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# New experimental density data and derived thermophysical properties of carbon dioxide - Sulphur dioxide binary mixture $\left(\mathrm{CO}_{2}-\mathrm{SO}_{2}\right)$ in gas, liquid and supercritical phases from 273 K to 353 K and at pressures up to 42 $\mathbf{M P a}$ 

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#### Abstract

Due in part to the toxicity of the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ binary system, there are no density data available in the literature. Densities for this system were measured using a vibrating tube densitometer (VTD), Anton Paar DMA 512, and the forced path mechanical calibration (FPMC) method in the gas, liquid and supercritical phases at pressures up to 41.7 MPa . The mole fraction of the mixture was $0.9478 \mathrm{CO}_{2}+0.0522 \mathrm{SO}_{2}$ at 298 K and $0.9503 \mathrm{CO}_{2}+0.0497 \mathrm{SO}_{2}$ at 273, 283, 323 and 353 K . The compressibility factor, isobaric heat capacity and bubble points were also derived from the measured densities. The classical cubic equations of state, i.e., Soave-Redlich-Kwong (SRK), Peng-Robinson (PR) and Valderrama version of Patel-Teja (VPT) with the $\mathrm{CO}_{2}$ volume correction term and Peneloux shift parameter in addition to a multi parameter EoS based on Helmholtz energy were evaluated using the measured density data. The most accurate EoSs for the investigated system were the multi parameter EoS and the PR-CO ${ }_{2}$ with overall AAD of $0.6 \%$ and $1.0 \%$, respectively.


Keywords: Density, Carbon capture transport and storage (CCS), $\mathrm{CO}_{2}$, Sulphur Dioxide $\left(\mathrm{SO}_{2}\right)$, Thermophysical properties, Equation of State (EoS)

## 1. Introduction

High demand for energy due to the rapid economic growth resulted in an ever increasing use of fossil fuels, i.e. coal, oil and natural gas following the industrial revolution. The effect of this has been to increase the amount of greenhouse gases such as $\mathrm{CO}_{2}$ in the atmosphere. Carbon capture and storage (CCS) is the name given to technology based solutions aimed at reducing $\mathrm{CO}_{2}$ emissions to the atmosphere [1]. This technology comprises capturing $\mathrm{CO}_{2}$ during burning of fossil fuels, compression and transport mainly via pipelines and injection into geological storage basins. The captured $\mathrm{CO}_{2}$ will contain ranges of impurities depend on the source of fossil fuel as well as the capturing technology [2][3].

Sulphur dioxide can be present in heavy oil production or in flue gas in the post-combustion or oxyfuel processes in coal-fired power plants. In the MEA-based absorption processes, impurities such as $\mathrm{O}_{2}, \mathrm{NO}_{2}$ and $\mathrm{SO}_{2}$ can lead to severe operational problems such as foaming, viscosity increase and formation of heat-stable salts. The typical range of $\mathrm{SO}_{2}$ in the MEAbased post-combustion processes is 500-3000 part per million by volume $\left(\mathrm{ppm}_{\mathrm{v}}\right)$. Flue gas desulphurisation (FGD) units with wet $\mathrm{SO}_{2}$ scrubbers can absorb $80-95 \%$ of the $\mathrm{SO}_{2}$ in the flue gas before entering the $\mathrm{CO}_{2}$ absorber. However, in case of failure in the FGD unit, $75 \%$ of the $\mathrm{SO}_{2}$ could be absorbed by MEA as it is not selective a solvent to acid gases [2]. The presence of $\mathrm{SO}_{2}$ can make problems such as corrosion in the presence of water [4] in the transportation of captured $\mathrm{CO}_{2}$ with impurities from both MEA-based post-combustion or oxyfuel processes [5][6].

Due to the toxicity of $\mathrm{SO}_{2}$, the Immediately Dangerous to Life and Health (IDLH) concentration of this component is set to $100 \mathrm{ppm}_{\mathrm{v}}$ by the National Institute for Occupational Safety and Health (NIOSH) [7]. Shell Cansolv also commissioned an integrated system to capture $\mathrm{CO}_{2}$ and $\mathrm{SO}_{2}$ simultaneously in a commercial scale post-combustion coal fired power plant in Saskatchewan. The captured $\mathrm{CO}_{2}$ is transported for the $\mathrm{CO}_{2}$ Enhanced Oil Recovery ( $\mathrm{CO}_{2}$-EOR) in Weyburn oil field and $\mathrm{SO}_{2}$ is used to produce sulphuric acid as a valuable byproduct [8].

Similar to injection of acid gases, i.e., injection of $\mathrm{CO}_{2}-\mathrm{H}_{2} \mathrm{~S}$ [9][10], technically, $\mathrm{CO}_{2}$ and $\mathrm{SO}_{2}$ can be co-stored in deep saline aquifers and this effectively reduces the capture cost by avoiding $\mathrm{SO}_{2}$ removal costs [11][12][13]. However, the reactivity of $\mathrm{SO}_{2}$ with rock in the presence of water and acids that form is an issue of concern [14][15][16]. The geochemical
effects can reduce the pH of the formation water, change the porosity of reservoir rock and cause mineral dissolution and sulphate precipitation [11][17][18][19][20].

A proper understanding of the thermodynamic and transport properties of $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ systems is required as an input to feasibility studies and equipment sizing in the above processes [21]. The presence of impurities in the captured streams of $\mathrm{CO}_{2}$ would affect the thermophysical properties, in particular density and viscosity, of high $\mathrm{CO}_{2}$ content mixtures. Equations of state (EoSs) should be evaluated using the experimental density and vapour-liquid equilibrium (VLE) data. The lack of experimental data for $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ systems is certainly due to toxicity of the system [22]. The only available data for this system is reported by Caubet [23] in 1904. A comprehensive thermodynamic behaviour of $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ mixture was studied experimentally by Coquelet and co-workers [24], [25] for transport purposes of $\mathrm{CO}_{2}$ mixtures in a CCS context. Only VLE data are available at 263.15 K and 333.21 K and at pressures ranging from 0.1 to 8.8 MPa .

In this work, the densities of approximately $95 \mathrm{~mol} \% \mathrm{CO}_{2}$ with $5 \mathrm{~mol} \% \mathrm{SO}_{2}$ were measured using a Vibrating Tube Densitometer (VTD) in the gas, liquid and supercritical phases. The measurements were carried out at five isotherms 273, 283, 298, 323 and 353 K at pressures up to 42 MPa . Thermodynamic properties such as compressibility factor, isobaric specific heat capacity and bubble points were obtained from the measured densities. The measured densities also were employed to evaluate the classical cubic EoSs, i.e., Soave-Redlich-Kwong (SRK-EoS) [26], Peng-Robinson (PR-ES) [27], and Valderrama modification of the [28] Patel-Teja (VPT-EoS) [29] EoSs. Then, to improve the density prediction, the $\mathrm{CO}_{2}$ volume correction term [30] and Peneloux shift parameter [31] were introduced to those EoSs. Also, a multi parameter EoS based on Helmholtz energy [32][33] with the short industrial equation from Lemmon \& Span for pure $\mathrm{SO}_{2}$ [34] (see Appendix A) and Span \&Wagner EoS for pure $\mathrm{CO}_{2}$ [35] was evaluated using the measured density data and derived thermodynamic properties.

## 2. Experimental part

Experimental work was carried out in the high safety laboratory at CTP - Centre of Thermodynamics of Processes research group at Mines ParisTech in France.

### 2.1. Material

A binary mixture of $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ was prepared to perform density measurements. Table 1 shows the details of the chemicals, suppliers and purities of the components used in this study. A pressure vessel with a volume of 100 mL was vacuumed and then after disconnecting from the vacuum pump, the mass was measured using a balance with four digit after the decimal point (brand: Sartorius) three times. Due to the lower vapour pressure of $\mathrm{SO}_{2}(0.35 \mathrm{MPa}$ at 293 K ) compared to $\mathrm{CO}_{2}$ (with a vapour pressure of 5.73 MPa at 293 K ), first $\mathrm{SO}_{2}$ was injected to the vacuumed pressure vessel. After neutralising the $\mathrm{SO}_{2}$ trapped in the line using sodium hydroxide $(\mathrm{NaOH})$ considering acid base reaction, the pressure vessel was disconnected and the weight was measured to obtain the exact amount of injected $\mathrm{SO}_{2}$. The weight of injected $\mathrm{SO}_{2}$ was 6.357 g . The pressure vessel then was connected to the $\mathrm{CO}_{2}$ cylinder in order to inject $\mathrm{CO}_{2}$. After disconnecting the pressure vessel and weighing with the balance, the amount of injected $\mathrm{CO}_{2}$ was 79.229 g . After calculations, the mole percent for $\mathrm{SO}_{2}$ and $\mathrm{CO}_{2}$ was $5.22 \mathrm{~mol} \%$ with $u_{r}(z)=0.010 \mathrm{~mol} \% 94.78 \mathrm{~mol} \%$ with $u_{r}(z)=0.180 \mathrm{~mol} \%$, respectively. The uncertainties are reported with $95 \%$ confidence level (coverage factor $k=2$ ). The prepared binary mixture was then used to perform density measurements at 298 K. Due to a leak through the piston to the nitrogen side resulting in a change in the composition, another binary mixture was prepared with a similar procedure to conduct the density measurements at the other isotherms. The amount of injected $\mathrm{SO}_{2}$ and $\mathrm{CO}_{2}$ was 4.579 and 60.183 g , respectively. The mole percent and uncertainties with $95 \%$ confidence level were $4.97 \mathrm{~mol} \%$ with $u_{r}(z)=0.010 \mathrm{~mol} \%$ for $\mathrm{SO}_{2}$ and $95.03 \mathrm{~mol} \%$ with $u_{r}(z)=0.181 \mathrm{~mol} \%$ for $\mathrm{CO}_{2}$, respectively.

### 2.2. Equipment description

A Vibrating Tube Densitometer (VTD), Anton Paar DMA 512 was used to measure the densities. Figure 1 shows a schematic view of the setup which has been thoroughly described in previous publication [36][37]. Briefly, the main part of the setup is a U-shaped vibrating tube Anton Paar densitometer (1) with a working pressure of up to 70 MPa and temperature range of $263-423 \mathrm{~K}$. The tube material is Hastelloy. A jacket through which fluid is circulated from a liquid bath (4) surrounds the densitometer allowing control of the temperature with a stability of $\pm 0.02 \mathrm{~K}$. The sample fluid flows from the $150 \mathrm{ml}, 70 \mathrm{MPa}$ rated pressurised vessel (2) to the densitometer through a tube with a diameter of 1.6 mm
( $1 / 16$ inches) and pressure rating of 100 MPa . The connecting tubes are fully immersed in a temperature controlled liquid bath model West P6100 (5).

The pressure of setup is measured with three pressure transducers (model: Druck PTX611) (6) with ranges of $0-10 \mathrm{MPa}, 10-30 \mathrm{MPa}$ and $30-70 \mathrm{MPa}$. The transducers were calibrated with an electronic balance (model: GE Sensing PACE 5000) at pressure up to 20 MPa and using a dead weight tester (model: Desgranges \& Huot 5202S) for pressures from 20 to 40 MPa. The pressure transducers can measure the pressure with standard uncertainties of $u(p)=$ $0.002 \mathrm{MPa}, u(p)=0.005 \mathrm{MPa}$ and $u(p)=0.005 \mathrm{MPa}$ in the ranges of $0-10 \mathrm{MPa}, 10-30 \mathrm{MPa}$ and 30-70 MPa, respectively. The temperature of the densitometer and the liquid bath were measured using four-wire $100-\Omega$ platinum resistance probes (Pt100) (7). The probes were calibrated against a reference thermometer with $25-\Omega$ (model: Tinsley Precision Instrument). The standard uncertainty of the temperature probes were estimated to be $u(T)=0.02 \mathrm{~K}$ after calibration. The pressure and temperature were recorded using an Agilent HP34970A data acquisition unit (10). The vibration period, $\tau$, also was recorded using a HP53131A data acquisition unit (10).

