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Computational material design of filled rubbers using multi-objective design exploration

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ABSTRACT: The rubber materials of tires contain nano-fillers i.e. carbon black and silica for the improvement of tire performances. The mechanical properties of filled rubber depend on the morphology of fillers. In this work multi-objective design exploration (MODE) is applied to material design of filled rubbers to get the information between mechanical properties and morphological design variables. A multi-scale random model based on a Poisson point process is used to generate a simulation model of filled rubber, and FFT (fast Fourier transform) based scheme is applied to solve large-scale dynamic viscoelastic simulation. To get big data including Pareto solution for data mining, multi-objective genetic algorithm are conducted on TSUB-AME, supercomputer at Tokyo Institute of Technology. Data mining is employed to highlight properties-sensitive features in the microstructure. First, the volume fraction of bound rubber plays a major role in the material design of filled rubbers. Second, the radius of aggregates contributes to mechanical properties of filled rubbers.

1 INTRODUCTION

The rubber materials of tires contain nano-fillers i.e. carbon black and silica for the improvement of tire performances e.g. rolling resistance, wear and so on. The mechanical properties of filled rubber depend on the morphology of fillers. It is said that uniformly dispersed fillers are good to reduce loss tangent, however, guideline of material design to improve loss tangent, modulus and strength at the same time is not clear.

For clarification of the mechanism and origin of mechanical properties of filled rubbers, numerical simulation of filled rubbers has been conducted in the past few decades. Recently, large-scale simulation using the model generated by 3D-TEM (transmission electron microtomography) was conducted by Akutagawa et al. (2008) and Kadowaki et al. (2016) to compute effective material properties. Two-dimensional pattern reverse Monte Carlo analysis was performed to make structural model from the data obtained by time-resolved two-dimensional ultra-small angle x-ray scattering (Hagita et al. 2007 & Hagita et al. 2008). And to compute effective shear modulus, the complex multi-scale microstructure of filled rubber was generated numerically from a morphological model that was identified from statistical moments out of transmission electron microscopy images (Jean et al. 2011, for a simpler version).

The information on effective material properties and morphological design variables is helpful for the material design of filled rubbers. So, the objective of this work is to get the information using multi-objective design exploration (MODE). MODE has been already applied to tire design (Koishi et al.

2006 & Koishi et al. 2014). MODE consists of numerical simulation, multi-objective genetic algorithm and data mining technique, and is a methodology to discover an evolutionary idea for making technical innovation. However, to apply MODE to material design, especially morphological design of filled rubbers, there are two big issues i.e. simulation models in which morphology of fillers can be changed parametrically and large-scale viscoelastic simulation. In this study, the issues were solved using multi-scale random model based on Poisson point process and complex FFT (fast Fourier transform) based scheme proposed by Figliuzzi et al. (2016). In addition, MODE for the morphological design of filled rubbers was conducted on TSUBAME, supercomputer at Global Scientific Information and Computing Center in Tokyo Institute of Technology.

2 SIMULATION MODELS AND LARGE-SCALE DYNAMIC VISCO-ELASTIC SIMULATION

2.1 Morphology of filled rubbers and their feature value

This work concerns a rubber material reinforced by carbon black and silica particles as fillers, which are embedded in a matrix of rubber and can be geometrically well-approximated by spheres. A key feature of the material is that the rubber matrix is constituted of two distinct polymers: an exclusion polymer, which cannot contain any filler, and its complementary polymer, which can contain fillers. Fillers tend to agglomerate together within the rubber matrix. To analyze the rubbers microstructure, we dispose of a set of 50 TEM micrographs of size 1024 by 1024 pixels

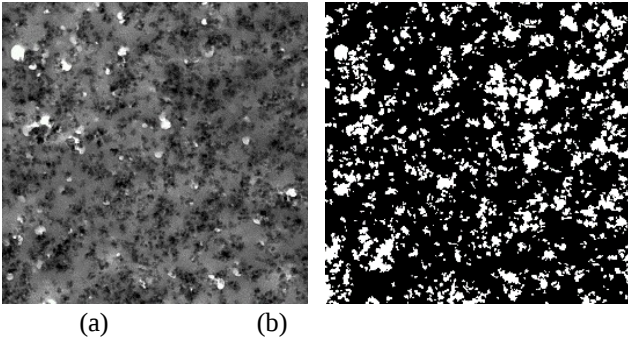


Figure 1. (a) Original TEM image of silica filled rubber, (b) segmented binary image showing the filler in white.

with resolution 2.13 nm per pixel. The slices of material probed by the microscope have a thickness around 40 nm. The first task is to segment these images, in order to identify the spatial distribution of the fillers as shown in Figure 1.

