditions

Although a robust workflow and an efficient history matching process are key aspects that help solve the problem of predicting future reservoir performance, a good estimate of future production also requires a good forecast of the operational conditions imposed to the reservoir. On the one hand, the geometry of the well field and the amounts of injected acid are the result of human decisions, and can therefore be determined precisely through sustained planning. The flow rates, on the other hand, are much more difficult to predict because they are largely controlled by coupled chemo-mechanical clogging phenomena (Vergnaud, 2020) and the operator can only perform curative actions whose effectiveness is temporary. Consequently, two blocks with equivalent reserves and geometries may have very variable production profiles depending on their level of clogging. Understanding and ultimately predicting these phenomena is essential to improve predictions. The wrong forecast of flow rates is responsible for most of the error in the production forecast at the block scale for the case study presented in Section 3.2.2 (9.2% versus 1.6% for forecasted and observed operational conditions, respectively). This result was even stronger at the cell scale. Accumulated over blocks, this error might have an important impact on the reliability of mining plans, and might affect the result of local optimisations. This area is conse-

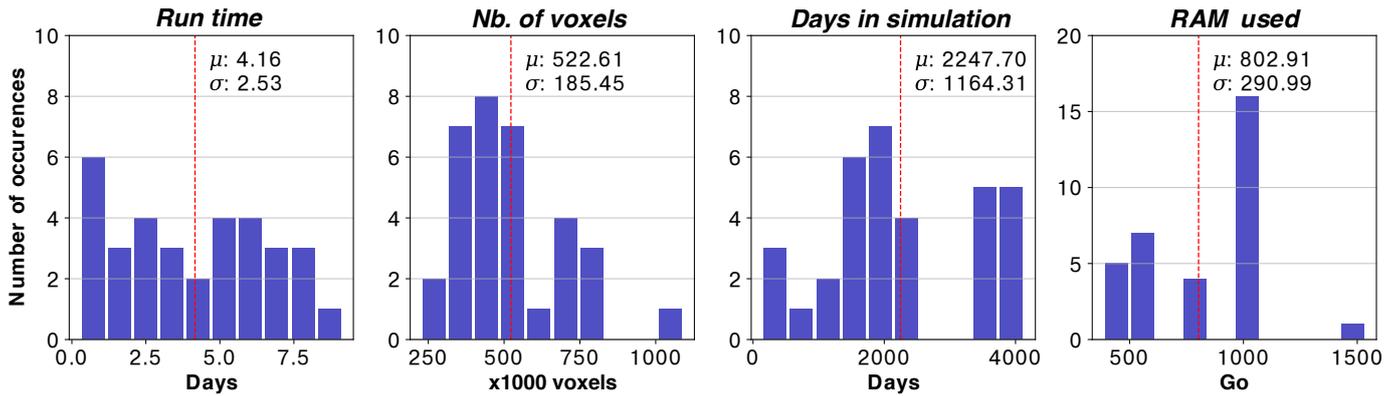


Fig. 15. Runtime, number of voxels in the 3D blocks, number of days simulated and RAM used in the history matching simulations presented.

quently an important research topic, which should be developed alongside automated history matching.

4.3. Industrial capacity

One of the fundamental aspects of a numerical model integrated in a regular workflow of operations is the speed with which the operator can obtain results on which to base his or her decisions. Regarding the presented workflow, due to its robustness and the low variability of adjusted geochemical parameters from one block to a neighbouring block, the model calibration only required two to three runs on average. This calibration is not a limitation for a systematic use of the workflow for mine planning or optimisation studies (several hundred runs per year).

However, the calculation time and CPU capacity may become factors limiting several lines of research previously discussed. Figure 15 shows the runtime, the number of voxels of the 3D models, the number of days of production simulated, and finally the RAM used to generate the simulation results (Section 3). Although the number of production days simulated is generally high - ~ 2250 days on average, as the study focused on areas reaching their end of life, an average of 4 days, and 1000 Go of RAM were required to run a simulation. If these constraints do not prohibit a single run, history matching might need hundreds to thousands of calls of the model with increased memory needs (Oliver and Chen, 2011).

Moreover, the tendency is to increase the size of the grid and

the period of time covered. First, simulating multiple blocks at once takes into account their interactions and removes the bias for border cells. Second, environmental monitoring and footprint assessment consider acid migration with the natural flow of the aquifer during the rehabilitation, up to a hundred years after mine closure, and for the far field domain, extending beyond the contour of the production blocks (de Boissezon et al., 2017; Lagneau et al., 2019; de Boissezon et al., 2020). Consequently, code performance optimisation (memory usage, parallelisation, etc.) is very important and should not be neglected while adding complexity to the workflow. An interesting approach to overcome these speed and memory issues is the usage of surrogate modelling, i.e., a statistical model of the model, also called a meta-model or proxy model (Sacks et al., 1989; Wang and Shan, 2006). This approach has already been widely used in the oil and gas industry at industrial scale (Feraille and Marrel, 2012; Feraille, 2013; Costa et al., 2014, among others), with limitations especially for automated history matching (Zubarev, 2009).