### 2.3. Calibration and measurement procedures

The densitometer was firstly calibrated using pure $\mathrm{CO}_{2}$ as a reference fluid and forced path mechanical calibration (FPMC) model developed by Bouchot and Richon [38][39][40]. This method considers that the vibrating tube is represented by a box with a known internal volume, $V$, and a known mass of tube $M_{0}$. The box is connected to a support with a spring with a constant of stiffness, $K$. Consequently, the period of vibration, $\tau$, is expressed by: $=2 \pi \sqrt{\frac{M}{K}}$, with $M=M_{0}+\rho V$. In this model, the stress and strain behaviour of the tube material would be represented from the realistic mechanical considerations. The reference fluid is used to set the magnitude of pressure independent from temperature. The following equation shows the frame for the FPMC model:

$$
\begin{equation*}
\rho=\left(\frac{M_{0}}{V_{i}(T, P)}\right)\left[\left(\frac{K(T, P)}{K_{0}(T)}\right)\left(\frac{\tau^{2}(T, P)}{\tau_{0}^{2}(T)}\right)-1\right] \tag{1}
\end{equation*}
$$

Where $\rho$ is the density of inner fluid, $M_{0}$ is the mass of the tube under vacuum, $V_{i}$ is the internal volume, $K$ is the natural transversal stiffness and $\tau$ is the vibrating period. The subscript 0 indicates the vacuum condition. By considering the tube as a thick-walled cylinder and replacing terms for the $M_{0} / V_{i}$ and $K / K_{0}$, the complete FPMC model can be formulated as [38]:

$$
\begin{equation*}
\rho(T, P)=\left(\frac{M_{0}}{L_{00}}\right)\left(\frac{1}{\pi r_{i}^{2}(T, P) \delta L(T, P)}\right)\left[\left(\frac{\Delta r^{4}(T, P)}{\Delta r_{0}^{4}(T)}\right) \exp \left(-3 \gamma_{T} P\right)\left(\frac{\tau^{2}(T, P)}{\tau_{0}^{2}(T)}\right)-1\right] \tag{2}
\end{equation*}
$$

The density data obtained from the Span and Wagner EoS [41] were used as a reference densities to tune the unknown parameters, $\left(\mathrm{M}_{0} / \mathrm{L}_{00}\right)$ and $\gamma_{\mathrm{T}}$, in this model at the full range of pressures for each measured isotherm. The measurement procedure as well as the method to determine the combined standard uncertainties [42][43] for each measured density were well described in the authors' previous publication [36].

## 3. Specific heat capacity calculations

The residual specific heat capacity ( $C_{p}-C_{p}^{0}$ ) can be calculated from the measured density data through the following equation [44]:

$$
\begin{equation*}
\rho=\left(\frac{\partial C_{p}}{\partial P}\right)_{T}=-T\left(\frac{\partial^{2} v}{\partial T^{2}}\right)_{P} \tag{3}
\end{equation*}
$$

In this equation, the gradient of molar volume with temperature at each constant pressure were plotted using the measured densities at the five measured isotherms. The procedure to calculate the specific heat capacity from Equation (3) has also been described in a previous publication for the $\mathrm{CO}_{2}-\mathrm{H}_{2} \mathrm{~S}$ system [36]. A similar procedure was undertaken in this work. The constants B to F in the Aly \& Lee equation [45] to calculate the ideal gas specific heat capacity, $\mathrm{C}_{\mathrm{pi}}^{0}$, for $\mathrm{CO}_{2}$ and $\mathrm{SO}_{2}$ components is summarised in Table 2. The obtained $\mathrm{C}_{\mathrm{pi}}^{0}$ from the Aly \& Lee equation [45] is in $J . \mathrm{K}^{-1} . \mathrm{kmol}^{-1}$.

## 4. Results and discussions

Densities of $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ binary systems were measured using vibrating tube densitometer (VTD), Anton Paar DMA 512 in the gas, liquid and supercritical phases at pressures up to 41.7 MPa. The composition of the binary system was $0.9478 \mathrm{CO}_{2}+0.0522 \mathrm{SO}_{2}$ at 298 K and $0.9503 \mathrm{CO}_{2}+0.0497 \mathrm{SO}_{2}$ at $273,283,323$ and 353 K . At each isotherm, the densitometer was firstly calibrated using pure $\mathrm{CO}_{2}$ with a forced path mechanical calibration (FPMC) technique [38]. The measured densities along with their uncertainties and compressibility factor at each corresponding pressure, temperature and phase are reported in Tables 3 through 7 for each isotherm. The uncertainty values in the gas, liquid and supercritical phases are summarised for each isotherm in Table 8. The measured densities then are compared against various equations of state including Soave-Redlich-Kwong [26] (SRK), Peng-Robinson [27] (PR), Patel-Teja [29] with Valderrama modification [28] (VPT), those with introducing $\mathrm{CO}_{2}$
volume fraction [30][46] and Peneloux shift parameter [31] as well as multi parameter equation of state based on Helmholtz energy [33]. In this work, the modified binary interaction parameter, $k_{i j}$ or $B I P$, for the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ was 0.02 for all cubic EoSs. The Average Absolute Deviation (AAD) of these model predictions from the obtained density data was calculated from the following equation:

$$
\begin{equation*}
A A D(\%)=N^{-1} \sum_{i=1}^{N}\left(\left|\rho_{\text {Exp. }}-\rho_{\text {Model }}\right| / \rho_{\text {Exp. }}\right) \times 100 \tag{4}
\end{equation*}
$$

Table 9 summarises the AAD and Maximum Absolute Deviation (MAD) of the investigated EoSs in the gas, liquid and supercritical phases as well as the overall quantities. Thermodynamic properties of the investigated mixtures, i.e., compressibility factor, isobaric specific heat capacity and bubble points, were derived from the measured densities. Table 10 gives the derived specific heat capacities of the binary system and predicted quantities with the multi parameter EoS. The bubble points of the mixture are summarised at two isotherms in Table 11.

The measured densities, as shown in Table 3 to 7, varies over a wide range from $1.0 \mathrm{~kg} / \mathrm{m}^{3}$ at 297.42 k and 0.051 MPa to $1110.7 \mathrm{~kg} / \mathrm{m}^{3}$ at 273.54 K and 41.723 MPa . Overall (see Table 8), 454 density data were obtained of which 97 points were in the gas phase, 221 points in the liquid phase and 136 points in the supercritical phase. Figure 2 demonstrates the measured and predicted densities using multi parameter EoS at different isotherms. Values at lower pressures, i.e. pressures less than 8 MPa and densities below $200 \mathrm{~kg} / \mathrm{m}^{3}$ are shown in Figure 3.

The maximum uncertainty of the measured densities [42][43], as shown in Table 8, is $u_{r}(\rho)=$ $4.4 \%$ in the gas phase at 298 K and very low pressure conditions. However, the average uncertainty in the gas phase at all isotherms is $u_{r}(\rho)=0.6 \%$. The average uncertainty in the liquid phase is also $u_{r}(\rho)=0.03 \%$ with the maximum value of $u_{r}(\rho)=1.0 \%$. Those in the supercritical phase is $u_{r}(\rho)=0.1 \%$ and $u_{r}(\rho)=1.0 \%$ for the average and maximum uncertainties, respectively. Overall, the average uncertainty for the measured densities is $u(\rho)$ $=0.4 \mathrm{~kg} / \mathrm{m}^{3}$ or $u_{r}(\rho)=0.2 \%$ with the maximum value of $u(\rho)=2.7 \mathrm{~kg} / \mathrm{m}^{3}$ or $u_{r}(\rho)=4.4 \%$.

The measured densities using VTD densitometer with the FPMC calibration procedure in this work, were already validated in the authors' previous publication [36] for the $\mathrm{CO}_{2}-\mathrm{H}_{2} \mathrm{~S}$
system by comparing the measured values of $\mathrm{CO}_{2}-\mathrm{H}_{2} \mathrm{~S}$ to the data published by Stouffer et al. [47][48] at two isotherms.

The measured densities were employed to evaluate accuracy of various equations of state in this work. As summarised in Table 9, first the classical cubic EoSs were tested. The AAD for the SRK-EoS in the gas, liquid and supercritical phases is $2.4 \%, 8.2 \%$ and $9.6 \%$ with an overall AAD of $7.4 \%$ and MAD of $15.2 \%$. Those for the PR-EoS was $1.8 \%, 3.2 \%$ and $2.4 \%$ with an overall AAD of $2.6 \%$ and MAD of $7.6 \%$. The AAD for the VPT-EoS is $1.8 \%, 1.9 \%$ and $2.6 \%$ in the gas, liquid and supercritical phases with an overall AAD of $2.1 \%$. The most accurate EoS in the gas phase is VPT and PR EoSs with an AAD of 1.8\%, VPT-EoS in the liquid phase with the AAD of $1.9 \%$ and PR-EoS in the supercritical phase with the AAD of $2.4 \%$. However, the VPT-EoS is the most accurate among them with the overall AAD of $2.1 \%$ and MAD of $8.0 \%$.

Introducing the $\mathrm{CO}_{2}$ correction term [30][46] to the above EoSs then could significantly improve their prediction accuracy for the densities of the investigated binary system. The overall AAD of SRK-CO ${ }_{2}$ and PR-CO 2 EoSs is $1.0 \%$ (reduced from $7.4 \%$ and $2.6 \%$ to $1.0 \%$ ) which are the most accurate EoSs with the $\mathrm{CO}_{2}$ volume correction term. The MAD for these are 8.0 and $7.4 \%$, respectively. $\mathrm{PR}-\mathrm{CO}_{2}$ in the gas phase (with the AAD of $1.7 \%$ ) and SRK$\mathrm{CO}_{2}$ in the liquid and supercritical phases (with the AAD of $0.6 \%$ and $0.8 \%$ ) are the most accurate EoS in the different phases. In addition to the $\mathrm{CO}_{2}$ volume correction term, the Peneloux shift parameter also was introduced to the SRK and PR EoSs. This could also reduce the overall AAD to $2.6 \%$ and $2.1 \%$ for the SRK and PR EoSs, respectively. Among all classical cubic EoSs, the PR-CO2 with the AAD and MAD of $1.0 \%$ and $7.4 \%$ is the most accurate EoS for the investigated mixture.

Apart from classical cubic EoSs, the multi parameter EoS also were evaluated using the measured densities. As shown in Table 9, the multi parameter EoS predicts the densities more accurately compared to the classical EoSs. The AAD of multi parameter EoS from the measured densities in the gas, liquid and supercritical phases are $1.6 \%, 0.2 \%$ and $0.6 \%$ with the overall AAD and MAD of $0.6 \%$ and $8.0 \%$. Figure 4 shows the deviations of the multi parameter EoS from the measured densities.

The compressibility factor of the investigated mixture were derived from the measured densities, which were reported in Tables 3 to 7 . Figures 5 and 6 show the derived z-factors at
all pressure ranges and at pressures lower than 10 MPa , respectively. The lines in these figures demonstrate the predicted z-factors using the multi parameter EoS at each isotherms. As can be seen, they are in good agreement and the AAD of the multi parameter EoS from the derived z -factors is $1.6 \%, 0.2 \%$ and $0.6 \%$ in the gas, liquid and supercritical phases. The overall AAD is also $0.6 \%$.

The isobaric specific heat capacities were calculated from thermodynamic equations and using the measured densities at various pressure and temperature. The $C_{p}$ were calculated at the constant pressures of $15,20,25,30,35$ and 40 MPa using Equation (3). The measured specific heat capacities were compared against the predictions using the multi parameter EoS. As shown in Table 10, the AAD of the multi parameter EoS from the derived values is $5.8 \%$ which shows the model predictions and the experimentally derived values are in the good agreement. Figure 7 also shows the determined specific heat capacities at different pressures. The lines in the figure show the predicted specific heat capacities using the multi parameter EoS. However, it is suggested that these values should be compared to the directly measured heat capacities, e.g., measured $C_{p}$ using adapted calorimeters.

The procedure of conducting the tests in each isotherm was injecting the sample fluid at a very slow rate to reach the dew point and continuing on the injection to reach the bubble point and further injection to achieve the desired pressure. Continuous data recording during the test, particularly in the vicinity of the dew and bubble points, allows fitting the representative correlation to the experimental data on each side of the dew or bubble point. Therefore, the precise location of the dew or bubble point could be determined by crossing the fitted correlations. The calculated bubble points at two isotherms of 273 K and 283 K as well as the predicted amounts using PR-CO $\mathrm{CO}_{2}$ EoS were summarised in Table 11. An overall AAD of $3.6 \%$ was achieved by comparing the measured and predicted values. Figures 8 shows the bubble point measurements. The circle points in this figure show the cross points of the fitted correlations which correspond to the dew or bubble points. The conclusion of this comparison is that the densitometer is not very accurate for estimation of bubble and dew point pressure. In comparison with VLE prediction using PR-CO2 EoS, there is a difference of at least 0.1 MPa , which is higher than experimental uncertainty of pressure using the static analytical method [25].