An efficient way to keep track of the information embedded in the segmented images is to rely on a morphological characterization of the material. In this work, the covariance and the granulometry of fillers are used as feature value of morphology. The covariance and the cumulative granulometry curve of silica fillers are shown in Figure 2. Using the covariance and the granulometry curves, we can select parameters for the identification of multi-scale random models as explained in the next section. This is important way to merge the information between real material and simulation model at a material design stage.

2.2 Multi-scale random model

A multi-scale random model is used to describe the microstructure (Figliuzzi et al. 2016) as shown in Figure 3. The first scale corresponds to the aggregates, while the second one describes more specifically

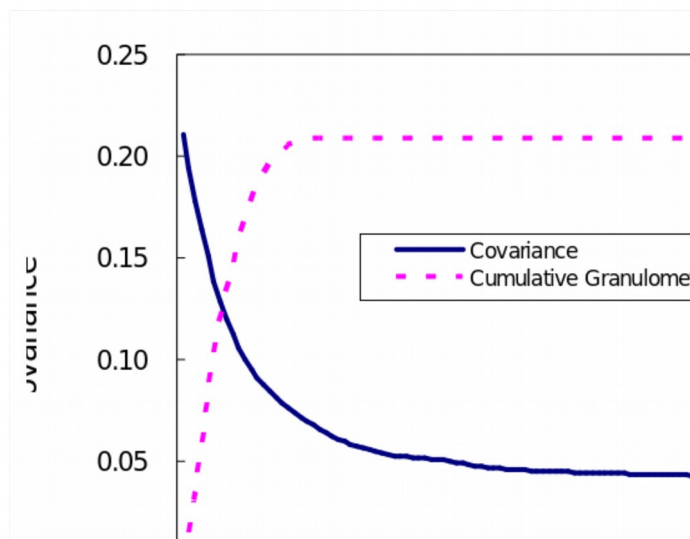


Figure 2. Covariance (solid line) and cumulative granulometry (broken line) computed from TEM image shown in Figure 1.

cally the single particles inside the aggregates. In addition, several alternatives can be considered to locate the aggregates outside of the exclusion polymer. Bound rubber in Figure 3 is the interface layer between polymer and filler. Morphological parameters of a multi-scale random model are followings;

- Poisson point intensity and volume fraction of exclusion polymer,
- Poisson point intensity and radius of aggregate,
- Poisson point intensity or volume fraction and radius of filler,
- Overlapping distance of fillers,
- Thickness of bound rubber.

These parameters can be used as design variables for parametric study, optimization and MODE. For example, cross sections of six 3D simulation models generated by multi-scale random modeling are shown in Figure 4. These models are generated with different Poisson point intensity and radius of aggre-