4.4. Applicability to other deposits and commodities

Started in 2006 (Nos, 2011), the project at the origin of the presented workflow represents 15 years of effort and development. These developments involved firstly the adaptation of reactive transport codes to the ISR case in porous media, secondly, the creation of a geochemical model, and, finally, the creation of pre- and post-processing interfaces, which actually

constitutes the main part of the work (Lagneau et al., 2019). Our experience shows that the use of this workflow for a new roll-front uranium mine, such as found in Kazakhstan, Mongolia or Uzbekistan, represents relatively little effort insofar as the geochemical model and the operating scheme do not change significantly. However, it requires much more effort when the geology changes, e.g., for high-grade uranium deposits of Athabasca Basin in Canada. In the latter case, the mineralogy and uranium proportions greatly differ, which means a new geochemical model must be established. In addition, the extraction is performed in fractured media, which means the flow transport must rely on different modelling approaches such as double porosity that must be incorporated in reactive-transport tools if not existing. Similarly, mining another metal (e.g., copper) requires creating and testing a new geochemical model and potentially adapting the tools if the geological context greatly differs, which can take up to several years. Therefore, the creation of an ISR modelling workflow for a mine site greatly depends on the existence or not of reactive transport model and pre- and post processing infrastructure for a similar deposit.

4.5. Comments about alternative simulation approaches

As explained in the section 2.1.2, the operator monitors the well field behaviour watching three main parameters: flow in the field, dissolved uranium concentration at the block scale, and acid consumption. Lagneau et al. (2019) illustrated the limit of traditional ISR operations forecast, where evolution is evaluated independently for the three parameters:

- Flow in the field is ignored.
- Acid consumption is based on empirical coefficients (e.g., mass of acid consumed by mass of uranium produced), based on supposedly similar areas of the exploitation.
- Evolution of uranium concentration in the leach solution is based on analytical functions using parameters adjusted on production data: the extrapolation of these functions is used as a predictor.

Such approach is acceptable only if operating conditions remain constant which is not the case in practice as illustrated with primary lines and block production curves (Figures 5 and 6).

Another alternative is pure hydrological simulation which has been reported for well field optimisation (Krause et al., 2016) and focuses on the flow within the reservoir, taking into account hydrological parameters only.

However, the use of this approach is limited in operational conditions because (i) homogeneous global values in porosity and permeability are used, data acquisition being too costly (ii) the validation of the hydrodynamic parameters can only be done by means of tracer tests which are spotty, or by having the well-head pressures, which is not a standard practice in the ISR industry because of its cost. Moreover, elements such as uranium or acidity cannot be used as tracers as they are largely impacted by the chemical dimension.

In the end, only the 3D reactive transport approach gathers the three pillars of ISR operations, which are (i) reservoir geometry and composition (ii) well field geometry (iii) operational conditions. This is the only method that correctly considers the leaching within the reservoir and provides a real metal balance and dissolution and recovery rates.

5. Conclusions

This paper presents one of the first large-scale well field applications of reactive transport (RT) simulation in the context of uranium in situ recovery (ISR). The RT-based workflow was successfully used on 39 production blocks containing 2394 wells of the Katco ISR Mine well field. The model was found to be very robust at the block and primary line scales, accurately reproducing uranium production and acid consumption over time scales of up to 12 years, with dramatic time-varying operational conditions (well field design, flow rates, and leaching solution acidity). The robustness of the model is based on the adjustment of only three global parameters of the 3D geological models: initial grades in clays (beidellite), initial grades in calcite, and initial grades in iron hydroxides (goethite). In addition, these calibration parameters are spatially continuous

and consistent with mineralogical internal studies. The statistical study of the model deviations has shown that the errors at the production well scale compensate for each other, therefore indicating that most of the remaining forecast errors are attributable to the 3D geological model and not to reactive transport simulations.

The optimisation case study validated the predictive nature of the RT-based workflow on a real example of an area of life management, showing less than 10% deviation between predictions and observed data 16 months later. It also revealed the significance of gains provided by the workflow in operations: +28% increase in uranium production and +35% increase in economic gains just over the first two years of end of block life management.

Overall, this paper proved the capacity of an RT-based workflow to be used industrially and how it became a game changer on several accounts. First, hydrogeologists and mining engineers are increasingly expected to make difficult decisions for which qualitative understanding of reservoirs is not sufficient. Instead, an accurate quantitative evaluation is needed and cannot be provided by empirical approaches. Second, large datasets of concentrations, flow rates, and operational conditions are available and must be considered when making these decisions. While qualitative approaches are still possible, numerical models such as HYTEC are required to fill in the gaps and make full use of data. Third, the time is ripe for geometallurgical approaches, when economic and environmental aspects are the main drivers in operation (Dominy et al., 2018; Michaux, 2020). The workflow presented here fulfils the needs by coupling geology, geostatistics and metallurgical response of the reservoir.

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