## 5. Conclusion

The densities of $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ binary mixture were measured using VTD densitometer, Anton Paar DMA 512, in the gas, liquid and supercritical phases. The densitometer was first calibrated using pure $\mathrm{CO}_{2}$ and the FPMC calibration technique. Then, the densities of a $0.9503 \mathrm{CO}_{2}-0.0497 \mathrm{SO}_{2}$ mixture were measured at temperatures of $273,283,323$ and 353 K . In addition the densities of $0.9478 \mathrm{CO}_{2}-0.0522 \mathrm{SO}_{2}$ were measured at 298 K . The overall average uncertainty of the measured densities with a confidence level of $95 \%$ was $u_{r}(\rho)=$ $0.2 \%$ or $u(\rho)=0.4 \mathrm{~kg} / \mathrm{m}^{3}$. The highest uncertainties were observed at very low pressure conditions in the gas phase or in the vicinity of the bubble point curve in the liquid phase. The measured densities were employed to evaluate classical cubic EoSs, those with $\mathrm{CO}_{2}$ volume correction term and Peneloux shift parameter as well as the multi parameter EoS. Among the classical EoSs, the PR-CO $\mathrm{CO}_{2}$ was the most accurate EoS for the investigated mixture with an AAD of $1.0 \%$ and MAD of $7.4 \%$. However, the multi parameter EoS was the most accurate EoS with an AAD of only $0.6 \%$ and MAD of $8.0 \%$. From the measured densities for the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system, the thermodynamic properties were derived and compared to the EoSs. The compressibility factor was in a good agreement with the multi parameter EoS with an AAD of $0.6 \%$. The isobaric specific heat capacity was derived from thermodynamic equations and measured densities. The AAD of the predicted specific heat capacity using the multi parameter EoS from the derived quantities was $5.8 \%$. The bubble points at two different isotherms of 273 and 283 K were measured by fitting the equations to the numerous measured densities on both sides of bubble points. The AAD of the predicted bubble points using $\mathrm{PR}-\mathrm{CO}_{2} \mathrm{EoS}$ from the measured values was $3.6 \%$.

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Table 1 - Details of the chemicals, suppliers and purities of the components used in this study.

| Chemical Name | Source | Initial Purity $^{\text {a }}$ | Certification | Analysis Method ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{SO}_{2}$ | Air Liquide | 0.995 vol | Air Liquide Certified | SM |
| $\mathrm{CO}_{2}$ | Air Liquide | 0.99995 vol | Air Liquide Certified | SM |

[^0]Table 2 - Constants B to F in the Aly \& Lee equation [45]

| $\mathrm{C}_{\mathrm{pi}}$ constants | $B$ | $C$ | $D$ | $E$ | $F$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CO}_{2}$ | 29400 | 34500 | -1430 | 26400 | 588 |
| $\mathrm{SO}_{2}$ | 33400 | 25900 | 933 | 10900 | 424 |

Table 3 - Experimental results of the 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ system at $273 \mathrm{~K}^{\text {a }}$

| No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ |  | Z | No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ |  | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Exp. | $u_{c}(\rho)$ |  |  |  |  |  | Exp. | $u_{c}(\rho)$ |  |
| 1 | Gas | 272.65 | 0.226 | 4.8 | 0.1 | 0.93 | 44 | Liquid | 273.55 | 25.039 | 1063.6 | 0.3 | 0.47 |
| 2 | Gas | 272.65 | 0.407 | 8.5 | 0.1 | 0.95 | 45 | Liquid | 273.55 | 24.523 | 1061.9 | 0.2 | 0.46 |
| 3 | Gas | 272.65 | 0.503 | 10.6 | 0.1 | 0.94 | 46 | Liquid | 273.55 | 24.032 | 1060.4 | 0.3 | 0.45 |
| 4 | Gas | 272.65 | 0.752 | 16.2 | 0.1 | 0.92 | 47 | Liquid | 273.56 | 23.496 | 1058.4 | 0.3 | 0.44 |
| 5 | Gas | 272.65 | 1.013 | 22.1 | 0.1 | 0.91 | 48 | Liquid | 273.57 | 23.015 | 1056.6 | 0.3 | 0.43 |
| 6 | Gas | 272.65 | 1.252 | 27.9 | 0.1 | 0.89 | 49 | Liquid | 273.56 | 22.501 | 1054.9 | 0.2 | 0.42 |
| 7 | Gas | 272.65 | 1.506 | 34.4 | 0.1 | 0.87 | 50 | Liquid | 273.56 | 21.993 | 1053.0 | 0.3 | 0.41 |
| 8 | Gas | 272.65 | 1.752 | 40.9 | 0.2 | 0.85 | 51 | Liquid | 273.56 | 21.519 | 1051.3 | 0.3 | 0.41 |
| 9 | Gas | 272.65 | 1.998 | 47.9 | 0.2 | 0.83 | 52 | Liquid | 273.56 | 21.029 | 1049.7 | 0.3 | 0.40 |
| 10 | Liquid | 273.54 | 41.723 | 1110.7 | 0.2 | 0.74 | 53 | Liquid | 273.55 | 20.535 | 1047.9 | 0.2 | 0.39 |
| 11 | Liquid | 273.56 | 41.601 | 1110.4 | 0.2 | 0.74 | 54 | Liquid | 273.56 | 20.028 | 1046.0 | 0.3 | 0.38 |
| 12 | Liquid | 273.55 | 41.016 | 1109.0 | 0.2 | 0.73 | 55 | Liquid | 273.56 | 19.509 | 1044.0 | 0.2 | 0.37 |
| 13 | Liquid | 273.55 | 40.508 | 1107.8 | 0.2 | 0.72 | 56 | Liquid | 273.56 | 19.000 | 1042.1 | 0.3 | 0.36 |
| 14 | Liquid | 273.55 | 40.023 | 1106.6 | 0.1 | 0.72 | 57 | Liquid | 273.56 | 18.515 | 1040.1 | 0.3 | 0.35 |
| 15 | Liquid | 273.55 | 39.553 | 1105.7 | 0.2 | 0.71 | 58 | Liquid | 273.56 | 18.049 | 1038.2 | 0.3 | 0.34 |
| 16 | Liquid | 273.55 | 38.992 | 1104.0 | 0.2 | 0.70 | 59 | Liquid | 273.56 | 17.514 | 1036.2 | 0.3 | 0.33 |
| 17 | Liquid | 273.54 | 38.558 | 1103.1 | 0.2 | 0.69 | 60 | Liquid | 273.57 | 17.024 | 1034.2 | 0.3 | 0.33 |
| 18 | Liquid | 273.54 | 38.033 | 1101.8 | 0.2 | 0.68 | 61 | Liquid | 273.57 | 16.500 | 1031.9 | 0.3 | 0.32 |
| 19 | Liquid | 273.54 | 37.529 | 1100.5 | 0.2 | 0.67 | 62 | Liquid | 273.57 | 15.999 | 1029.8 | 0.3 | 0.31 |
| 20 | Liquid | 273.54 | 37.047 | 1099.0 | 0.2 | 0.67 | 63 | Liquid | 273.58 | 15.602 | 1028.1 | 0.3 | 0.30 |
| 21 | Liquid | 273.54 | 36.490 | 1097.6 | 0.2 | 0.66 | 64 | Liquid | 273.57 | 14.951 | 1025.4 | 0.3 | 0.29 |
| 22 | Liquid | 273.54 | 36.045 | 1096.7 | 0.2 | 0.65 | 65 | Liquid | 273.57 | 14.518 | 1023.6 | 0.3 | 0.28 |
| 23 | Liquid | 273.54 | 35.534 | 1095.1 | 0.2 | 0.64 | 66 | Liquid | 273.56 | 23.496 | 1058.4 | 0.3 | 0.44 |
| 24 | Liquid | 273.54 | 35.043 | 1093.9 | 0.3 | 0.63 | 67 | Liquid | 273.56 | 13.506 | 1019.3 | 0.3 | 0.26 |
| 25 | Liquid | 273.54 | 34.491 | 1092.3 | 0.2 | 0.62 | 68 | Liquid | 273.56 | 13.012 | 1017.2 | 0.3 | 0.25 |
| 26 | Liquid | 273.54 | 34.032 | 1091.1 | 0.2 | 0.62 | 69 | Liquid | 273.56 | 12.509 | 1014.7 | 0.3 | 0.24 |
| 27 | Liquid | 273.54 | 33.521 | 1089.7 | 0.2 | 0.61 | 70 | Liquid | 273.57 | 12.005 | 1012.2 | 0.3 | 0.23 |
| 28 | Liquid | 273.54 | 33.027 | 1088.3 | 0.2 | 0.60 | 71 | Liquid | 273.57 | 11.502 | 1009.5 | 0.3 | 0.23 |
| 29 | Liquid | 273.54 | 32.491 | 1086.7 | 0.3 | 0.59 | 72 | Liquid | 273.57 | 11.003 | 1007.0 | 0.3 | 0.22 |
| 30 | Liquid | 273.54 | 31.975 | 1085.1 | 0.2 | 0.58 | 73 | Liquid | 273.57 | 10.516 | 1004.5 | 0.4 | 0.21 |
| 31 | Liquid | 273.55 | 31.482 | 1083.6 | 0.2 | 0.57 | 74 | Liquid | 273.57 | 9.944 | 1001.9 | 0.3 | 0.20 |
| 32 | Liquid | 273.55 | 30.952 | 1082.2 | 0.2 | 0.57 | 75 | Liquid | 273.58 | 9.518 | 999.7 | 0.4 | 0.19 |
| 33 | Liquid | 273.54 | 30.524 | 1080.9 | 0.2 | 0.56 | 76 | Liquid | 273.58 | 9.008 | 996.7 | 0.4 | 0.18 |
| 34 | Liquid | 273.55 | 30.026 | 1079.4 | 0.3 | 0.55 | 77 | Liquid | 273.58 | 8.503 | 993.8 | 0.4 | 0.17 |
| 35 | Liquid | 273.54 | 29.514 | 1077.7 | 0.2 | 0.54 | 78 | Liquid | 273.60 | 8.003 | 990.6 | 0.4 | 0.16 |
| 36 | Liquid | 273.54 | 29.024 | 1076.3 | 0.2 | 0.53 | 79 | Liquid | 273.60 | 7.688 | 987.5 | 0.4 | 0.15 |
| 37 | Liquid | 273.55 | 28.539 | 1074.9 | 0.2 | 0.53 | 80 | Liquid | 273.60 | 7.034 | 984.6 | 0.4 | 0.14 |
| 38 | Liquid | 273.55 | 28.041 | 1073.0 | 0.3 | 0.52 | 81 | Liquid | 273.60 | 6.503 | 981.9 | 0.4 | 0.13 |
| 39 | Liquid | 273.55 | 27.554 | 1071.7 | 0.2 | 0.51 | 82 | Liquid | 273.60 | 6.005 | 978.7 | 0.4 | 0.12 |
| 40 | Liquid | 273.54 | 26.999 | 1069.9 | 0.2 | 0.50 | 83 | Liquid | 273.60 | 5.521 | 975.5 | 0.4 | 0.11 |
| 41 | Liquid | 273.55 | 26.484 | 1068.3 | 0.2 | 0.49 | 84 | Liquid | 273.61 | 5.013 | 972.1 | 0.4 | 0.10 |
| 42 | Liquid | 273.55 | 26.016 | 1066.9 | 0.3 | 0.48 | 85 | Liquid | 273.61 | 4.518 | 968.2 | 0.4 | 0.09 |
| 43 | Liquid | 273.54 | 25.506 | 1065.1 | 0.2 | 0.47 | 86 | Liquid | 273.60 | 4.001 | 964.9 | 0.5 | 0.08 |

${ }^{\frac{a}{a}}$ Standard uncertainties, $u$, are $u(T)=0.02 \mathrm{~K}, u(p)=0.002 \mathrm{MPa}$ for pressures up to 10 MPa and $u(p)=0.005$ MPa for pressures from $10-40 \mathrm{MPa}$, for $\mathrm{SO}_{2} u(z)=0.0001$ and for $\mathrm{CO}_{2} u(z)=0.0018$