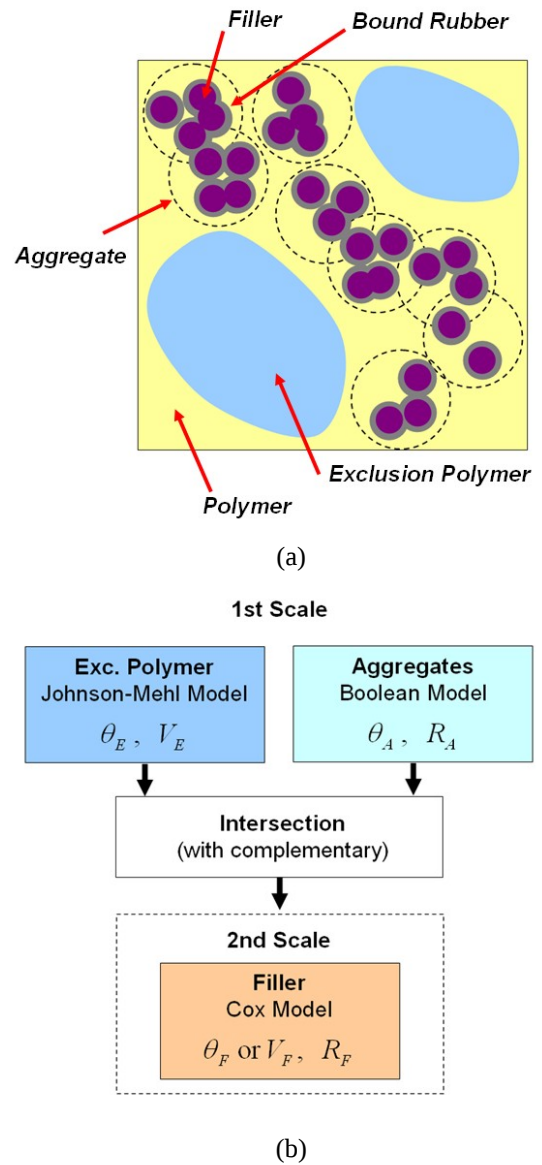


Figure 3. (a) Schematic figure of filled rubber constituted of two distinct polymers and (b) procedure of a multi-scale random model.

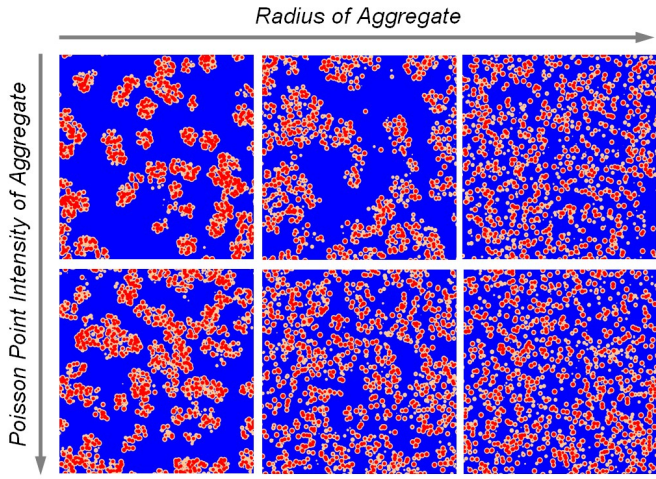


Figure 4. Cross section of six 3D simulation models generated with different Poisson point intensity and radius of aggregate, domain size: 1,000nm x 1,000nm x 1,000nm, the volume fraction of filler: 15%, the radius of filler: 10nm, the thickness of bound rubber: 5nm.

gate as design parameters, however, the volume fraction and radius of filler remain constant.

2.3 Computation of the effective dynamic viscoelastic properties using FFT-based scheme

According to our research, RVE (representative volume element) size of multi-scale random model should be 20 times larger than the radius of filler. And for sufficient resolution of bound rubber, the element size of the bound rubber should be smaller than its thickness. Moreover more than thousand computations should be done to get a Pareto solution using multi-objective genetic algorithm. Therefore, a fast simulation scheme is needed for large-scale dynamic viscoelastic problems. Though the homogenization procedure based on FEM for dynamic viscoelasticity is proposed by Koishi et al. (1997), a

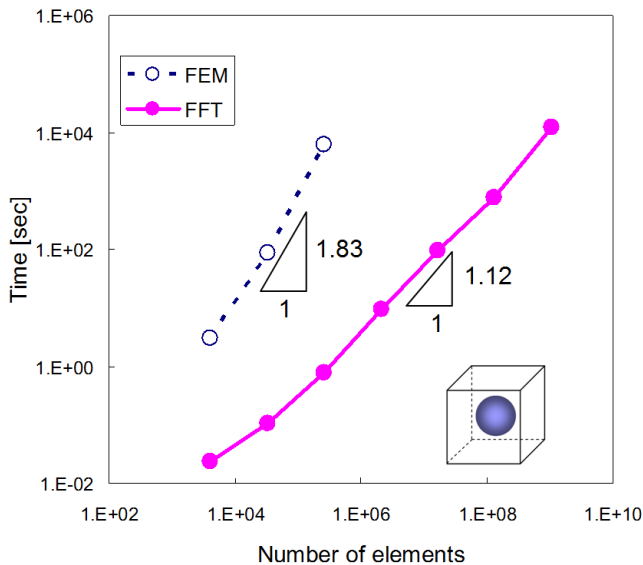


Figure 5. Computation time of the FFT-based scheme and FEM against the number of elements.

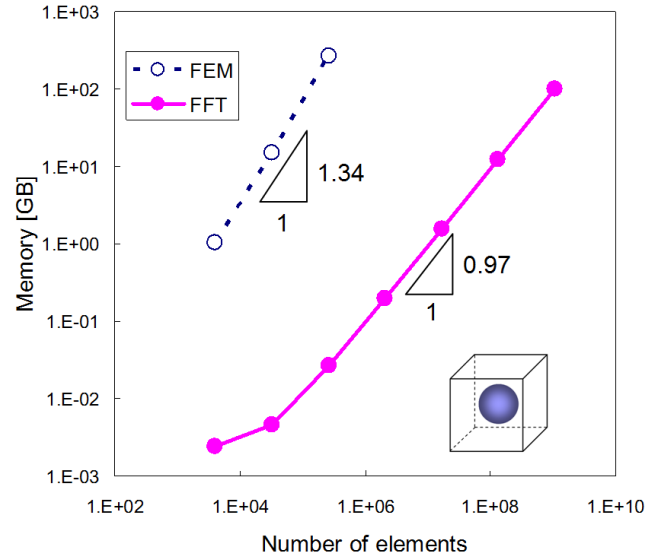


Figure 6. Required memory size of the FFT-based scheme and FEM against the number of elements.

FFT-based scheme (Figliuzzi et al. 2016 & Willot 2015) is used in this study.

Here, we demonstrate the efficiency of FFT-based scheme as a solver of large-scale problems. A single spherical filler embedded in rubber matrix shown in Figure 5 is considered for a benchmark test. Simulation models are discretized in uniform voxel mesh. The largest model consists of over 1 billion elements (1024x1024x1024 elements). Figure 5 and Figure 6 show computation time and required memory of the FFT-based scheme against the number of elements, respectively. Those of FEM are also shown in the same figures. Both of FFT-based scheme and FEM were run on 8 CPUs. The computational time and required memory size of the FFT-based scheme are almost proportional to the number of elements. The figures show that as the number of elements increases, the FFT-based scheme is much faster than FEM.

3 MULTI-OBJECTIVE DESIGN EXPLORATION FOR MORPHOLOGICAL DESIGN OF FILLED RUBBERS

3.1 Multi-objective design exploration (MODE)

The decision making in the real world depends on multiple criteria. Multiple criteria decision making is indispensable even in the design process of rubber materials of tires. So the material design of rubber is so-called multi-objective design optimization. The multi-objective design optimization is to find design variables which minimize or maximize each objective function i.e. mechanical properties of filled rubbers. Since some of objective functions have trade-off, a set of optimal solutions called Pareto solution is found out in the multi-objective optimization. We can obtain design information by clarifying the relationship between objective functions and design