Table 4 - Experimental results of the 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ system at $283 \mathrm{~K}^{\text {a }}$

| No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} . \mathrm{m}^{-3}$ |  | Z | No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} . \mathrm{m}^{-3}$ |  | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Exp. | $u_{c}(\rho)$ |  |  |  |  |  | Exp. | $u_{c}(\rho)$ |  |
| 1 | Gas | 282.66 | 0.120 | 2.5 | 0.1 | 0.92 | 48 | Liquid | 283.32 | 26.503 | 1034.9 | 0.3 | 0.49 |
| 2 | Gas | 282.66 | 0.211 | 4.3 | 0.1 | 0.94 | 49 | Liquid | 283.32 | 26.038 | 1033.5 | 0.2 | 0.48 |
| 3 | Gas | 282.66 | 0.301 | 6.1 | 0.1 | 0.94 | 50 | Liquid | 283.32 | 25.509 | 1031.3 | 0.3 | 0.47 |
| 4 | Gas | 282.66 | 0.408 | 8.5 | 0.1 | 0.92 | 51 | Liquid | 283.32 | 25.025 | 1029.4 | 0.3 | 0.46 |
| 5 | Gas | 282.66 | 0.511 | 10.6 | 0.1 | 0.92 | 52 | Liquid | 283.32 | 24.535 | 1027.4 | 0.3 | 0.46 |
| 6 | Gas | 282.66 | 0.608 | 12.3 | 0.1 | 0.95 | 53 | Liquid | 283.33 | 24.074 | 1025.3 | 0.2 | 0.45 |
| 7 | Gas | 282.65 | 0.800 | 16.5 | 0.1 | 0.93 | 54 | Liquid | 283.32 | 23.509 | 1023.3 | 0.2 | 0.44 |
| 8 | Gas | 282.66 | 1.009 | 21.1 | 0.1 | 0.92 | 55 | Liquid | 283.32 | 23.052 | 1021.8 | 0.3 | 0.43 |
| 9 | Gas | 282.65 | 1.249 | 26.3 | 0.1 | 0.91 | 56 | Liquid | 283.32 | 22.565 | 1019.8 | 0.3 | 0.42 |
| 10 | Gas | 282.66 | 1.509 | 32.8 | 0.1 | 0.88 | 57 | Liquid | 283.32 | 22.046 | 1017.6 | 0.2 | 0.41 |
| 11 | Gas | 282.66 | 1.705 | 37.5 | 0.1 | 0.87 | 58 | Liquid | 283.32 | 21.504 | 1015.3 | 0.3 | 0.40 |
| 12 | Gas | 282.66 | 1.909 | 42.7 | 0.1 | 0.86 | 59 | Liquid | 283.32 | 21.035 | 1013.2 | 0.2 | 0.40 |
| 13 | Gas | 282.66 | 2.010 | 45.2 | 0.1 | 0.85 | 60 | Liquid | 283.32 | 20.507 | 1011.0 | 0.3 | 0.39 |
| 14 | Gas | 282.66 | 2.199 | 50.5 | 0.2 | 0.83 | 61 | Liquid | 283.32 | 20.038 | 1008.7 | 0.3 | 0.38 |
| 15 | Gas | 282.66 | 2.508 | 59.6 | 0.2 | 0.81 | 62 | Liquid | 283.32 | 19.496 | 1006.2 | 0.3 | 0.37 |
| 16 | Gas | 282.66 | 2.702 | 65.5 | 0.2 | 0.79 | 63 | Liquid | 283.32 | 19.016 | 1004.1 | 0.3 | 0.36 |
| 17 | Gas | 282.66 | 3.008 | 76.0 | 0.2 | 0.76 | 64 | Liquid | 283.32 | 18.520 | 1001.7 | 0.3 | 0.35 |
| 18 | Liquid | 283.32 | 40.729 | 1080.4 | 0.2 | 0.72 | 65 | Liquid | 283.33 | 18.078 | 999.5 | 0.3 | 0.35 |
| 19 | Liquid | 283.33 | 40.700 | 1080.6 | 0.2 | 0.72 | 66 | Liquid | 283.32 | 17.551 | 996.8 | 0.3 | 0.34 |
| 20 | Liquid | 283.33 | 40.601 | 1080.3 | 0.2 | 0.72 | 67 | Liquid | 283.32 | 17.047 | 994.7 | 0.3 | 0.33 |
| 21 | Liquid | 283.33 | 40.145 | 1078.8 | 0.2 | 0.71 | 68 | Liquid | 283.32 | 16.561 | 992.4 | 0.3 | 0.32 |
| 22 | Liquid | 283.32 | 39.558 | 1077.4 | 0.2 | 0.70 | 69 | Liquid | 283.32 | 16.044 | 989.5 | 0.3 | 0.31 |
| 23 | Liquid | 283.32 | 39.056 | 1076.1 | 0.2 | 0.69 | 70 | Liquid | 283.32 | 15.505 | 986.8 | 0.4 | 0.30 |
| 24 | Liquid | 283.32 | 38.461 | 1074.6 | 0.2 | 0.68 | 71 | Liquid | 283.32 | 15.011 | 984.1 | 0.3 | 0.29 |
| 25 | Liquid | 283.31 | 38.061 | 1073.3 | 0.2 | 0.68 | 72 | Liquid | 283.32 | 14.496 | 980.8 | 0.4 | 0.28 |
| 26 | Liquid | 283.31 | 37.578 | 1072.1 | 0.2 | 0.67 | 73 | Liquid | 283.33 | 14.003 | 978.2 | 0.4 | 0.27 |
| 27 | Liquid | 283.32 | 37.026 | 1070.5 | 0.2 | 0.66 | 74 | Liquid | 283.32 | 13.536 | 975.3 | 0.4 | 0.27 |
| 28 | Liquid | 283.31 | 36.515 | 1068.6 | 0.2 | 0.65 | 75 | Liquid | 283.32 | 13.000 | 972.6 | 0.4 | 0.26 |
| 29 | Liquid | 283.31 | 36.037 | 1067.5 | 0.2 | 0.64 | 76 | Liquid | 283.32 | 12.514 | 969.7 | 0.4 | 0.25 |
| 30 | Liquid | 283.31 | 35.516 | 1065.8 | 0.2 | 0.64 | 77 | Liquid | 283.32 | 12.009 | 966.2 | 0.4 | 0.24 |
| 31 | Liquid | 283.32 | 34.989 | 1064.3 | 0.2 | 0.63 | 78 | Liquid | 283.33 | 11.512 | 963.0 | 0.4 | 0.23 |
| 32 | Liquid | 283.31 | 34.500 | 1062.8 | 0.2 | 0.62 | 79 | Liquid | 283.32 | 11.007 | 959.9 | 0.4 | 0.22 |
| 33 | Liquid | 283.32 | 33.995 | 1060.8 | 0.2 | 0.61 | 80 | Liquid | 283.32 | 10.507 | 956.6 | 0.4 | 0.21 |
| 34 | Liquid | 283.32 | 33.527 | 1059.6 | 0.2 | 0.60 | 81 | Liquid | 283.32 | 9.995 | 953.3 | 0.4 | 0.20 |
| 35 | Liquid | 283.32 | 33.032 | 1057.9 | 0.2 | 0.60 | 82 | Liquid | 283.32 | 9.510 | 949.7 | 0.4 | 0.19 |
| 36 | Liquid | 283.32 | 32.516 | 1056.2 | 0.2 | 0.59 | 83 | Liquid | 283.33 | 9.019 | 946.2 | 0.4 | 0.18 |
| 37 | Liquid | 283.32 | 32.033 | 1054.6 | 0.3 | 0.58 | 84 | Liquid | 283.33 | 8.543 | 942.8 | 0.5 | 0.17 |
| 38 | Liquid | 283.32 | 31.500 | 1052.8 | 0.2 | 0.57 | 85 | Liquid | 283.32 | 8.008 | 938.7 | 0.5 | 0.16 |
| 39 | Liquid | 283.32 | 31.007 | 1050.9 | 0.3 | 0.56 | 86 | Liquid | 283.32 | 7.506 | 934.7 | 0.5 | 0.15 |
| 40 | Liquid | 283.32 | 30.506 | 1049.6 | 0.3 | 0.56 | 87 | Liquid | 283.32 | 7.000 | 929.5 | 0.5 | 0.14 |
| 41 | Liquid | 283.32 | 30.008 | 1047.3 | 0.3 | 0.55 | 88 | Liquid | 283.32 | 6.507 | 925.6 | 0.5 | 0.13 |
| 42 | Liquid | 283.32 | 29.470 | 1045.7 | 0.2 | 0.54 | 89 | Liquid | 283.32 | 6.002 | 920.8 | 0.5 | 0.12 |
| 43 | Liquid | 283.32 | 29.081 | 1044.1 | 0.3 | 0.53 | 90 | Liquid | 283.32 | 5.506 | 916.4 | 0.6 | 0.11 |
| 44 | Liquid | 283.32 | 28.527 | 1042.4 | 0.2 | 0.52 | 91 | Liquid | 283.32 | 5.005 | 910.4 | 0.6 | 0.11 |
| 45 | Liquid | 283.32 | 28.043 | 1040.7 | 0.2 | 0.51 | 92 | Liquid | 283.33 | 4.499 | 904.4 | 0.6 | 0.10 |
| 46 | Liquid | 283.31 | 27.537 | 1038.9 | 0.2 | 0.51 | 93 | Liquid | 283.33 | 4.307 | 902.3 | 0.6 | 0.09 |
| 47 | Liquid | 283.32 | 27.023 | 1037.0 | 0.2 | 0.50 |  |  |  |  |  |  |  |

${ }^{\bar{a}}$ Standard uncertainties, $u$, are $u(T)=0.02 \mathrm{~K}, u(p)=0.002 \mathrm{MPa}$ for pressures up to 10 MPa and $u(p)=0.005 \mathrm{MPa}$ for pressures from $10-40 \mathrm{MPa}$, for $\mathrm{SO}_{2} u(z)=0.0001$ and for $\mathrm{CO}_{2} u(z)=0.0018$

Table 5 - Experimental results of the 0.9478 mole $\mathrm{CO}_{2}+0.0522$ mole $\mathrm{SO}_{2}$ system at $298 \mathrm{~K}^{\text {a }}$