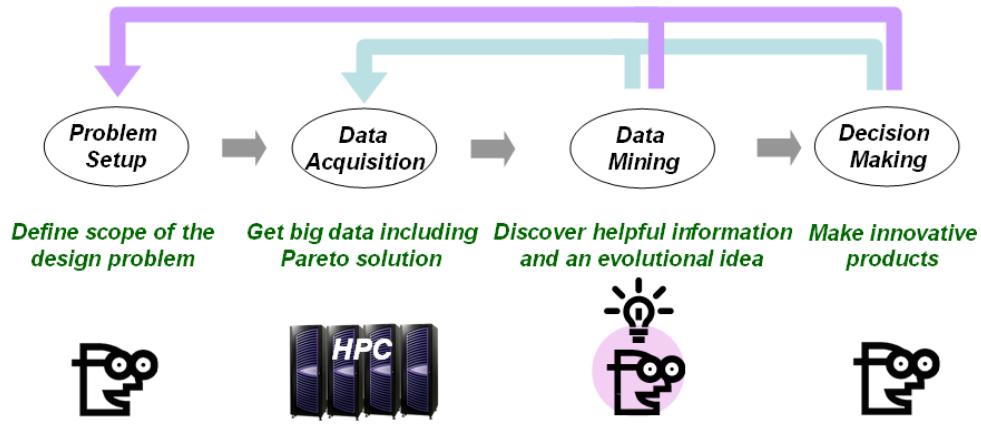


Figure 6. Procedure of multi-objective design exploration (MODE) to discover helpful information and an evolutionary idea for making new productions. HPC stands for high performance computing.

variables in design space including Pareto solutions. The information and the evolutionary idea inspired by the information are helpful for the multi-criteria decision making at material design stage.

MODE is a methodology to get helpful information between objective functions and design parameters using multi-objective optimization and data mining. From the information, we can find out an evolutionary idea for making new productions. Figure 7 shows procedure of MODE. Here the procedure of MODE consists of FFT-based scheme to simulate properties of filled rubber generated by multi-scale random model, evolutionary computation e.g. multi-

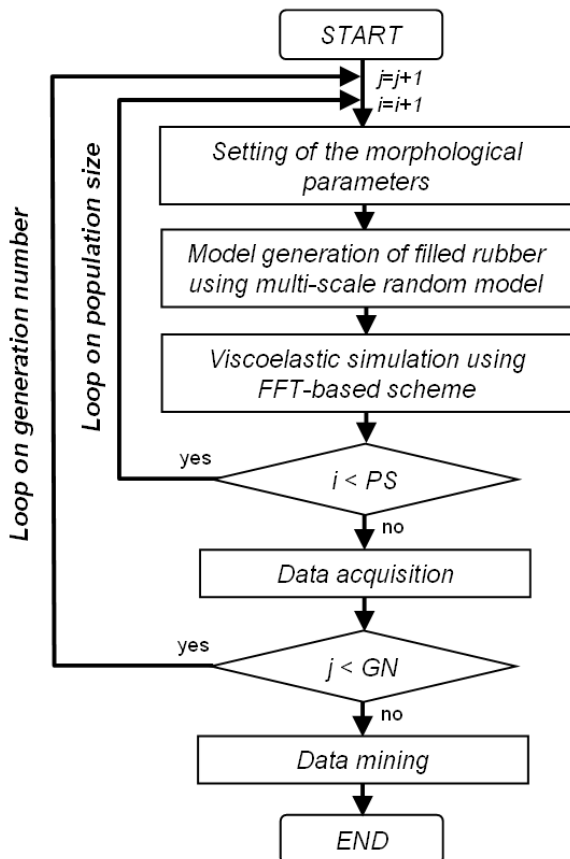


Figure 7. MODE for morphological design of filled rubbers. PS and GN stand for population size and generation number in multi-objective genetic algorithm.

objective genetic algorithm to get desirable solutions including Pareto solution, and data mining using self-organizing map (SOM) to find out morphological design information of filled rubbers as shown in Figure 7. Since the viscoelastic simulation of each individual can be conducted independently, parallel computing is effective in this study.

3.2 Problem set-up

The simulation model of the filled rubber which consists of three domain i.e. polymer, filler and bound rubber is considered here. Modulus of polymer, filler and bound rubber are 2MPa, 2000MPa and 20MPa, respectively. And loss tangent of polymer, filler and bound rubber are 0.05, 0.0 and 0.1, respectively. The radius of filler is 10 nm and the size of RVE is 500nm^3 . Figure 8 shows a simulation model which consists of 134 million elements ($512 \times 512 \times 512$ elements) to resolve the bound rubber of the thickness of 5nm.

The design variables are the following parameters that can change the morphology of filler;

- Poisson point intensity of aggregate,
- Radius of aggregate,
- Volume fraction of filler,
- Overlapping distance of fillers.

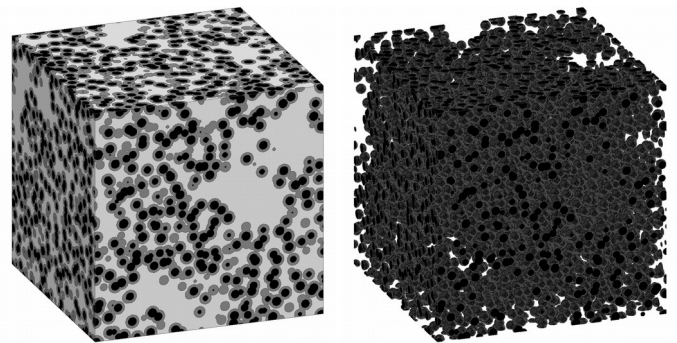


Figure 8. (a) 3D simulation model of filled rubber generated by multi-scale random model and (b) fillers embedded in the model. The number of elements is 134 million ($512 \times 512 \times 512$).

The objective functions are following;

- Effective loss tangent (to be minimized),
- Effective modulus (to be maximized),
- Average Mises stress in polymer domain (to be minimized),
- Standard deviation of Mises stress in polymer domain (to be minimized).

The last two objective functions are as indicators of resistance to wear. A multi-objective genetic algorithm, NSGA-II (Deb et al. 2000) is used to get data set including Pareto solution. The population size is 100, and the generation number is 40. Therefore, the computation of 4,000 large-scale models which consist of 134 million elements is carried out in this study.

3.3 Data mining using SOM (self-organizing map)

A sophisticated visualization technique is required to show high-dimensional objective functions and design parameters simultaneously. To visualize high-dimensional data, self-organizing map (SOM) proposed by Kohonen (1995) is employed in this work. SOM is one of the neural network model based on unsupervised and competitive learning. It provides a mapping with preserving topology from the high-dimensional space to two-dimensional plane, so called map. Although SOM does not remain the direction and distance in the original high-dimensional space, nearby points in the high-dimensional space are mapped to the nearby points on SOM. Roughly speaking, a relation between high-dimensional data and SOM is similar to the relation between the earth