| No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ |  | Z | No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ |  | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Exp. | $u_{c}(\rho)$ |  |  |  |  |  | Exp. | $u_{c}(\rho)$ |  |
| 1 | Gas | 297.42 | 0.051 | 1.0 | 0.0 | 0.93 | 47 | Liquid | 298.11 | 28.987 | 993.1 | 0.3 | 0.53 |
| 2 | Gas | 297.41 | 0.100 | 1.8 | 0.1 | 1.01 | 48 | Liquid | 298.10 | 28.400 | 990.6 | 0.3 | 0.52 |
| 3 | Gas | 297.41 | 0.200 | 3.6 | 0.1 | 1.01 | 49 | Liquid | 298.10 | 27.973 | 988.6 | 0.3 | 0.51 |
| 4 | Gas | 297.42 | 0.397 | 7.5 | 0.1 | 0.96 | 50 | Liquid | 298.10 | 27.508 | 986.6 | 0.3 | 0.51 |
| 5 | Gas | 297.42 | 0.502 | 9.4 | 0.1 | 0.97 | 51 | Liquid | 298.10 | 27.025 | 984.3 | 0.3 | 0.50 |
| 6 | Gas | 297.42 | 1.817 | 37.6 | 0.1 | 0.88 | 52 | Liquid | 298.09 | 26.503 | 982.1 | 0.3 | 0.49 |
| 7 | Gas | 297.41 | 2.012 | 42.1 | 0.1 | 0.87 | 53 | Liquid | 298.09 | 26.076 | 980.0 | 0.3 | 0.48 |
| 8 | Gas | 297.41 | 2.215 | 47.2 | 0.1 | 0.86 | 54 | Liquid | 298.10 | 25.593 | 977.9 | 0.3 | 0.48 |
| 9 | Gas | 297.42 | 2.421 | 53.0 | 0.1 | 0.83 | 55 | Liquid | 298.10 | 25.050 | 975.1 | 0.3 | 0.47 |
| 10 | Gas | 297.42 | 2.588 | 57.0 | 0.1 | 0.83 | 56 | Liquid | 298.10 | 24.505 | 972.6 | 0.3 | 0.46 |
| 11 | Gas | 297.42 | 2.854 | 64.1 | 0.2 | 0.81 | 57 | Liquid | 298.10 | 24.029 | 970.2 | 0.3 | 0.45 |
| 12 | Gas | 297.44 | 3.064 | 70.1 | 0.2 | 0.80 | 58 | Liquid | 298.10 | 23.522 | 967.7 | 0.3 | 0.44 |
| 13 | Gas | 297.43 | 3.223 | 74.6 | 0.2 | 0.79 | 59 | Liquid | 298.11 | 23.041 | 965.2 | 0.3 | 0.43 |
| 14 | Gas | 297.43 | 3.396 | 79.8 | 0.2 | 0.78 | 60 | Liquid | 298.10 | 22.537 | 962.6 | 0.3 | 0.43 |
| 15 | Gas | 297.42 | 3.638 | 87.4 | 0.2 | 0.76 | 61 | Liquid | 298.10 | 21.994 | 959.8 | 0.3 | 0.42 |
| 16 | Gas | 297.42 | 3.822 | 93.7 | 0.2 | 0.74 | 62 | Liquid | 298.11 | 21.501 | 957.0 | 0.3 | 0.41 |
| 17 | Gas | 297.42 | 3.996 | 99.9 | 0.2 | 0.73 | 63 | Liquid | 298.10 | 21.016 | 954.5 | 0.4 | 0.40 |
| 18 | Gas | 297.43 | 4.206 | 107.7 | 0.2 | 0.71 | 64 | Liquid | 298.11 | 20.492 | 951.5 | 0.4 | 0.39 |
| 19 | Gas | 297.42 | 4.401 | 115.6 | 0.3 | 0.69 | 65 | Liquid | 298.11 | 20.051 | 948.9 | 0.4 | 0.38 |
| 20 | Gas | 297.42 | 4.507 | 120.1 | 0.3 | 0.68 | 66 | Liquid | 298.11 | 19.477 | 945.6 | 0.4 | 0.37 |
| 21 | Gas | 297.42 | 4.600 | 124.4 | 0.3 | 0.67 | 67 | Liquid | 298.11 | 19.025 | 942.9 | 0.4 | 0.37 |
| 22 | Gas | 297.42 | 4.703 | 129.2 | 0.3 | 0.66 | 68 | Liquid | 298.11 | 18.527 | 939.8 | 0.4 | 0.36 |
| 23 | Gas | 297.40 | 4.803 | 134.4 | 0.6 | 0.65 | 69 | Liquid | 298.11 | 17.978 | 936.5 | 0.4 | 0.35 |
| 24 | Liquid | 298.12 | 40.411 | 1032.1 | 0.2 | 0.71 | 70 | Liquid | 298.11 | 17.492 | 933.3 | 0.4 | 0.34 |
| 25 | Liquid | 298.11 | 40.060 | 1031.1 | 0.3 | 0.71 | 71 | Liquid | 298.11 | 17.024 | 930.2 | 0.4 | 0.33 |
| 26 | Liquid | 298.11 | 39.519 | 1029.5 | 0.2 | 0.70 | 72 | Liquid | 298.11 | 16.534 | 926.8 | 0.4 | 0.32 |
| 27 | Liquid | 298.11 | 38.913 | 1027.8 | 0.3 | 0.69 | 73 | Liquid | 298.11 | 16.016 | 923.0 | 0.4 | 0.32 |
| 28 | Liquid | 298.11 | 38.545 | 1026.6 | 0.3 | 0.68 | 74 | Liquid | 298.11 | 15.500 | 919.1 | 0.4 | 0.31 |
| 29 | Liquid | 298.11 | 37.960 | 1024.8 | 0.2 | 0.67 | 75 | Liquid | 298.11 | 15.011 | 915.2 | 0.4 | 0.30 |
| 30 | Liquid | 298.11 | 37.574 | 1023.6 | 0.2 | 0.67 | 76 | Liquid | 298.12 | 14.500 | 910.9 | 0.5 | 0.29 |
| 31 | Liquid | 298.10 | 37.078 | 1022.0 | 0.2 | 0.66 | 77 | Liquid | 298.12 | 14.006 | 906.7 | 0.5 | 0.28 |
| 32 | Liquid | 298.10 | 36.493 | 1020.2 | 0.3 | 0.65 | 78 | Liquid | 298.11 | 13.500 | 902.3 | 0.5 | 0.27 |
| 33 | Liquid | 298.10 | 35.971 | 1018.4 | 0.2 | 0.64 | 79 | Liquid | 298.11 | 13.010 | 897.8 | 0.5 | 0.26 |
| 34 | Liquid | 298.11 | 35.494 | 1016.9 | 0.2 | 0.63 | 80 | Liquid | 298.12 | 12.503 | 892.9 | 0.5 | 0.25 |
| 35 | Liquid | 298.10 | 35.077 | 1015.5 | 0.2 | 0.63 | 81 | Liquid | 298.12 | 12.000 | 887.9 | 0.5 | 0.25 |
| 36 | Liquid | 298.10 | 34.441 | 1013.3 | 0.3 | 0.62 | 82 | Liquid | 298.12 | 11.504 | 882.9 | 0.5 | 0.24 |
| 37 | Liquid | 298.11 | 33.949 | 1011.6 | 0.2 | 0.61 | 83 | Liquid | 298.11 | 11.004 | 877.7 | 0.6 | 0.23 |
| 38 | Liquid | 298.10 | 33.435 | 1009.8 | 0.3 | 0.60 | 84 | Liquid | 298.11 | 10.505 | 872.1 | 0.6 | 0.22 |
| 39 | Liquid | 298.10 | 33.068 | 1008.6 | 0.2 | 0.60 | 85 | Liquid | 298.12 | 10.039 | 866.6 | 0.6 | 0.21 |
| 40 | Liquid | 298.10 | 32.518 | 1006.5 | 0.2 | 0.59 | 86 | Liquid | 298.12 | 9.508 | 860.5 | 0.6 | 0.20 |
| 41 | Liquid | 298.10 | 32.016 | 1004.6 | 0.2 | 0.58 | 87 | Liquid | 298.10 | 9.007 | 854.0 | 0.7 | 0.19 |
| 42 | Liquid | 298.11 | 31.516 | 1002.6 | 0.2 | 0.57 | 88 | Liquid | 298.11 | 8.501 | 846.7 | 0.7 | 0.18 |
| 43 | Liquid | 298.11 | 30.997 | 1000.7 | 0.2 | 0.56 | 89 | Liquid | 298.11 | 8.006 | 838.7 | 0.8 | 0.17 |
| 44 | Liquid | 298.11 | 30.505 | 998.9 | 0.3 | 0.56 | 90 | Liquid | 298.11 | 7.503 | 829.8 | 0.8 | 0.16 |
| 45 | Liquid | 298.11 | 30.013 | 996.8 | 0.3 | 0.55 | 91 | Liquid | 298.10 | 7.001 | 819.7 | 0.9 | 0.16 |
| 46 | Liquid | 298.11 | 29.543 | 994.8 | 0.3 | 0.54 |  |  |  |  |  |  |  |

${ }^{2}$ Standard uncertainties, $u$, are $u(T)=0.02 \mathrm{~K}, u(p)=0.002 \mathrm{MPa}$ for pressures up to 10 MPa and $u(p)=0.005$ MPa for pressures from $10-40 \mathrm{MPa}$, for $\mathrm{SO}_{2} u(z)=0.0001$ and for $\mathrm{CO}_{2} u(z)=0.0018$

Table 6 - Experimental results of the 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ system at $323 \mathrm{~K}^{\text {a }}$

| No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} . \mathrm{m}^{-3}$ |  | Z | No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg}$ |  | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Exp. | $u_{c}(\rho)$ |  |  |  |  |  | Exp. | $u_{c}(\rho)$ |  |
| 1 | SC | 322.47 | 40.947 | 956.3 | 0.3 | 0.72 | 44 | SC | 322.50 | 19.491 | 818.5 | 0.5 | 0.40 |
| 2 | SC | 322.48 | 40.902 | 956.7 | 0.3 | 0.72 | 45 | SC | 322.49 | 19.008 | 812.8 | 0.5 | 0.39 |
| 3 | SC | 322.48 | 40.153 | 953.9 | 0.3 | 0.71 | 46 | SC | 322.50 | 18.503 | 806.6 | 0.6 | 0.39 |
| 4 | SC | 322.48 | 39.641 | 951.7 | 0.3 | 0.70 | 47 | SC | 322.49 | 18.008 | 800.3 | 0.6 | 0.38 |
| 5 | SC | 322.47 | 39.200 | 950.0 | 0.3 | 0.69 | 48 | SC | 322.50 | 17.499 | 793.5 | 0.6 | 0.37 |
| 6 | SC | 322.47 | 38.434 | 946.6 | 0.3 | 0.68 | 49 | SC | 322.51 | 17.005 | 786.2 | 0.6 | 0.36 |
| 7 | SC | 322.47 | 38.091 | 945.0 | 0.3 | 0.68 | 50 | SC | 322.51 | 16.502 | 779.1 | 0.7 | 0.36 |
| 8 | SC | 322.46 | 37.561 | 942.4 | 0.3 | 0.67 | 51 | SC | 322.52 | 16.003 | 770.9 | 0.7 | 0.35 |
| 9 | SC | 322.46 | 37.005 | 940.1 | 0.3 | 0.66 | 52 | SC | 322.52 | 15.501 | 761.8 | 0.7 | 0.34 |
| 10 | SC | 322.46 | 36.509 | 937.7 | 0.3 | 0.65 | 53 | SC | 322.52 | 15.012 | 753.2 | 0.8 | 0.33 |
| 11 | SC | 322.46 | 36.061 | 935.4 | 0.3 | 0.65 | 54 | SC | 322.52 | 14.504 | 742.9 | 0.8 | 0.33 |
| 12 | SC | 322.46 | 35.500 | 933.0 | 0.3 | 0.64 | 55 | SC | 322.52 | 14.000 | 731.9 | 0.9 | 0.32 |
| 13 | SC | 322.46 | 34.988 | 930.2 | 0.3 | 0.63 | 56 | SC | 322.53 | 13.501 | 720.4 | 1.0 | 0.31 |
| 14 | SC | 322.47 | 34.511 | 928.0 | 0.3 | 0.62 | 57 | SC | 322.54 | 13.000 | 706.7 | 1.1 | 0.31 |
| 15 | SC | 322.47 | 34.062 | 925.5 | 0.3 | 0.62 | 58 | SC | 322.53 | 12.505 | 691.1 | 1.2 | 0.30 |
| 16 | SC | 322.47 | 33.539 | 923.2 | 0.3 | 0.61 | 59 | SC | 322.51 | 12.003 | 672.3 | 1.4 | 0.30 |
| 17 | SC | 322.47 | 33.070 | 920.6 | 0.3 | 0.60 | 60 | SC | 322.51 | 11.504 | 649.9 | 1.7 | 0.30 |
| 18 | SC | 322.47 | 32.536 | 917.5 | 0.3 | 0.60 | 61 | SC | 322.49 | 11.003 | 621.1 | 2.1 | 0.30 |
| 19 | SC | 322.48 | 32.039 | 914.6 | 0.3 | 0.59 | 62 | SC | 322.47 | 10.501 | 585.0 | 2.7 | 0.30 |
| 20 | SC | 322.47 | 31.517 | 912.0 | 0.3 | 0.58 | 63 | SC | 322.46 | 9.992 | 538.0 | 2.0 | 0.31 |
| 21 | SC | 322.47 | 31.027 | 908.9 | 0.3 | 0.57 | 64 | SC | 322.45 | 9.501 | 460.8 | 2.5 | 0.35 |
| 22 | SC | 322.46 | 30.511 | 905.8 | 0.3 | 0.57 | 65 | SC | 322.41 | 9.006 | 371.0 | 1.9 | 0.41 |
| 23 | SC | 322.47 | 29.929 | 902.4 | 0.3 | 0.56 | 66 | SC | 322.41 | 8.521 | 307.2 | 1.1 | 0.47 |
| 24 | SC | 322.49 | 29.507 | 899.6 | 0.3 | 0.55 | 67 | SC | 322.41 | 8.037 | 254.6 | 0.7 | 0.53 |
| 25 | SC | 322.49 | 29.025 | 896.4 | 0.3 | 0.54 | 68 | SC | 322.39 | 7.504 | 218.4 | 0.5 | 0.58 |
| 26 | SC | 322.48 | 28.501 | 892.7 | 0.4 | 0.54 | 69 | SC | 322.39 | 7.009 | 189.5 | 0.4 | 0.62 |
| 27 | SC | 322.49 | 28.018 | 889.5 | 0.4 | 0.53 | 70 | SC | 322.41 | 6.514 | 166.3 | 0.3 | 0.66 |
| 28 | SC | 322.49 | 27.508 | 886.3 | 0.4 | 0.52 | 71 | Gas | 322.39 | 6.019 | 145.7 | 0.2 | 0.69 |
| 29 | SC | 322.48 | 27.026 | 882.9 | 0.4 | 0.51 | 72 | Gas | 322.39 | 5.528 | 127.9 | 0.2 | 0.73 |
| 30 | SC | 322.49 | 26.517 | 878.8 | 0.4 | 0.51 | 73 | Gas | 322.39 | 5.017 | 111.5 | 0.2 | 0.76 |
| 31 | SC | 322.49 | 26.001 | 875.4 | 0.4 | 0.50 | 74 | Gas | 322.39 | 4.519 | 96.9 | 0.2 | 0.78 |
| 32 | SC | 322.48 | 25.500 | 871.4 | 0.4 | 0.49 | 75 | Gas | 322.39 | 4.009 | 82.8 | 0.2 | 0.81 |
| 33 | SC | 322.50 | 25.003 | 867.7 | 0.4 | 0.48 | 76 | Gas | 322.39 | 3.512 | 70.9 | 0.1 | 0.83 |
| 34 | SC | 322.50 | 24.497 | 864.4 | 0.4 | 0.48 | 77 | Gas | 322.40 | 3.008 | 58.8 | 0.1 | 0.86 |
| 35 | SC | 322.49 | 24.003 | 860.4 | 0.4 | 0.47 | 78 | Gas | 322.40 | 2.511 | 48.1 | 0.1 | 0.88 |
| 36 | SC | 322.49 | 23.500 | 856.5 | 0.4 | 0.46 | 79 | Gas | 322.39 | 2.008 | 37.0 | 0.1 | 0.91 |
| 37 | SC | 322.48 | 23.049 | 853.3 | 0.4 | 0.45 | 80 | Gas | 322.39 | 1.707 | 31.7 | 0.1 | 0.90 |
| 38 | SC | 322.49 | 22.496 | 848.2 | 0.4 | 0.45 | 81 | Gas | 322.40 | 1.509 | 27.5 | 0.1 | 0.92 |
| 39 | SC | 322.49 | 22.009 | 843.9 | 0.4 | 0.44 | 82 | Gas | 322.39 | 1.252 | 22.2 | 0.1 | 0.95 |
| 40 | SC | 322.49 | 21.533 | 839.7 | 0.5 | 0.43 | 83 | Gas | 322.40 | 1.002 | 17.9 | 0.1 | 0.94 |
| 41 | SC | 322.49 | 21.007 | 834.7 | 0.5 | 0.42 | 84 | Gas | 322.40 | 0.749 | 13.6 | 0.1 | 0.92 |
| 42 | SC | 322.48 | 20.496 | 829.2 | 0.5 | 0.41 | 85 | Gas | 322.39 | 0.392 | 7.0 | 0.1 | 0.94 |
| 43 | SC | 322.49 | 20.012 | 824.3 | 0.5 | 0.41 |  |  |  |  |  |  |  |