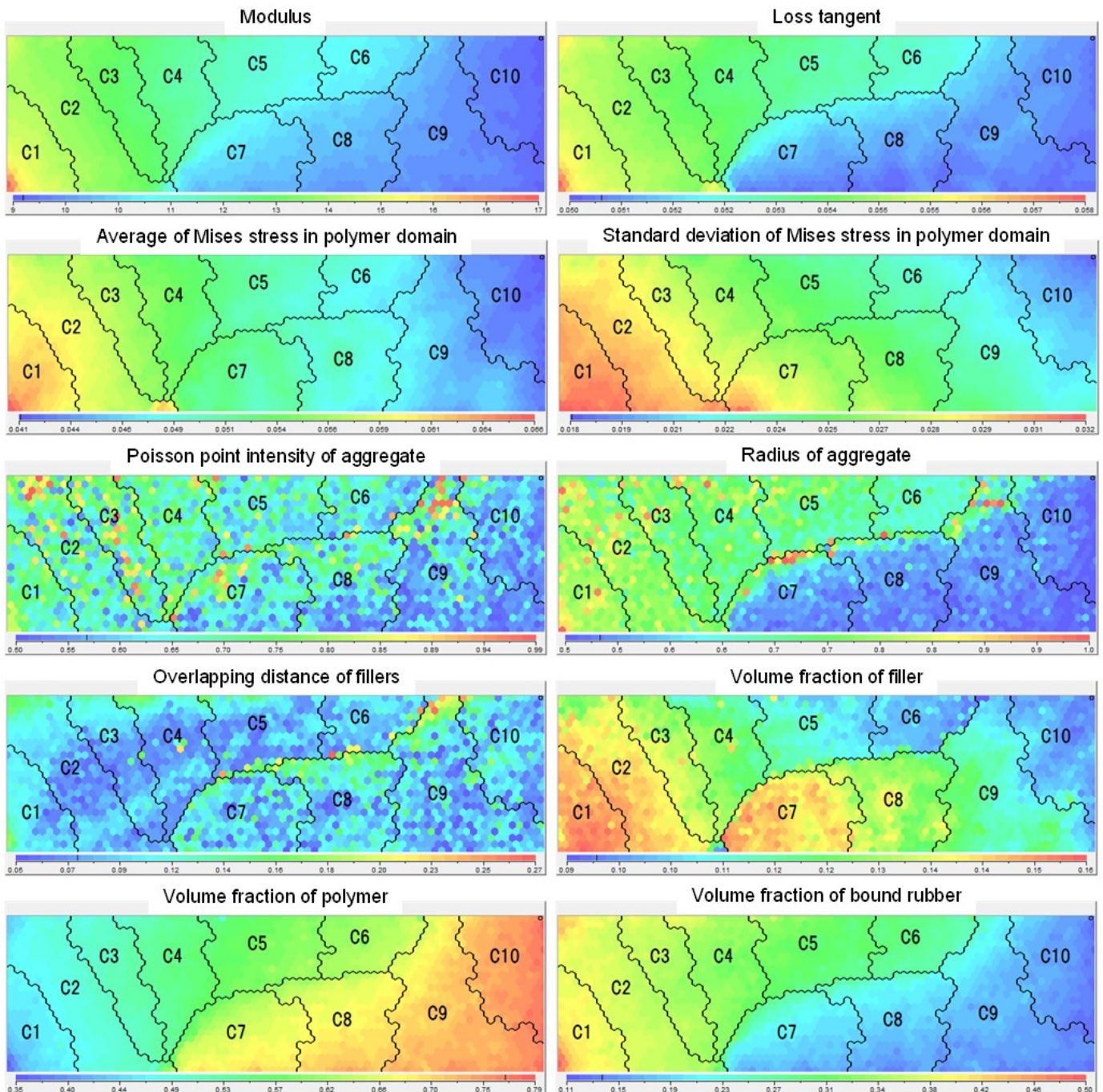


Figure 9. Contour plot of four objective functions, four design variables and two additional variables on the self-organizing map constructed using four objective functions.

and a world map. Nearby countries on the earth are mapped to nearby positions on a world map. SOM is useful not only for visualization of high-dimensional data but also for the cluster analysis for design problems in industry (Koishi et al. 2006 & Koishi et al. 2014).

Using NSGA-II, ten-dimensional data of about 4,000 models were obtained for data mining. Each data contains four objective functions and four design variables and two additional variables, volume fraction of polymer and that of bound rubber. Figure 9 shows the contour plot of four objective functions, four design variables and two additional variables on the same SOM generated using four-dimensional objective functions space.

Each map shown in Figure 9 is divided into ten clusters, C1-C10. The relation between each objective function can be understood visually by comparing upper four maps in this figure. It is shown that modulus (to be maximized) has a tradeoff with loss tangent (to be minimized). Cluster C10 is the best design domain on minimization of loss tangent. The desirable cluster to maximize modulus is C1. Furthermore, the figures show the correlation between average and standard deviation of Mises stress. According to visual data mining using Figure 9, we obtain the following results:

- The volume fraction of bound rubber, more than that of filler, greatly contributes to mechanical properties of filled rubbers,
- The radius of aggregate contributes to mechanical properties of filled rubbers.

4 CONCLUSIONS

For the morphological material design of filled rubbers, multi-objective design exploration based on multi-scale random model, FFT-based scheme, NSGA-II and self-organizing map was proposed in this work. The parametric models of morphology are generated using multi-scale random model. The FFT-based scheme has big advantage against FEM for large-scale viscoelastic simulation from the view points of time and memory size. For the MODE of filled rubbers, the computations of 4,000 large-scale models which consist of 134 million elements were carried out on TSUBAME, super computer at Tokyo Institute of Technology. As a result of data mining, the following conclusions are drawn. The volume fraction of bound rubber plays a major role in the material design of filled rubbers. Furthermore, the radius of aggregates contributes to mechanical properties of filled rubbers.

MODE for filled rubbers in which the rubber matrix is constituted of two distinct polymers will be studied in a next step.

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