${ }^{\frac{a}{a}}$ Standard uncertainties, $u$, are $u(T)=0.02 \mathrm{~K}, u(p)=0.002 \mathrm{MPa}$ for pressures up to 10 MPa and $u(p)=0.005$ MPa for pressures from $10-40 \mathrm{MPa}$, for $\mathrm{SO}_{2} u(z)=0.0001$ and for $\mathrm{CO}_{2} u(z)=0.0018$

Table 7 - Experimental results of the 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ system at $353 \mathrm{~K}^{\text {a }}$

| No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} . \mathrm{m}^{-3}$ |  | Z | No | Phase | T/K | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ |  | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Exp. | $u_{c}(\rho)$ |  |  |  |  |  | Exp. | $u_{c}(\rho)$ |  |
| 1 | SC | 352.98 | 39.330 | 850.5 | 0.3 | 0.71 | 45 | SC | 352.97 | 18.007 | 583.3 | 1.0 | 0.47 |
| 2 | SC | 352.98 | 39.300 | 850.2 | 0.3 | 0.71 | 46 | SC | 352.95 | 17.520 | 569.4 | 1.0 | 0.47 |
| 3 | SC | 352.97 | 39.009 | 848.1 | 0.3 | 0.71 | 47 | SC | 352.96 | 17.006 | 552.6 | 1.1 | 0.47 |
| 4 | SC | 352.97 | 38.520 | 845.7 | 0.3 | 0.70 | 48 | SC | 352.95 | 16.515 | 535.1 | 1.2 | 0.47 |
| 5 | SC | 352.98 | 38.023 | 842.1 | 0.3 | 0.69 | 49 | SC | 352.96 | 16.004 | 514.7 | 1.2 | 0.48 |
| 6 | SC | 352.97 | 37.499 | 838.7 | 0.3 | 0.69 | 50 | SC | 352.95 | 15.497 | 493.2 | 1.3 | 0.48 |
| 7 | SC | 352.96 | 36.996 | 835.2 | 0.3 | 0.68 | 51 | SC | 352.96 | 15.003 | 470.1 | 1.4 | 0.49 |
| 8 | SC | 352.97 | 36.496 | 831.8 | 0.3 | 0.67 | 52 | SC | 352.95 | 14.502 | 447.3 | 1.4 | 0.50 |
| 9 | SC | 352.98 | 36.013 | 828.1 | 0.3 | 0.67 | 53 | SC | 352.96 | 14.004 | 422.3 | 1.4 | 0.51 |
| 10 | SC | 352.97 | 35.510 | 824.7 | 0.3 | 0.66 | 54 | SC | 352.96 | 13.501 | 397.6 | 1.4 | 0.52 |
| 11 | SC | 352.97 | 35.014 | 821.4 | 0.4 | 0.65 | 55 | SC | 352.96 | 12.998 | 371.8 | 1.4 | 0.54 |
| 12 | SC | 352.98 | 34.563 | 818.1 | 0.4 | 0.65 | 56 | SC | 352.95 | 12.505 | 346.8 | 1.4 | 0.55 |
| 13 | SC | 352.97 | 34.055 | 814.5 | 0.4 | 0.64 | 57 | SC | 352.95 | 12.000 | 321.9 | 1.3 | 0.57 |
| 14 | SC | 352.96 | 33.519 | 809.8 | 0.4 | 0.63 | 58 | SC | 352.97 | 11.505 | 298.8 | 1.2 | 0.59 |
| 15 | SC | 352.96 | 33.014 | 805.8 | 0.4 | 0.63 | 59 | SC | 352.96 | 11.001 | 276.4 | 1.1 | 0.61 |
| 16 | SC | 352.97 | 32.552 | 802.4 | 0.4 | 0.62 | 60 | SC | 352.97 | 10.506 | 255.3 | 1.0 | 0.63 |
| 17 | SC | 352.96 | 31.993 | 797.6 | 0.4 | 0.62 | 61 | SC | 352.96 | 10.075 | 238.1 | 1.0 | 0.65 |
| 18 | SC | 352.95 | 31.494 | 793.2 | 0.4 | 0.61 | 62 | SC | 352.95 | 9.230 | 209.5 | 0.3 | 0.68 |
| 19 | SC | 352.96 | 31.058 | 789.4 | 0.4 | 0.60 | 63 | SC | 352.94 | 9.008 | 201.9 | 0.3 | 0.68 |
| 20 | SC | 352.97 | 30.512 | 784.7 | 0.4 | 0.60 | 64 | SC | 352.96 | 8.507 | 185.5 | 0.2 | 0.70 |
| 21 | SC | 352.96 | 29.991 | 779.0 | 0.4 | 0.59 | 65 | SC | 352.94 | 8.038 | 170.3 | 0.2 | 0.72 |
| 22 | SC | 352.96 | 29.492 | 773.9 | 0.4 | 0.58 | 66 | SC | 352.94 | 7.498 | 154.1 | 0.2 | 0.75 |
| 23 | SC | 352.97 | 29.001 | 768.7 | 0.4 | 0.58 | 67 | Gas | 352.94 | 7.017 | 140.9 | 0.2 | 0.76 |
| 24 | SC | 352.96 | 28.507 | 764.2 | 0.5 | 0.57 | 68 | Gas | 352.94 | 6.516 | 127.7 | 0.2 | 0.78 |
| 25 | SC | 352.96 | 28.006 | 758.3 | 0.5 | 0.57 | 69 | Gas | 352.93 | 6.001 | 114.8 | 0.2 | 0.80 |
| 26 | SC | 352.96 | 27.501 | 752.6 | 0.5 | 0.56 | 70 | Gas | 352.95 | 5.490 | 102.6 | 0.2 | 0.82 |
| 27 | SC | 352.98 | 27.043 | 747.4 | 0.5 | 0.55 | 71 | Gas | 352.95 | 4.997 | 91.5 | 0.1 | 0.84 |
| 28 | SC | 352.97 | 26.597 | 742.8 | 0.5 | 0.55 | 72 | Gas | 352.94 | 4.493 | 80.5 | 0.1 | 0.86 |
| 29 | SC | 352.96 | 26.036 | 736.4 | 0.5 | 0.54 | 73 | Gas | 352.94 | 4.003 | 70.6 | 0.1 | 0.87 |
| 30 | SC | 352.96 | 25.555 | 731.2 | 0.5 | 0.54 | 74 | Gas | 352.96 | 3.495 | 60.3 | 0.1 | 0.89 |
| 31 | SC | 352.95 | 25.002 | 723.7 | 0.5 | 0.53 | 75 | Gas | 352.95 | 3.009 | 51.0 | 0.1 | 0.90 |
| 32 | SC | 352.95 | 24.538 | 717.4 | 0.6 | 0.52 | 76 | Gas | 352.95 | 2.800 | 47.2 | 0.1 | 0.91 |
| 33 | SC | 352.96 | 24.023 | 710.4 | 0.6 | 0.52 | 77 | Gas | 352.94 | 2.504 | 41.8 | 0.1 | 0.92 |
| 34 | SC | 352.96 | 23.524 | 703.1 | 0.6 | 0.51 | 78 | Gas | 352.95 | 2.248 | 37.0 | 0.1 | 0.93 |
| 35 | SC | 352.95 | 23.011 | 694.8 | 0.6 | 0.51 | 79 | Gas | 352.95 | 2.002 | 33.0 | 0.1 | 0.93 |
| 36 | SC | 352.95 | 22.493 | 686.4 | 0.6 | 0.50 | 80 | Gas | 352.94 | 1.742 | 28.6 | 0.1 | 0.93 |
| 37 | SC | 352.95 | 21.993 | 677.2 | 0.7 | 0.50 | 81 | Gas | 352.95 | 1.507 | 24.3 | 0.1 | 0.95 |
| 38 | SC | 352.96 | 21.521 | 668.5 | 0.7 | 0.49 | 82 | Gas | 352.96 | 1.248 | 19.9 | 0.1 | 0.96 |
| 39 | SC | 352.96 | 20.999 | 657.9 | 0.7 | 0.49 | 83 | Gas | 352.96 | 0.982 | 15.1 | 0.1 | 1.00 |
| 40 | SC | 352.96 | 20.490 | 647.4 | 0.8 | 0.49 | 84 | Gas | 352.95 | 0.740 | 11.4 | 0.1 | 1.00 |
| 41 | SC | 352.96 | 20.014 | 636.9 | 0.8 | 0.48 | 85 | Gas | 352.95 | 0.511 | 7.6 | 0.1 | 1.03 |
| 42 | SC | 352.95 | 19.511 | 624.5 | 0.8 | 0.48 | 86 | Gas | 352.95 | 0.402 | 6.0 | 0.1 | 1.03 |
| 43 | SC | 352.96 | 19.011 | 611.7 | 0.9 | 0.48 | 87 | Gas | 352.95 | 0.306 | 4.6 | 0.1 | 1.02 |
| 44 | SC | 352.97 | 18.500 | 597.8 | 0.9 | 0.47 | 88 | Gas | 352.93 | 0.202 | 3.0 | 0.1 | 1.03 |

${ }^{\text {a }}$ Standard uncertainties, $u$, are $u(T)=0.02 \mathrm{~K}, u(p)=0.002 \mathrm{MPa}$ for pressures up to 10 MPa and $u(p)=0.005$ MPa for pressures from $10-40 \mathrm{MPa}$, for $\mathrm{SO}_{2} u(z)=0.0001$ and for $\mathrm{CO}_{2} u(z)=0.0018$

Table 8 - Uncertainties with $95 \%$ level of confidence $(k=2)$ for the measured densities of the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system

| $T / \mathrm{K}$ | Phase | Data <br> No. | Uncertainties $U(\rho)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Average |  | Max. |  |
|  |  |  | $\mathrm{kg} \cdot \mathrm{~m}^{-3}$ | \% | kg.m ${ }^{-3}$ | \% |
| 273 | Gas | 9 | 0.2 | 0.7 | 0.3 | 2.2 |
|  | Liquid | 77 | 0.3 | 0.0 | 0.5 | 0.1 |
|  | SC | 0 | 0.0 | 0.0 | 0.0 | 1.0 |
|  | Total | 86 | 0.3 | 0.1 | 0.5 | 2.2 |
| 283 | Gas | 17 | 0.2 | 0.8 | 0.7 | 4.1 |
|  | Liquid | 76 | 0.3 | 0.0 | 0.6 | 0.1 |
|  | SC | 0 | 0.0 | 1.0 | 0.0 | 1.0 |
|  | Total | 93 | 0.3 | 0.2 | 0.7 | 4.1 |
| 298 | Gas | 23 | 0.3 | 0.7 | 1.2 | 4.4 |
|  | Liquid | 68 | 0.4 | 0.0 | 0.9 | 0.1 |
|  | SC | 0 | 0.0 | 1.0 | 0.0 | 1.0 |
|  | Total | 91 | 0.3 | 0.2 | 1.2 | 4.4 |
| 323 | Gas | 15 | 0.1 | 0.4 | 0.2 | 1.4 |
|  | Liquid | 0 | 0.0 | 1.0 | 0.0 | 1.0 |
|  | SC | 70 | 0.6 | 0.1 | 2.7 | 0.6 |
|  | Total | 85 | 0.5 | 0.2 | 2.7 | 1.4 |
| 353 | Gas | 22 | 0.1 | 0.6 | 0.2 | 2.9 |
|  | Liquid | 0 | 0.0 | 1.0 | 0.0 | 1.0 |
|  | SC | 66 | 0.7 | 0.1 | 1.4 | 0.4 |
|  | Total | 88 | 0.5 | 0.2 | 1.4 | 2.9 |
| Total | Gas | 86 | 0.2 | 0.6 | 1.2 | 4.4 |
|  | Liquid | 221 | 0.3 | 0.03 | 0.9 | 1.0 |
|  | SC | 136 | 0.6 | 0.12 | 2.7 | 1.0 |
|  | Total | 443 | 0.4 | 0.2 | 2.7 | 4.4 |

Table 9 - Summarised AADs for the measured density of the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system

|  |  | Gas | Liquid | SC | Overall |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No of Exp. Data |  | 86 | 221 | 136 | 443 |
| Average | SRK | 2.4 | 8.2 | 9.6 | 7.4 |
| Absolute | PR | 1.8 | 3.2 | 2.4 | 2.6 |
| Deviation | VPT | 1.8 | 1.9 | 2.6 | 2.1 |
| $(\%)$ | $\mathrm{SRK-CO}_{2}$ | 1.9 | 0.6 | 0.8 | 1.0 |
|  | $\mathrm{PR-CO}_{2}$ | 1.7 | 0.7 | 1.1 | 1.0 |
|  | VPT-CO $_{2}$ | 2.2 | 0.7 | 1.1 | 1.1 |
|  | SRK-Peneloux $^{2}$ | 1.9 | 1.6 | 4.6 | 2.6 |
|  | PR-Peneloux | 1.9 | 1.1 | 3.8 | 2.1 |
|  | Multi parameter EoS | 1.6 | 0.2 | 0.6 | 0.6 |
| Maximum | SRK | 13.1 | 14.6 | 15.2 | 15.2 |
| Absolute | PR | 7.3 | 7.6 | 7.3 | 7.6 |
| Deviation | VPT | 7.3 | 8.0 | 7.5 | 8.0 |
| (\%) | SRK-CO $_{2}$ | 7.4 | 8.0 | 6.3 | 8.0 |
|  | PR-CO | 7.4 | 7.1 | 5.8 | 7.4 |
|  | VPT-CO | 7.4 | 7.2 | 5.6 | 7.4 |
|  | SRK-Peneloux | 8.5 | 9.3 | 11.9 | 11.9 |
|  | PR-Peneloux | 7.3 | 8.0 | 9.2 | 9.2 |
|  | Multi parameter EoS | 7.4 | 8.0 | 8.0 | 8.0 |

Table 10 - Specific heat capacity calculations for the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system ${ }^{\text {a }}$

| T/K | $p / \mathrm{MPa}$ | $\begin{gathered} \rho / \\ \mathrm{kg} \cdot \mathrm{~m}^{-3} \end{gathered}$ | $\begin{gathered} v / \\ \left(\mathrm{m}^{3} \cdot \mathrm{~mol}^{-1}\right) \end{gathered}$ | $\begin{gathered} C_{p}^{0} / \\ \left(\mathrm{J}^{-1} \cdot \mathrm{~mol}^{-1}\right) \end{gathered}$ | $\begin{gathered} C_{p \text { Exp }} / \\ \left(\mathrm{J} . \mathrm{K}^{-1} \cdot \mathrm{~mol}^{-1}\right) \end{gathered}$ | $\begin{gathered} U\left(C_{p}\right) / \\ \left({\left.\mathrm{J} . \mathrm{K}^{-1} \cdot \mathrm{~mol}^{-1}\right)}^{2}\right. \end{gathered}$ | $\begin{gathered} C_{p M P} / \\ \left(\mathrm{J} . \mathrm{K}^{-1} \cdot \mathrm{~mol}^{-1}\right) \end{gathered}$ | Dev./(\%) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 40 MPa |  |  |  |  |  |  |  |  |
| 273.55 | 40.023 | 1106.61 | $4.0671 \mathrm{E}-05$ | 36.08 | 76.66 | 0.14 | 77.75 | 1.4 |
| 283.33 | 40.145 | 1078.76 | $4.1721 \mathrm{E}-05$ | 36.34 | 76.54 | 0.15 | 77.88 | 1.8 |
| 298.11 | 40.060 | 1031.14 | $4.3648 \mathrm{E}-05$ | 37.08 | 76.92 | 0.16 | 78.25 | 1.7 |
| 322.48 | 40.153 | 953.87 | $4.7184 \mathrm{E}-05$ | 38.25 | 77.63 | 0.17 | 79.25 | 2.1 |
| 352.98 | 39.330 | 850.47 | $5.292 \mathrm{E}-05$ | 39.58 | 78.39 | 0.18 | 80.78 | 3.1 |
| 35 MPa |  |  |  |  |  |  |  |  |
| 273.54 | 35.043 | 1093.91 | $4.1143 \mathrm{E}-05$ | 35.83 | 80.66 | 0.17 | 78.90 | -2.2 |
| 283.32 | 34.989 | 1064.30 | $4.2288 \mathrm{E}-05$ | 36.34 | 81.21 | 0.18 | 79.29 | -2.4 |
| 298.10 | 35.077 | 1015.50 | $4.432 \mathrm{E}-05$ | 37.08 | 82.07 | 0.19 | 79.98 | -2.5 |
| 322.46 | 34.988 | 930.22 | $4.8383 \mathrm{E}-05$ | 38.25 | 83.86 | 0.20 | 81.85 | -2.4 |
| 352.97 | 35.014 | 821.42 | $5.4792 \mathrm{E}-05$ | 39.58 | 85.51 | 0.21 | 83.87 | -1.9 |
| 30 MPa |  |  |  |  |  |  |  |  |
| 273.55 | 30.026 | 1079.37 | $4.1697 \mathrm{E}-05$ | 35.83 | 82.95 | 0.20 | 80.32 | -3.2 |
| 283.32 | 30.008 | 1047.27 | $4.2976 \mathrm{E}-05$ | 36.34 | 83.82 | 0.21 | 81.00 | -3.4 |
| 298.11 | 30.013 | 996.85 | $4.5149 \mathrm{E}-05$ | 37.08 | 85.34 | 0.22 | 82.27 | -3.6 |
| 322.47 | 29.929 | 902.37 | $4.9877 \mathrm{E}-05$ | 38.25 | 88.50 | 0.24 | 85.43 | -3.5 |
| 352.96 | 29.991 | 778.96 | $5.7779 \mathrm{E}-05$ | 39.58 | 91.81 | 0.24 | 89.08 | -3.0 |
| 25 MPa |  |  |  |  |  |  |  |  |
| 273.55 | 25.039 | 1063.62 | $4.3152 \mathrm{E}-05$ | 35.83 | 87.42 | 0.26 | 82.09 | -6.1 |
| 283.32 | 25.025 | 1029.35 | $4.4009 \mathrm{E}-05$ | 36.34 | 88.89 | 0.28 | 83.20 | -6.4 |
| 298.10 | 25.050 | 975.15 | $4.6687 \mathrm{E}-05$ | 37.08 | 91.66 | 0.29 | 85.32 | -6.9 |
| 322.50 | 25.003 | 867.65 | $5.3224 \mathrm{E}-05$ | 38.26 | 97.26 | 0.31 | 90.70 | -6.7 |
| 352.95 | 25.002 | 723.72 | $6.4973 \mathrm{E}-05$ | 39.58 | 103.82 | 0.30 | 97.64 | -6.0 |
| 20 MPa |  |  |  |  |  |  |  |  |
| 273.56 | 20.028 | 1046.04 | $4.3026 \mathrm{E}-05$ | 35.83 | 91.74 | 0.42 | 84.42 | -8.0 |
| 283.32 | 20.038 | 1008.74 | $4.4617 \mathrm{E}-05$ | 36.34 | 93.99 | 0.43 | 86.19 | -8.3 |
| 298.11 | 20.051 | 948.90 | $4.7431 \mathrm{E}-05$ | 37.08 | 98.42 | 0.45 | 89.81 | -8.7 |
| 322.49 | 20.012 | 824.32 | $5.4599 \mathrm{E}-05$ | 38.26 | 109.99 | 0.46 | 99.90 | -9.2 |
| 352.96 | 20.014 | 636.90 | $7.0666 \mathrm{E}-05$ | 39.58 | 121.49 | 0.42 | 114.42 | -5.8 |
| 15 MPa |  |  |  |  |  |  |  |  |
| 273.57 | 14.951 | 1025.38 | $4.3893 \mathrm{E}-05$ | 35.83 | 102.28 | 0.92 | 87.64 | -14.3 |
| 283.32 | 15.011 | 984.11 | $4.5734 \mathrm{E}-05$ | 36.34 | 106.18 | 0.94 | 90.58 | -14.7 |
| 298.11 | 15.011 | 915.17 | $4.9179 \mathrm{E}-05$ | 37.08 | 115.12 | 0.94 | 97.28 | -15.5 |
| 322.52 | 15.012 | 753.20 | $5.9754 \mathrm{E}-05$ | 38.26 | 146.76 | 0.90 | 121.74 | -17.0 |
| 352.96 | 15.003 | 470.12 | $9.5734 \mathrm{E}-05$ | 39.58 | 143.82 | 0.98 | 141.94 | -1.3 |
|  |  |  | AAD (\%) |  |  | 0.37 |  | 5.8 |

[^1]Table 11 - Estimated bubble points from the measured densities for the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system ${ }^{\text {a }}$

| Type | Experimental |  |  |  |  | Prediction (PR-CO $\left.{ }_{2}\right)$ | Deviations (\%) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $T / \mathrm{K}$ | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $u_{c}(\rho) /$ <br> $\mathrm{kg} \cdot \mathrm{m}^{-3}$ | $p / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $p$ | $\rho$ |
| Bubble Point | 273.56 | 3.484 | 964.4 | 0.5 | 3.303 | 976.4 | -5.2 | 1.2 |
| Bubble Point | 283.33 | 4.304 | 908.4 | 0.6 | 4.221 | 929.2 | -1.9 | 2.3 |
| Absolute Average Deviation (AAD) (\%) |  |  |  |  |  | 3.6 | 1.8 |  |

${ }^{\text {a }}$ Standard uncertainties, $u$, are $u(T)=0.02 \mathrm{~K}, u(p)=0.002 \mathrm{MPa}$ for pressures up to 10 MPa


Figure 1 - Schematic diagram of the densitometer apparatus

1) Anton Paar DMA 512 densitometer, 2) High pressure fluid vessel, 3) Capillary Valve , 4)

Liquid bath (model: Lauda RE206), 5) Liquid bath of circuit (model: West P6100), 6)
Pressure transducers (model: Druck PTX611), 7) Temperature probes, 8) Vacuum pump, 9)
Neutralisation column, 10) Data acquisition unit, V1) Circuit valve, V2) Flow controlling ball valve, V3)Vacuum valve, V4) Venting valve, V5) Neutralisation valve


Figure 2 - Experimental and predicted densities of the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system. Experimental results: ( $\Delta$ ) 273.15 K, , $\left.^{*}\right) 283.15 \mathrm{~K}$, ( () 323.15 K and (■) 353.15 K for the $0.9503 \mathrm{~mole} \mathrm{CO}_{2}+0.0497 \mathrm{~mole} \mathrm{SO}_{2}$ and ( $\circ$ ) 298.15 K for the 0.9478 mole $\mathrm{CO}_{2}+0.0522 \mathrm{~mole}_{\mathrm{SO}_{2}}$. Lines: Predictions using the multi parameter EoS


Figure 3 - Low pressure experimental and predicted densities of the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system. Experimental results: $(\Delta) 273.15 \mathrm{~K},\left(^{*}\right) 283.15 \mathrm{~K},(\diamond) 323.15 \mathrm{~K}$ and (■) 353.15 K for the 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ and (○) 298.15 K for the 0.9478 mole $\mathrm{CO}_{2}+0.0522$ mole $\mathrm{SO}_{2}$. Lines: Predictions using the multi parameter EoS


Figure 4 - Deviations of the predictions using the multi parameter EoS from the measured data, ( $\Delta$ ) 273. $15 \mathrm{~K},\left(^{*}\right) 283.15 \mathrm{~K},(\diamond) 323.15 \mathrm{~K}$ and (■) 353.15 K for the $0.9503 \mathrm{~mole}_{\mathrm{CO}}^{2}+0.0497$ mole $\mathrm{SO}_{2}$ and (○) 298.15 K for the 0.9478 mole $\mathrm{CO}_{2}+0.0522$ mole $\mathrm{SO}_{2}$.


Figure 5 - Compressibility factor of the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system.
Experimental results: ( $\Delta$ ) $273.15 \mathrm{~K},\left(^{*}\right) 283.15 \mathrm{~K},(\diamond) 323.15 \mathrm{~K}$ and (■) 353.15 K for the 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ and (०) 298.15 K for the $0.9478 \mathrm{~mole}_{\mathrm{CO}}^{2}+0.0522$ mole $\mathrm{SO}_{2}$. Lines:

Predictions using the multi parameter EoS


Figure 6 - Compressibility factor of the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system.
Experimental results: ( $\Delta$ ) $273.15 \mathrm{~K},\left(^{*}\right) 283.15 \mathrm{~K},(\diamond) 323.15 \mathrm{~K}$ and (ロ) 353.15 K for the 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ and (०) 298.15 K for the $0.9478 \mathrm{~mole}_{2} \mathrm{CO}_{2}+0.0522$ mole $\mathrm{SO}_{2}$. Lines:

Predictions using the multi parameter EoS


Figure 7 - Specific heat capacity of the $\mathrm{CO}_{2}-\mathrm{SO}_{2}$ system ( 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ at $273.15 \mathrm{~K}, 283.15 \mathrm{~K}, 323.15 \mathrm{~K}$ and 353.15 K and 0.9478 mole $\mathrm{CO}_{2}+0.0522{\text { mole } \mathrm{SO}_{2} \text { at } 298.15 \mathrm{~K} \text { ): }}_{\text {: }}$
$(\bullet)$ calculated $\mathrm{C}_{\mathrm{p}}$ with $3 \%$ error, Lines: predictions using the multi parameter EoS


Figure 8 - Bubble point determination of 0.9503 mole $\mathrm{CO}_{2}+0.0497$ mole $\mathrm{SO}_{2}$ system for different isotherms, ( $\Delta$ ) $273.15 \mathrm{~K},\left({ }^{*}\right) 283.15 \mathrm{~K}$

## Appendix A

## Equation of State for pure sulphur dioxide [34]:

In this work, an industrial short equation from Lemmon \& Span was used to predict the thermodynamic properties of pure sulphur dioxide. The equation of state explicit in the Helmholtz energy is expressed in a fundamental form as below:

$$
\begin{equation*}
a(\rho, T)=a^{0}(\rho, T)+a^{r}(\rho, T) \tag{A-01}
\end{equation*}
$$

where $a(\rho, T)$ is the Helmholtz energy as function of density and temperature, $a^{0}(\rho, T)$ is the ideal gas contribution to the Helmholtz energy, and $a^{r}(\rho, T)$ is the residual Helmholtz energy due to the intermolecular forces. In the dimensionless form, the equation can be expressed as:

$$
\begin{equation*}
\frac{a(\rho, T)}{R T}=\alpha(\delta, \tau)=\alpha^{0}(\delta, \tau)+\alpha^{r}(\delta, \tau) \tag{A-02}
\end{equation*}
$$

where $\alpha(\delta, \tau)$ is the dimensionless Helmholtz energy as a function of dimensionless density, $\delta=\rho / \rho_{c}$, and dimensionless temperature, $\tau=T_{c} / T$.
The critical density and temperature of sulphur dioxide are $8.195 \mathrm{~mol}^{\mathrm{dm}}{ }^{-3}$ and 430.64 K , respectively.

The Helmholtz energy of the ideal gas is given by:

$$
\begin{equation*}
a^{0}=h^{0}-R T-T s^{0} \tag{A-03}
\end{equation*}
$$

Or, in the dimensionless form is given by:

$$
\begin{equation*}
\alpha^{0}=a_{1}+a_{2} \tau+\ln \delta+\left(c_{0}-1\right) \ln \tau-\frac{c_{1}\left(\frac{T_{c}}{K}\right)^{c_{2}}}{c_{2}\left(c_{2}+1\right)} \tau^{-c_{2}}+\sum_{k=1}^{5} v_{k} \ln \left[1-\exp \left(-u_{k} \tau / T_{c}\right)\right] \tag{A-04}
\end{equation*}
$$

The constants in the above equation is available in the following Table A-01 for pure sulphur dioxide.

The residual Helmholtz energy term can be find from the work of Span and Wagner for polar fluids including sulphur dioxide [55][56][57]:

$$
\begin{gather*}
\alpha^{r}(\delta, \tau)=n_{1} \delta \tau^{0.25}+n_{2} \delta \tau^{1.25}+n_{3} \delta \tau^{1.5}+n_{4} \delta^{3} \tau^{0.25}+n_{5} \delta^{7} \tau^{0.875}+n_{6} \delta \tau^{2.375} \exp ^{-\delta}+ \\
\quad n_{7} \delta^{2} \tau^{2.0} \exp ^{-\delta}+n_{8} \delta^{5} \tau^{2.125} \exp ^{-\delta}+n_{9} \delta \tau^{3.5} \exp ^{-\delta^{2}}+n_{10} \delta \tau^{6.5} \exp ^{-\delta^{2}}+ \\
n_{11} \delta^{4} \tau^{4.75} \exp ^{-\delta^{2}}+n_{12} \delta^{2} \tau^{12.5} \exp ^{-\delta^{3}} \tag{A-05}
\end{gather*}
$$

The constants $\mathrm{n}_{1}$ to $\mathrm{n}_{12}$ is also available in Table A-01.

Table A-01 - Constant values of the parameters in the Lemmon \& Span EoS

| Parameter | value | Parameter | value |
| :---: | :---: | :---: | :---: |
| $v_{l}$ | 1.0620 | $n_{l}$ | 0.93061 |
| $u_{l} / \mathrm{K}$ | 775.0 | $n_{2}$ | -1.9528 |
| $v_{2}$ | 1.9401 | $n_{3}$ | -0.17467 |
| $u_{2} / \mathrm{K}$ | 1851.0 | $n_{4}$ | 0.061524 |
| $v_{3}$ | 0 | $n_{5}$ | 0.00017711 |
| $u_{3} / \mathrm{K}$ | 0 | $n_{6}$ | 0.21615 |
| $v_{4}$ | 0 | $n_{7}$ | 0.51353 |
| $u_{4} / \mathrm{K}$ | 0 | $n_{8}$ | 0.010419 |
| $c_{0}$ | 4.0 | $n_{9}$ | -0.25286 |
| $c_{1}$ | $0.72453 \times 10^{-4}$ | $n_{10}$ | -0.054720 |
| $c_{2}$ | 1.0 | $n_{11}$ | -0.059856 |
| $a_{l}$ | -4.5328346436 | $n_{12}$ | -0.016523 |
| $a_{2}$ | 4.4777967379 |  |  |

## Equation of state for the mixtures [32][33][58]:

The Eos explicit in the Helmholtz energy in dimensionless form with the independent variables of reduced mixture density, $\delta=\rho / \rho_{r}(\bar{x})$, inverse reduced mixture temperature, $\tau=T_{r}(\bar{x}) / T$, and molar composition, $\bar{x}$, is expressed as below for the mixtures:

$$
\begin{equation*}
\frac{a}{R T}=\alpha(\delta, \tau, \bar{x})=\alpha^{0}(\rho, T, \bar{x})+\alpha^{r}(\delta, \tau, \bar{x}) \tag{A-06}
\end{equation*}
$$

The ideal gas part, $\alpha^{0}$, is given by:

$$
\begin{equation*}
\alpha^{0}(\rho, T, \bar{x})=\sum_{i=1}^{N} x_{i}\left[\alpha_{0, i}^{0}\left(\delta_{0, i}, \tau_{0, i}\right)+\ln x_{i}\right] \tag{A-07}
\end{equation*}
$$

where $N$ is the number of components in the mixture, $x_{i}$ is the mole fraction of component $i$, and $\alpha_{0, i}^{0}$ is the ideal gas part of the Helmholtz energy of component $i$ in the mixture. The reduced density and inverse reduced temperature for the pure components are given by:

$$
\begin{equation*}
\delta_{0, i}=\rho / \rho_{c, i} \quad \text { and } \quad \tau_{0, i}=T_{c, i} / T \tag{A-08}
\end{equation*}
$$

The residual part of the Helmholtz energy in Equation (A-06) is given by:

$$
\begin{equation*}
\alpha^{r}(\delta, \tau, \bar{x})=\sum_{i=1}^{N} x_{i} \alpha_{0, i}^{r}(\delta, \tau)+\Delta \alpha^{r}(\delta, \tau, \bar{x}) \tag{A-09}
\end{equation*}
$$

where $\alpha_{0, i}^{r}$ is the residual part of the reduced Helmholtz energy of component $i$ and $\Delta \alpha^{r}$ is the departure function given by:

$$
\begin{equation*}
\Delta \alpha^{r}(\delta, \tau, \bar{x})=\sum_{i=1}^{N-1} \sum_{j=i+1}^{N} x_{i} x_{j} F_{i j} \alpha_{i j}^{r}(\delta, \tau) \tag{A-10}
\end{equation*}
$$

where $\alpha_{i j}^{r}$ is the binary specific departure function and $F_{i j}$ is the weighing factor [59]. In this work, $F_{i j}$ is considered equal to zero.
The reducing functions $\rho_{r}(\bar{x})$ and $T_{r}(\bar{x})$ are also given by:

$$
\begin{equation*}
\frac{1}{\rho_{r}(\bar{x})}=\sum_{i=1}^{N} x_{i}^{2} \frac{1}{\rho_{c, i}}+\sum_{i=1}^{N-1} \sum_{j=i+1}^{N} 2 x_{i} x_{j} \beta_{v, i j} \gamma_{v, i j} \frac{x_{i}+x_{j}}{\beta_{v, i j}^{2} x_{i}+x_{j}} \frac{1}{8}\left(\frac{1}{\rho_{c, i}^{1 / 3}}+\frac{1}{\rho_{c, j}^{1 / 3}}\right)^{3} \tag{A-11}
\end{equation*}
$$

and

$$
\begin{equation*}
T_{r}(\bar{x})=\sum_{i=1}^{N} x_{i}^{2} T_{c, i}+\sum_{i=1}^{N-1} \sum_{j=i+1}^{N} 2 x_{i} x_{j} \beta_{T, i j} \gamma_{T, i j} \frac{x_{i}+x_{j}}{\beta_{T, i j}^{2} x_{i}+x_{j}}\left(T_{c, i} T_{c, j}\right)^{0.5} \tag{A-12}
\end{equation*}
$$

The binary parameters which allow for the arbitrary symmetric and asymmetric shapes of the functions were set as below:

$$
\begin{align*}
& \beta_{v, i j}=1.0 \quad \text { and } \quad \gamma_{v, i j}=1.0  \tag{A-13}\\
& \beta_{T, i j}=0.99686 \quad \text { and } \quad \gamma_{T, i j}=1.0093 \tag{A-14}
\end{align*}
$$

These parameters were adjusted on the available VLE data.


Figure A. 1 Pressure - composition diagram of the $\mathrm{CO}_{2}(1)+\mathrm{SO}_{2}$ (2) system. From Coquelet et al. [25]: ( O ), Liquid phase $\mathrm{T}=333.15 \mathrm{~K}$; ( $\bullet$ ), Vapour phase $\mathrm{T}=333.15 \mathrm{~K}$; ( $\diamond$ ), Liquid phase T $=263.15$ K. ( $*$ ), Vapour phase $T=263.15$ K; From Caubet [23] ( $\triangle$ ), Liquid Phase T $=333 \mathrm{~K}$; From this work : $(\bullet)$, Bubble point measured at $\mathrm{T}=283.33 \mathrm{~K},(\triangle)$, Bubble point
measured at $\mathrm{T}=273.56 \mathrm{~K}$. Black lines: calculated VLE lines using the multi parameter EoS. Dashed lines: calculated VLE lines using the PR-EoS model with $k_{i j}=0.02$.


[^0]:    ${ }^{a}$ No additional purification is carried out for all samples.
    ${ }^{\mathrm{b}}$ SM: Supplier method

[^1]:    ${ }^{\text {a }}$ Standard uncertainties, $u$, are $u(T)=0.02 \mathrm{~K}$ and $u(p)=0.005 \mathrm{MPa}$ for pressures from $10-40 \mathrm{MPa}$

